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Printed for *James Hodges*, at the *Looking-glaſs* on *Lond*

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No *Art* can ſhow thee fully, but thine own.
Arithmetick, alone can ſhow,
f *Thanks*, we for thy *Labours* owe.

[redacted]

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The FORTY-EIGHTH EDITION, carefully Corrected and Amended.

By GEORGE FISHER, *Accompt.*
Licenſed *Sept.* 3. 1677. *Roger L'Eſtrange.*

LONDON: Printed for *A. Betteſworth*, and *C. Hitch*,
at the *Red-Lyon* in *Pater-noſter-Row*; *Ware*, at the
Sun and *Bible* in *Amen-Corner*; and *Hodges*, at the
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TO his much honoured Friends *Manwaring Davies* of the *Inner Temple*, Eſq; and Mr. *Humphry Davies* of St. *Mary Newington-Butts*, in the County of *Surrey*.

John Hawkins, as an Acknowledgment of unmerited Favours; humbly dedicated this *Manual of Arithmetick*.

To the READER.

Courteous Reader,

I Having had the Happineſs of an intimate Acquaintance with Mr. *Cocker* in his Life time, often ſollicited him to remember his Promiſe to the World, of publiſhing his *Arithmetick*; (but for Reaſons beſt known to himſelf) he refuſed it; and after his Death (the Copy falling accidently into my Hand) I thought it not convenient to ſmother a Work of ſo conſiderable a Moment, not queſtioning but it might be as kindly accepted, as if it had been preſented by his own Hand. The Method is familiar and eaſy, diſcovering as well the Theorick as the Practick of that neceſſary Art of *Vulgar Arithmetick*. And in this new Edition there are many remarkable Alterations for the Benefit of the Teacher or Learner, which I hope will be very acceptable to the World; I have alſo performed my Promiſe, in Publiſhing the *Decimal Arithmetick*, which finds Encouragement to my Expectation, and the Bookſellers too. I am thine to ſerve the.

BRITISH MUSEUM 30 DEC 68

John Hawkins.

Mr. *Edward Cocker's*

PROEME *or* PREFACE.

BY the ſecret Influence of Divine Providence, I have been inſtrumental to the Benefit of many, by Virtue of theſe uſeful Arts. Writing *and* Engraving: *And do now with the ſame wonted Alarcity, caſt this my Arithmetical Mite into the publick Treaſury, beſeeching the Almighty to grant the like Bleſſing to theſe as to my former Labours.*

Seven Sciences ſupremly excellent,
Are the chief Stars in *Wiſdom*'s Firmament:
Whereof *Arithmetick* is one, whoſe Worth
The Beams of Profit and Delight **ſhine** forth;
This crowns the reſt, this makes Man's Mind compleat,
This treats of Numbers, and of this we treat.

I have been often deſired by my intimate Friends, to publiſh ſomething in this Subject, who, in a pleaſing Freedom have ſignified to me, that they expected it would be extraodinary. How far I have anſwered their Expectation, I know not; but this I know, That I have deſigned this Work not extraordinary abſtruſe or profound; but have, by all Means poſſible, within the Circumference of my Capacity, endeavoured to render it extraordinary uſeful to all thoſe, whoſe Occaſions ſhall indue them to make uſe of Numbers, *If it be objected, that the Books already publiſhed, treating of* Numbers, *are innumerable; I anſwer, That's but a ſmall Wonder, ſince the Art is infinite. But that there ſhould be ſo many excellant Tracts of* Practical Arithmetick *extant, and ſo little practiſed, is to me a great Wonder knowing that as* Merchandize *is the Life of the Weal publick, ſo* Practical Arithmetick *is the Soul of* Merchandize. *Therefore I do ingeniouſly profeſs, That in the Beginning of this Undertaking, the numerous Concerns of the honoured*

Merchant firſt poſſeſſeth my Conſideration: And how far I have accommodated this Compoſure for his moſt worthy Service, let his own profitable Experience be Judge.

Secondly, *For your Service, moſt excellent Profeſſions, wh Underſtandings ſoar to the Sublimity of the Theory and Practice of this noble Science, was this Arithmetical Tractate compoſed; which you may pleaſe to employ as a Monitor to inſtruct your young* Tyroes, *and thereby take Occaſion to reſerve your precious Moments, which might be exhauſted that Way, for your more important Affairs.*

Thirdly, *For you the ingenious Off-ſpring of happy Parents, who will willingly pay the full Price of Induſtry and Exerciſe for thoſe Arts and choice Accompliſhments, which may contribute to the Felicity of your future State: For you, I ſay (ingenious Practioners) was this Work compoſed, which may prove the Pleaſure of your Youth, and the Glory of your Age.*

Laſtly, *For you the pretended Numariſts of this Vapuring Age, who are more diſingeouſly witty to propound unneceſſary Queſtions, than ingeniouſly judicious to reſolve ſuch as are neceſſary; for you was this Book compoſed and publiſhed, if you will deny your ſelves ſo much as not to invert the Streams of your Ingenuity, but by ſtudiouſly conferring with the Notes, Names, Orders, Progreſs, Species, Properties, Proprieties, Proportions, Powers, Affections, and Applications of* Numbers *delivered herein, become ſuch Artiſts indeed, as you now only ſeem to be. This* Arithmetick *ingeniouſly obſerved, and diligently practis'd, will turn to good Accompt to all that ſhall be concerned in Accompts; ſince all its Rules are grounded on Verity, and delivered with Sincerity; the Examples built up gradually from the ſmalleſt Conſideration to the greateſt; and all the Problems or Propoſitions, well weighed, pertiment and clear, and not one of them throughout the Tract, taken upon Truſt, therefore now,*

Zoilus and *Momus*, lie you down and die,
For theſe Inventions your whole Force defie.

Edward Cocker.

BRITISH MUSEUM 30 DEC 68

Courteous READER.

BEing well acquainted with the deceaſed Author, and finding him knowing and ſtudious in the Myſteries of Numbers and Algebra, of which he had ſome choice Manuſcripts, and a great Collection of printing Authors in ſeveral Languages, I doubt not but he hath writ his Arithmetick ſuitable to his own Preſace, and worthy Acceptation, which I thought fit to certify, on a Requeſt to that Purpoſe, made that him that wiſheth thy Welfare, and the Progreſs of Arts.

John Collins.

Novemb. 27. 1677.

* * *

This Manual of Arithmetick *is recommended to the World by Us whoſe Names are ſubſcribed,* viz.

Mr. John Collens
Mr. James Atkinſon
Mr. Peter Perkins
Matth
Mr. Rich. Lawrence, *Sen.*
Mr. Eleazar Wigan
Mr. Rich. Noble *of Guilford*
Mr. William Norgate

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Mr. Benj. Tichbourn
Mr. Joſeph Symmonds
Mr. Jerem. Miles
Mr. Joſiah Cuffley
Mr. John Hawkins

And generally Approved by all Ingenious Artiſts.

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CHAP.

CHAP. I.

Notation of Numbers.

A*Rithmetick* is an Art of Numbering or Knowledge, which teacheth to Number well. And there are diverſe Species and Kinds of *Arithmetick* and *Geometry*, the which we do intend to treat of n order, applying the Principles of the one to the Defini-ion of the other. For as Greatneſs is the Subject of *Geometry*, ſo Number is the Subject of *Arithmetick*; and if , then their firſt Principles and chief Fundamentals muſt ave like Definitions; or, at leaſt ſome Congruency.

2. Number is that, by which the Quantity of any Thing s expreſſed or numbered; as the Unit is the Number by vhich the Quantity of the Thing is expreſſed or ſaid to be ne, and two by which it is named two, and ½ half, by vhich it is named or called half, and the Root of 3, by vhich it is called the Root of 3, the like of any other.

3. Hence it is that Unit is Number; for the Part is of he ſame Matter that is his whole, the Unit is part of the Iultitude of Units, therefore the Unit is of the ſame Iatter, that is the Multitude of Units; but the Matter f the Multitude of Units is Number; therefore the Iatter of Units is Number; or elſe, if from a Number iven no Number but ſubtracted, the Number given re-aineth; as ſuppoſe 3 the given Number, if as ſome ſuppoſe, 1 be no Number, then if you ſubtract 1 from 3, here muſt remain 3 ſtill; which is very abſurd.

4. Hence it will be convenient to examine from whence umber hath its Riſe or Beginning. Moſt Authors main-ain, that Unit is the Beginning of Number, and it ſelf no umber; but looking upon the Principles and Definitions n the firſt Rudiments of Geometry, we ſhall find that the

Definition of a Point is in no way congurous with the Definition of an Unit in Arithmetick; and therefore One or Unit muſt be in the Bounds or Limits of Number, and conſequently the Beginning of Number is not to be found in the Number 1; wherefore making Number and Magnitude congruent in Principles, and like in Definitions, we make and conſtitute a Cypher to be the Beginning of Number, or rather the Medium between increaſing and decreaſing Numbers, commonly called abſolute or whole Numbers, and negative and fractional Numbers, between which nothing can be imagin'd more agreeable to the Definition of a Point in Geometry; for as a Point is an Adjunct of Line, and itſelf no Line, ſo is (0) Cypher an Adjunct of Number, and it ſelf no Number: And as a Point in Geometry cannot be divided or increaſed into Parts; ſo likewiſe (0) cannot be divided or increaſed into Parts; for as many Points, though in Number infinite, do make no Line, ſo many (0) Cyphers, though in Number infinite, do make no Number. For the Line A B cannot be increaſed be the Addition of the Point C, neither the Number D be increaſed by the Addition of the (0) Cypher E; for if you add nothing to 6, the Sum will be 6, (0) Cypher neither increaſing nor diminiſhing the Number; but if it be granted that A B be extended or prolonged to the Point C, ſo that A C be made a continued Line, then A B is increaſed by the Addition of the Point C. In like manner, if we grant D (6) be prolonged to E (0), ſo that D E (60) be a continued Number, making 60, then 6 is augmented by the Aid of (0) as conſtituting the Number (60) Sixty; and furthermore that 1 or Unit is material, and a Number, and that (0) is the Beginning of Number, is proved by all Authors, although directly; for the Tables and Signs and Tangents prove one Degree to be a Number, becauſe the Sine of 1 Degree is 174524, (the Radius being 10000000) and the Beginning of the Table is (0), and it anſwereth 00000, *&c.*

A——B
C

D 6
E 0
—
Sum 6

A—B—C

D E|60
6 0|

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5. Hence it is that Numbers is not Quanity diſcontinued for that which is but one Quantity, is not Quantity diſjunct: (60) Sixty, as it is a Number, is one Quantity, *viz.* one Number (60) Sixty; therefore as it is a Number, it is not Quantity diſjunct, for Number is ſome ſuch Thing in Magnitude, as Humidity in Water: for as Humidity extends it ſelf though all and every Part of Water, ſo Number related to Magnitude, do extend it ſelf through all and every Part of Magnitude. Alſo, as continued Water doth anſwer a continued Humidity, ſo to a continued Magnitude doth anſwer a continned Number. As the continued Humidity of an intire Water, ſuffereth the ſame Diviſion and Diſtinction that his Water doth; ſo the continued Number ſuffereth the ſame Diviſion and Diſtinction that his Magnitude doth. And thus much concerning the Definition and Principles of Number and Magnitude. We come now to treat of,

6. The Characters Notes by which Numbers are ſignified, or by which a Number is ordinarily expreſſed; and they are theſe, *viz*, (0) Cypher or Nothing, 1 One, 2 Two, 3 Three, 4 Four, 5 Five, 6 Six, 7 Seven, 8 Eight 9 Nine. The Cypher, which though of it ſelf it expreſſeth not any certain or known Quantity, yet is the Beginning or Root of Number, and the other 9 Figures are called ſignificand Figures or Digits.

7. In Number of any Sort, two Things are to be conſidered, *viz. Notation and Numeration.*

8. *Notation* teacheth how to deſcribe any Number by certain Notes and Charecters, and to declare the Value thereof being ſo deſcribed, that is by Degrees and Periods.

9. A Degree conſiſts of three Figures, *viz.* Of three Places, comprehending Units, Tens, and Hundreds, ſo 265 is a Degree, and the firſt Figure (5) on the right Hand, ſtands ſimply for his own Value, being Units, or ſo many Ones, *viz.* Five; the ſecond in order from the Right, ſignifies as many times Ten as there are Units contained in it, *viz.* Sixty; the Third in the ſame Order ſignifies ſo many Hundreds as it contains Units, ſo will the Expreſſion of the Number be Three hundred ſixty five, &c.

10. A Period is when a Number conſiſts of more than 3 Figures or Places, and whoſe proper Order is to prick

every third Place, beginning at the right Hand, and ſo on to the Left; ſo the Number 6 452 being given, it will be diſtinguiſhed thus, 633,452, and expreſſed thus; Sixty three thouſand, four hundred fifty two; likewiſe 4,571, 236, 782, being diſtinguiſhed as you ſee, will be expreſſed thus; Four thouſand, five hundred ſeventy eight Millions, two hundred thirty ſix thouſand, ſeven hundred eighty two.

11. Number is either abſolute or Negative,

12. Abſolute or intire, Whole, increaſing Number, is that by which annexing another Figure or Cypher, it becomes ten times as much as it ſtood for before; and if two Figures or Cyphers be annexed, it make an hundred times as much as it ſtood for before, &c. As if you annex to the Figure 6 a Cypher, then it will be (60) Sixty; ſo if two Cyphers are annexed, then it will be (603) Six hundred, and if you do annex to it (4) Four, then it will be (64) Sixty four: and if you annex (78) Seventy eight, it will be then (678) Six hundred ſeventy eight, &c.

13. A Negative, or broken, Fractional, Decreaſing Number, is that which by perfixing a Point or Prick toward the left Hand, its Value has decreaſed from ſo many Units, to ſo many tenth Parts of any Thing; and if a Point and (0) Cypher, or Digit, be prefixed, it will be then ſo many hundred Parts; and if a Point and two Cyphers or Digits be prefixed, its Value is decreaſed to be ſo many thouſand Parts; as if you would prefix before the Figure 3 a Point (.) or Prick thus (.3), it is then decreaſed from 3 Units or 3 Integers, to 3 tenth Parts of an Unit or an Integar: And if you prefix a Point and Cypher thus (.03,) it is decreaſed from 3 Integars to 3 hundred Parts of an Integar; and by this Means 5 *l.* abſolute, by prefixing of a Point, will be decreaſed to 5 *l.* negative, which is 5 tenth Parts of a Pound, equal in Value to 10 Shillings, and ſo by prefixing of more Cyphers or Digits its Value is decreaſed in a decuple Porportion *ad infinitum*. As in the following Scheme, or rather Order of Numbers, we have placed (0) Cypher in its due Place and Order, as it is in the Beginning and Medium of Number; for going from (0) towards the left Hand, you deal with intire, abſolute, whole, increaſing Numbers.

In

Increaſing Numbers. Decreaſing Numbers.

29	876	543	256	2 1 0 1 2	345	678	976	3
mm mm mm mm X	mmm mmm CX	mmm mmm CX	mmm	CXUXC	mmm XC	mmm mmm XC	mmm mmm mmm XC	m m m

But going from (o) the Place of Units towards the right Hand, you meet with broken, negative, fractional, and decreaſing Numbers. And hence it follows, that *Multiplication* increaſeth the Product in abſolute Numbers, but decreaſeth the Product in negative Numbers. Alſo Diviſion decreaſeth the Quotient in whole Numbers, and increaſeth it in negative fractional Numbers.

14. An abſolute, intire, whole, increaſing Number, hath always a Point annexed towards the right Hand; and therefore,

15. A negative, broken, decimal, decreaſing Number, hath always a Point perfixed towards the left Hand. When we expreſs Integers or whole Numbers, as 5 *Pounds*, 5 *Feet*, 26 *Men*, we uſually annex a Point or Prick after
l. feet. men. inch.
the Number thus, 5. 5. 26. 347.
But when we expreſs Decimals, or Numbers that are denied to be intire, or decreaſing Numbers, we do commonly prefix a Point or Prick before the ſaid Decimal or decreaſing Number thus (3), that is three Tenths, or 3 Primes; (.03) that is 3 Hundredths, or 3 Seconds.

16. A whole or abſolute Number is a Unit, or a compoſed Multitude of Units, and it is either a Prime or elſe a compound Number.

17. Prime Numbers amongſt themſelves, are thoſe which have no Multitude of Units for a common Meaſure, as 8 and 7, or 10 and 13, becauſe not any Multitude of Units can equally meaſure or divide them without a Remainder.

18. Compound Numbers amongſt themſelves, are thoſe which have a Multitude of Units for a common Meaſurer, as 9 and 12, becauſe 4 meaſures them exactly, and abbreviates them to three and four.

19. A broken Number commonly called a Fraction, is a Part or Parts of a whole Number, *viz.* A Part of an Integar, as $\frac{1}{3}$ one Third, is one third Part of an Unit.

20. A broken Number or Fraction, conſiſts of 2 Parts, *viz.* the Numerator and Denominator.

21. The Numerator and Denominator of a Fraction, and ſet one over the other, with a Line between them; and the Numerator is ſet above the Line, and expreſſeth the Parts therein contained.

22. The Denominator of a Fraction, is the inferior Number placed below the Line, and expreſſeth the Number of Parts, into which the Unit or Integer is divided; and let $\frac{3}{4}$ be the Fraction given, ſo ſhall 3 be the Numerator, and doth expreſs or Number the Multitude of Parts contained in this Fraction, for $\frac{3}{4}$ is a Fraction compounded of Fourths or Quarters, and the Figure 3 in numbering ſhews us, that in that Fraction there are 3 of the 4th Parts or Quarters; alſo in the ſame Fraction $\frac{3}{4}$ is the Denominator, and doth expreſs the Quality of the Fraction, *viz.* that the whole or Integar is divided into 4 equal Parts.

23. A broken Number is either Proper or Improper; *viz.* proper when the Numerator is leſs then the Denominator, for $\frac{3}{4}$ is a perfect proper Fraction, but an improper Fraction hath its Numerator greater, or at leaſt equal to the Denominator, thus $\frac{13}{8}$ is an improper Fraction, the Reaſon is in given in the Definition.

24. A proper broken Number, is either Simple or Compound, *viz.* Simple when it hath one Denomination, and Compound when it conſiſteth of divers Denominations; if $\frac{3}{4}$ $\frac{6}{12}$ $\frac{25}{100}$ were given, we ſay, they are each of them Single or Simple Fractions, becauſe they conſiſt but of one Numerator, and one Denominator: but if $\frac{3}{4}$ of $\frac{2}{12}$ of $\frac{35}{100}$ of a Pound Sterling were given, we ſay that it is a compound broken Number or Fraction, becauſe the Expreſſion and Repreſentation conſiſteth of more Denominations than one; and ſuch by ſome are called Fraction or Fractions; they have always this Particle (of) between them.

25. When a ſingle broken Number or Fraction hath for his Denominator a Number conſiſting of a Unit in the firſt Place towards the left Hand, and nothing but Cyphers from the Unit towards the right Hand, it is then the more

aptly and rightly called a decimal Fraction; under this Head are all our decreaſing Numbers placed, and in our 13 the Definition, called Negatives; and by the Order there preſcribed, we order them to be Decimals, by ſigning a Prick or Point before them, or the Numerator, rejecting the Denominator: Therefore according to our laſt Rule, $\frac{5}{10}$ $\frac{5}{100}$ $\frac{25}{1000}$ and the ſaid to be Decimals; and a Decimal Fraction may be expreſſed without its Denominator (as before) by prefixing a Point or Prick before the Numerator of the ſaid Fraction, and then ſhall the former Fractions 25 $\frac{5}{10}$ and $\frac{25}{1000}$ ſtand thus, 5, and 025.-

But oftentimes, as in the ſecond and Fourth Fractions $\frac{5}{100}$ and $\frac{25}{1000}$, a Prick or Point will not do without the Help of a Cypher or Cyphers perfixed before the ſignificant Figures of the Numerator, and therefore when the Numerator of a decimal Fraction conſiſteth not of ſo many Places as the Denominator hath Cyphers, fill up the void Places of the Numerator with perfixing Cyphers before the ſignificant Figures of the Numerator, and then ſign for a Decimal, ſo ſhall $\frac{5}{100}$ be .05, and $\frac{25}{1000}$ will be .025, and $\frac{72}{10000}$ will be .0072. Now by this we may eaſily diſcover the Denominator having the Numerator for always the *Denominater* of any decimal Fraction conſiſts of ſo many Cyphers, as the Numerator hath Places, with an Unit prefixed before the ſaid Cypher, *viz.* under the Point or Prick.

26. A decimal Number or Fraction, is expreſſed by Primes, Seconds, Thirds, Fourths, *&c.* and is a Numbers decreaſing. Here inſtead of natural and common Fractions, as $\frac{3}{4}$ of a Thing, we order the Thing or Integar into Primes, Seconds, Thirds, Fourths, Fifths, *&c.* that our Expreſſion may be conſonant to our former Order.

27. In decimal Arithmetick, we always imagine that all intire Units, Integars, and Things, are divided firſt into ten equal Parts, and theſe Parts ſo divided we call Primes; and Secondly, we divide alſo each of the former Primes, into other ten equal Parts, and every one of theſe Diviſions we call Seconds; and Thirdly, we divide each of the ſaid Seconds into ten other equal Parts, and thoſe ſo divided, we call Thirds; and ſo by decimating the former, and ſubdecimating theſe latter, we run on *ad infinitum.*

28. Let a Pound *Sterling*, *Troy-weight*, *Averdupois-weight*, *Liquid-meaſure*, *Dry-meaſure* *Long-meaſure*, *Time*, *Dozen*, or any other Thing or Integer be given to be decimally divided; In this Notion promiſed, we ought to let the firſt Diviſion be Primes, the next Diviſion Seconds, the next Thirds, &c. So one Pound Sterling being 20 Shillings, when divided into ten equal Parts, the Value of each Part will be 2 Shillings, therefore one Prime of a Pound Sterling will ſtand thus (.1), which is in Value 2 Shillings; 3 primes will ſtand thus (.3), and that is in value 6 Shillings. Again, a Prime or .1 being divided into ten equal Parts, each of thoſe Parts will be one Second, and is thus expreſſed (01) and its Value will be found 2 *d.* Farthing, and $\frac{6}{10}$ of a Farthing; and ſo will .05 ſignify one Shilling or five Seconds. And if .01 be divided into ten other equal Parts, each of thoſe Parts ſo divided will be Thirds, and will ſtand thus .001, and its Value will be found to be 96 of a Farthing, or $\frac{96}{100}$ of a Farthing, and .009 Thirds will be 2*d.* and .64 of a Farthing, or $\frac{64}{100}$ of a Farthing &c. So that .375, will be found to repreſent 7 *s.* 6 *d.* for the 3 Primes are 6 Shillings, and the 7 Seconds are 1 *s.* 4 *d.* and $\frac{2}{13}$ of a Penny, and the 5 Thirds are 1 Penny, $\frac{8}{10}$ of a Penny, both which added together make 7 *s.* 6 *d.*

29. If you put any Bulk or Body, repreſenting an Integer, if it be decimally divided, then the Parts in the firſt Decimation are Primes, the next Seconds and the next Decimation is Thirds, the next Fourths, &c. As let there be given a Bullet of Lead, or ſuch like, whoſe Weight let it be 50 *l.* *Troy*, this is called a Unit, Integer, or Thing; then will the like Weight and Matter make 10 other the which together will be equal to 50 *l.* and will weigh each of them 5 *l.* a-piece; take of the ſame Matter, and equal to 5 *l.* make 10 more, then each of thoſe weigh 6 Ounces a-piece; alſo, if again, you take 6 Ounces, and thereof make 10 other ſmall Bullets, each of them will weigh 12 Penny-weight *Troy*; and thus have you made Primes, Seconds, and Thirds, in Reſpect of the Integer, containing 50 *l.* *Troy-weight*; ſo that 5 Prime is equal to the half Maſs and 2 Primes, and 5 Seconds, is a Quarter of the Maſs, and therefore one of the firſt Diviſion,

2 of the ſecond Diviſion, and 5 of the third Diviſion, will be equal in Weight to half a Quarter of the Maſs, and contains 6 *l.* 3 Ounces.

30. When a Decimal Fraction followeth a whole Number, you are to ſeperate or part the Decimal from the whole Number by a Point or Prick; ſo if 75 followed the whole Number 32, ſet them thus, 32.75. You ſhall find that diverſe Authors, have diverſe ways in expreſſion mixt Numbers, as thus, 32|75, or 32|$\frac{75}{100}$, or $32|\ddot{75}$, but you will find that 32.75 thus placed and expreſſed, is the fitteſt for Calculation.

31. A mixt Number hath two Parts, the whole, and the broken; the whole is that which is compoſed of Integars and the broken is a Fraction annexed thereunto. So the mixt the Number, $36\frac{8}{12}$ being given, we ſay, that 36 is the whole Number, which is compoſed of Integers; and the $\frac{8}{12}$ is the broken Number annexed, which ſheweth that one of the former Integers (of that 36) being divided into 12 Parts $\frac{8}{12}$ doth expreſs 8 of thoſe 12 Parts more, belonging to the ſaid 36 Integers.

32. Denominative Numbers are of one, or of many; and thoſe are of diverſe Sorts and Kinds, *viz.* Singular called Unit, as 1; and Plural a Multitude, as 2, 3, 4, 5; Single, of one kind only called Digits, as 1, 2, 3, 4, 5, 6, 7, 8, 9; and Compounds of many, 10, 11, 12, *&c.* 102, 367, *&c.*

Proportional, as Single, Multiple, Double, Triple, Quadruple, *&c.* Denominate, as Pounds, Shillings, Pence; Undenominate, as 1, 2, 3, *&c.* Perfect, as 6, 28, 496, 8128, 130816, 2096128, *&c.* whoſe Parts are equal to the Numbers; imperfect unequal, and more than the Sum, as 12, to 1, 2, 3, 4, 6; imperfect, unequal, and more than the Sum, as 8 to 1, 2, 4. Numbers Commenſurable, becauſe 3 meaſures them both; but 16 and 17 are Incommenſurable, becauſe no one commom Number or Meaſure can meaſure them; Linear, in form of a Line, as .. ... Superficial, in Form of a Superficies or Plane, as :::::: or : :, *&c.* and Number cubical or ſolid, in Form of a
. :
Cube. Thoſe two Latter are otherwiſe called Figurative Numbers: There are alſo other Number called Tabu-

lar, and Sines, Tangents, Secants, *&c.* Others that be called Logarithmetick, or borrow'd Numbers, fitted to Proportion for Eaſe, and ſpeedy Calculation of all manner of Queſtions.

CHAP. II.

Of the Natural Diviſions of Integers, and the ſeveral Denominations of the Parts.

1. AND that we may advance methodically herein, we will begin with the main Pillars on which Arithmetick is founded, *viz.* the ſeveral Species of that Art; But firſt,

Of Money, Weights, &c.

2. The leaſt Denomination or Fraction of Money uſed in *England* is a Farthing, from which is produced the following Table, called the Table of Coin, *&c.*

1 Farth.	make	1 Farthing
4 Farth.		1 Penny
12 Pence.		1 Shilling
20 Shil.		1 Pound

And therefore,

l.	*s.*	*d.*	*qrs.*
1	20	12	4
1	20	240	960
	1	12	48
		1	4

The Firſt of theſe Tables, *viz.* that on the Left Hand is plain and eaſy to be underſtood, and therefore wants no Direction. In the ſecond Table above the Line, you have 1 *l.* 20 *s.* 12 *d.* 4 *qrs.* whereby is meant, That a Pound is equal to 20 Shillings, and 1 Shilling is equal to 12 Pence, and 1 Penny equal to 4 Farthings; under the Line is 1 *l.* 20 *s* 240 *d.* 960 *qrs.* which ſignifies 1 *l.* to contain 20 Shillings, or 240 Pence, or 960 Farthings; in the ſecond Line below that is 1 *s.* 12 *d.* 48 *qrs.* the Firſt ſtanding under the Denomination of Shillings, whereby is to be noted, that 1 Shilling is equal to 12 Pence or 48 Farthings; and likewiſe that below that, one Penny is equal in Value to four Farthings; underſtand the like Reaſon in the following Tables of Weight, Meaſure, Time, Motion, and Dozen.

Of Troy Weight.

3. The leaſt Fraction or Denomination of Weight uſed in *England*, is a Grain of Wheat gathered out of the Middle of the Ear, and well dried; from whence are produced theſe following Tables of Weight, called *Troy Weight.*

32 Grains of Wheat	make	24 Artificial Grains
24 Artificial Grains		1 Penny-weight
20 Penny-weight		1 Ounce
12 Ounces		1 Pound Troy-weight.

And therefore,

l.	*own.*	*p. w.*	*grains.*
1	12	20	24
1	12	240	5760
	1	20	480
		1	24

Troy Weight ſerveth only to weigh Bread, Gold, Silver, and Electuaries; it alſo regulateth and preſcribeth a Form how to keep the Money of *England* at a certain Standard.

Of Apothecaries Weight.

4. The *Apothecaries* have their Weights deduced from *Troy Weight*, a Pound *Troy* being the greateſt Integer, a Table of whoſe Diviſion aud Subdiviſion followeth, *viz.*

And therefore,

			l.	*oun.*	*drams*	*ſcrup.*	*gr.*
1 Pound	make	12 Ounces	1	12	8	3	20
1 Ounce		8 Drams	1	12	96	288	5760
1 Dram		3 Scruples		1	8	24	480
1 Scruple		20 Grains			1	3	60
						1	20

5. Thus much concerning *Troy Weight*, and its Derivative Weights; beſides which, there is another Kind of Weight uſed in *England*, known by the Name of *Averdupois Weight*, (1 Pound of which is equal to 14 Ounces 12 Penny-weight *Troy-weight*) and it ſerveſt to weigh all Kinds of Grocery-wares, and alſo Butter, Cheeſe, Fleſh, Wax, Tallow, Reſin, Pitch, Lead, *&c.* the Taple of which is as followeth.

A Table of Averdupois-Weight.

4 Quarters of a Dram	make	1 Dram
16 Drams		1 Ounce
16 Ounces		1 Pound
28 Pounds		1 Quarter of a Hundred
4 Quarters		1 Hund. Weit. or 112 *l.*
20 Hundred		1 Tun,

And therefore,

Tun	*C.*	*qr.*	*l.*	*oun.*	*drams*	*qrs.*
1	20	4	28	16	19	4
1	20	80	2240	35040	573440	2293760
	1	4	112	1792	28672	114688
		1	28	448	7168	28672
			1	16	256	1024
				1	16	64
					1	4

Wool is weighed with this Weight, but only the Diviſions are not the ſame.

7 Pounds	make	1 Clove
2 Cloves		1 Stone
2 Stones		1 Todd
6 Todd 1 Stone		1 Wey
2 Weys		1 Sack
12 Sacks		1 Laſt.

And therefore,

laſt	*ſack*	*way*	*todd*	*ſtone*	*cloves*	*l.*
1	12	2	6½	2	2	7
1	12	24	150	312	624	4368
	1	2	13	26	52	364
		1	6½	13	26	182
			1	2	4	28
				1	2	14
					1	7

Note, That in ſome Countries the Wey is 256 *l.* *Averdupois*, as in the *Suffolk* Wey; but in *Eſſex* there is 336 *l.* in a Wey.

6. The leaſt denominative Part of Liquid Meaſure is a Pint, which was formerly taken from *Troy-weight*, (1 Pound of Wheat *Troy-weight* making a Pint of Liquid Meaſure) but ſince, by a late Act of Parliament, to prevent Fraud in the Exciſe, the Pint Beer Meaſurs is to contain 35 $\frac{1}{4}$ ſolid Inches, and the Pint Wine 28 $\frac{7}{8}$ the like Inches, &c.

A Table of Liquid Meaſure.

35 $\frac{1}{4}$ Cubical Inches	make	1 Pint Beer Meaſure
28 $\frac{7}{8}$ Cubical Inches		1 Pint Wine Meaſure
2 Pints		1 Quart
2 Quarters		1 Pottle
2 Pottles		1 Gallon
8 Gallons		1 Firkin of Ale, Soap, or Beer
9 Gallons		1 Firkin of Beer
10 Gallons and half		1 Firkin of Salmon or **Eels**
2 Firkins		1 Kilderkin
2 Kilderkins		1 Barrel
42 Gallons		1 Terce of Wine
63 Gallons		1 Hogſhead
2 Hogſheads		1 Pipe or Butt
2 Pipes or Butts		1 Tun of Wine

And therefore,

Tun's	*pipes*	*hhds.*	*gall.*	*pints*
1	2	2	63	8
1	2	4	252	2016
	1	2	126	1008
		1	63	504
			1	8

7. The leaſt denominative Part of dry-Meaſure is alſo a Pint, and this is likewiſe taken from *Troy-weight*.

A Table of Dry Meaſure.

1 Pound *Troy*	make	1 Pint
2 Pints		1 Quart
2 Quarts		1 Pottle
2 Pottles		1 Gallon

Gallons

2 Gallons	make	1 Peck
4 Pecks		1 Buſhel
2 Buſhels		1 Comb
2 Combs		1 Quarter
2 Quarters		1 Chaldren
5 Quarters		1 Wey
3 Weys		1 Laſt.

And therefore,

laſt	*way*	*qrs.*	*com.*	*buſh.*	*pecks*	*gall.*	*pints*
1	2	5	2	4	4	2	8
1	2	10	20	80	320	940	5120
	1	5	10	40	160	320	2560
		1	2	8	32	65	512
			1	4	16	32	256
				1	4	8	64
					1	2	16
						1	8

8. The leaſt Denominative Part of Long-meaſure is a Barly-corn well dried, and taken out of the Middle of the Ear, whoſe Table of Parts followeth.

3 Barly-corns	make	1 Inch
12 Inches		1 Foot
3 Feet		1 Yard
3 Feet 9 Inches, or a Yard and a Quarter		1 Ell *Engliſh*
6 Feet		1 Fathom
5 Yards and a Half		1 Pole, Perch, or Rod
40 Poles or Perches		1 Furlong
8 Furlongs		1 *Engliſh* Mile.

And therefore,

mile	*furl.*	*poles*	*yards*	*feet*	*inches*	*barly-corn*
1	8	40	5½	3	12	3
1	8	320	1760	5280	63360	190080
	1	4	220	660	7920	23760
		1	5½	16½	198	594
			2	3	36	108
				1	12	36
					1	3

And note, that the Yard, as alſo the Ell, is uſually divided into Quarters, and each Quarter into 4 Nails.

Note alſo, That a Geometrical Pace is 5 Feet, and there are 1056 ſuch Paces in an *Engliſh* Mile.

9. The Parts of the ſuperficial Meaſures of Land are ſuch as are mentioned in the following Table, *viz.*

A Table of Land Meaſure.

40 Square Poles or Perches	make	1 Rood, or Quarter or an Acre
4 Roods		1 Acre.

By the foregoing *Table of Land Meaſure*, you are informed what a Pole or Perch is; and by this, that 40 ſquare Perches is a Rood. Now a ſquare Perch is a Superficies very aptly reſembled by a ſquare Trencher, every Side thereof being a Perch of 5 Yards and Half in Length, 40 of them is a Rood, and 4 Roods an Acre. So that a Superficies, that is 40 Perches long, and 4 Broad, is an Acre of Land, the Acre containing in all 160 ſquare Perches.

10. The leaſt denominative Part of Time, is one Minute, the greateſt Integer being a Year, from whence is produced this

Table of Time.

1 Minute	make	1 Minute
60 Minutes		1 Hour
24 Hours		1 Day natural
7 Days		1 Week
4 Weeks		1 Month
13 Months, 1 day, 6 hours		1 Year.

But the Year is uſually divided into twelve unequal Calendar Months, whoſe Names, and the Number of Days they contain, are as follows, *viz.*

	Days		Days
January	31	*July*	31
February	28	*Auguſt*	31
March	31	*Septemb.*	30
April	30	*October*	31
May	31	*Novemb.*	30
June	30	*Decemb.*	31

So that the Year containeth 365 Days, and 6 Hours; but the 6 Hours are not reckoned, but only every fourth Year, and then there is a Day added to the latter End of *February*, and then it containeth 29 Days; and that Year is called Leap-Year, and containeth 366 Days.

And here note, That as the Hour is divided into 60 Minutes, ſo each Minute is ſub-divided into 60 Seconds, and each Second into 60 Thirds, and each Third into 60 Fourths, *&c.*

The Tprophical Year, by the exacteſt Obſervation of the moſt accurate Aſtronomers, is found to be 365 Days, 5 Hours, 49 Minutes,, 4 Seconds, and 21 Thirds.

CHAP. III.

Of the Species or Kinds of Arithmetick.

THere are ſeveral Species of this Art; and which may be termed either Natural, Artificial, Analtycal, Algebraical, Lineal, or Inſtrumental: But what we are now to treat upon, relates to the ſingle Parts of Natural Arithmetick, ſo far as concerns Numeration; of which there are alſo four Kinds, viz. *Addition*, *Subtraction*, *Multiplication*, and *Diviſion*.

CHAP. IV.

Additions of Whole Numbers.

1. A*Ddition* is the Reduction of two or more Numbers, of like Kind, together into one Sum or Total: Or, it is that by which diverſe Numbers are added together, to the End that the Sum or Total Value of them all may be diſorvered.

The firſt Number in every *Addition* is called the *Addible Number*; the other, the *Number* or *Numbers* added; and the *Number* invented by the *Addition*, is called the *Aggregate* or *Sum*, containing the Value of the *Addition*.

The Collation of the Numbers, is the right placing the Numbers given reſpectively to each Denomination, and the Operation is the artificial adding of the Numbers given together, in order to the finding out of the Aggrevate or Sum.

2. In *Addition* place the Numbers given reſpectively the one above the other, in ſuch ſort, that the like Degree, Place, or Denomination, may ſtand in the ſame Series, *viz.* Units under Units, Tens under Tens, Hundreds under Hundreds, *&c.* Pounds under Pounds, Shillings

under Shillings, Pence under Pence, &c. Yards under Yards, Feet under, &c.

3. Having thus placed the Number given (as before) and drawn a Line under them, add them together, beginning with the leſſar Denomination, *viz.* at the right Hand; and ſo on, ſubſcribing the Sum under the Line reſpectively: As for Example,

Let there be given 3352, and 213, 133, to be added together: I ſet the Units in each particular Number under each other, and ſo Likewiſe the Tens under the Tens, &c. and draw a Line under them, as in the Margent; then I begin at the Place of Units, and add them together upwards, ſaying 3 and 3 are 6, and 2 makes 8, which I ſet under the Line, and under the ſame Figure added together; then I proceed to the next Place, being the Place of Tens, and add them in the ſame Manner as I did in the Place of Units, ſaying, 3 and 1 are 4, and 5 are 9, which likewiſe ſet under the Line reſpectively; then I go to the Place of Hundreds, and add them up as I did the other, ſaying, 1 and 2 are 3, and 3 are 6, which is alſo ſet under the Line; and laſtly, I go to the Place of Thouſands, and becauſe there are another Figures to add to the 3. I ſet it under the Line in its reſpective Place, and ſo the Work is finiſhed; and I find the Sum of the 3 given Numbers to be 3698.

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3352
 213
 133
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3968
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4. But if the Sum of the Figures of any Series exceedeth Ten, or any Number of Tens, ſubcribe under the ſame the Exceſs above the Tens, and for every Ten carry one, to be added to the next Series towards the Left Hand, and ſo go on till you have finiſhed your Addition; always remembring, that how great ſoever the Sum of the Figures of the laſt Series is, it muſt all be ſet down under the Line reſpectively. So 3678 being given to be added to 2357, I ſet them down as is before directed, and as you ſee in the Margent, with a Line drawn under them, then I begin and add them together, ſaying, 7 and 8 are 15, which is 5 above 10, wherefore I ſet 5 under the Line, and carrry 1 for the 10 to be added to the next Series, ſaying, 1 that I carried and 5 is 6, and 7 are 13, wherefore I ſet down 3,

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3678
2357
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6035
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and carry 1 (for the Ten) to the next Series; then I ſay, 1 that I carried and 3 are 4, and 6 are 10, now, becauſe it comes to juſt 10, and no more, I ſet 0 under the Line, and carry 1 from the 10 to the next, and ſay, 1 that I carried and 2 are 3, and 3 are 6, which I ſet down in its reſpective Place; thus the Addition is ended, and the Total Sum of theſe Numbers is found to be 6035. Several Examples of this Kind follow.

Numbers to be added
354867
573846
785946
347205
Sum 2061864

Numbers to be added
748647
465834
76483
648400
Sum 1939364

Numbers to be added
45346
38074
8437
923
76
Sum 92856

5. If the Numbers given to be added, are contained under diverſe Denominations, as of *Pounds. Shillings*, *Pence*, and *Farthings*; or of *Tuns*, *Hundreds*, *Quarters*, *Pounds*, &c. Then in this Caſe, having diſpoſed of the Numbers of each Denominations under other of the like kind; beginning at the leaſt Denomination (minding how many of one Denomination do make an Integer in the next) and having added them up, for every Integer of the next greater Denomination that you find therein contained, bear an Unit in Mind to be added to the ſaid next greater Denomination, expreſſing the Exceſs reſpectively under the Line; proceed in this Manner until your Addition be finiſhed; the following Example will make the Rule plain to the Learner. Thus theſe following Sums being given to be added, *viz.* 136 *l.* 13 *s.* 4 *d.* 2 *qrs.* and 79 *l.* 07 *s.* 10 *d.* 3 *qrs.* and 33 *l.* 18 *s.* 09 *d.* 1 *qr.* alſo 15 *l.* 09 *s.* 05 *d.* 0 *qrs.* The Numbers being diſpoſed according to Order, will ſtand as in the Margent. Then I begin at the Denomination of Farthings, and add them up, ſaying, 1

and

l.	*s.*	*d.*	*qrs.*
136—	13—	04—	2
79—	07—	10—	3
33—	18—	09—	1
15—	09—	05—	0
265—	09—	05—	2

and 3 are 4 and 2 makes 6. Now I conſider that ſix Farthings are 1 Penny 2 Farthings; wherefore I ſet down the 2 Farthings in its place under the Line; and keep 1 in Mind to be added to the next Denomination of Pence: Then I go on, ſaying, 1 that I carried and 5 are 6, and 9 are 15 and 10 are 25, and 4 are 29; now I conſider that 29 Pence are 2 Shillings and 5 Pence, therefore I ſet down 5 Pence in order under the Line, and keep 2 in Mind for the 2 Shillings to be added to the Shillings; then I go on, ſaying, 2 that I carried and 9 are 11, and 18 are 29, and 7 are 36, and 13 are 49; then I conſider that 49 Shillings are 2 Pounds and 9 Shillings, wherefore I ſet the 9 Shillings under the Line, and carry the 2 for the 2 Pounds to the next and laſt Denomination of Pounds; and proceed, ſaying, 2 that I carried and 5 makes 7, and 3 are 10, and 9 are 19, and 6 are 25; then I ſet down 5, and carry 2 for the 2 Tens; and proceed, ſaying, 2 that I carry and 1 is 3, and 3 are 6, and 7 are 13, and 3 make 16, and I ſet down 6, and carry 1 for the 10, and go on; ſaying, 1 that I carried and 1 are 2, which I ſet in its Place under the Line, and the Work is finiſhed: And thus I find the Sum of the aforeſaid Numbers to be 265 *l.* 9 *s.* 5 *d.* 2 *qrs.* Here is another Example in the Operation, of which the Learner muſt have an Eye to the Table of *Troy-Weight.* The Numbers given are 38 *l.* 7 *oz.* 13 *pw.* 18 *gr.* and 50 *l.* 10 *oz.* 10 *p. w.* 12 *gr.* and 42 *l.* 08 *oz.* 05 *p. w.* 26 *gr.* And in order to the Addition thereof, I place them as you ſee, and proceed to the Operation ſaying, 16 and 12 are 28, and 18 are 46; now becauſe 24 Grains make 1 Penny-weight, 46 Grains are 1 Penny-weight, and 22 Grains, therefore I ſet down 22, and carry 1 for the Penny-weight, and 5 makes 6, and 10 are 16, and 13 are 29 which is one Ounce and 9 Penny-weight. I ſet down 9 in it Place under the Line, and carry 1 to the Ounces, ſaying, 1 that I carry and 1

l.	*oz.*	*p. w.*	*gr.*
38—	07—	13—	18
50—	10—	10—	12
42—	08—	05—	16
132—	02—	09—	22

are 9; and 10 are 19, and 7 are 26, and becauſe 26 Ounces make 2 Pounds 2 Ounces, I ſet down 2 for the Ounces, and carry 2 to the Pounds; going on, 2 that I carry and 2 are 4, and 8 make 12, that is 2 and g : 1; then 1 I carry and 4 are 5, and 5 are 10, and 3 are 13, which I ſet down as in the Margent, and the Work is finiſhed, and I find the Sum of the ſaid Numbers to amount to 132 *l.* 2 *oz.* 2 *p. w.* 22 *gr.* The Way of proving theſe, or any Sum in this Rule, is ſhewed immediately after the enſuing Example.

Addition of Engliſh Meaſure.

l.	*s.*	*d.*	*qrs.*	*l.*	*s.*	*d.*	*qrs.*
436	03	07	1	48	15	11	1
184	09	10	3	76	10	07	3
768	17	04	2	18	00	05	3
584	11	01	0	24	19	09	2
1954	12	09	2	168	06	10	1

Addition of Troy-Weight.

l.	*oz.*	*p. w.*	*gr.*	*l.*	*oz.*	*p. w.*	*gr.*
15	07	13	12	145	09	12	18
18	06	04	20	726	08	14	10
11	10	16	18	389	07	06	13
09	04	10	22	83	10	16	20
19	11	18	04	130	00	10	12
22	00	00	05	74	07	15	00
97	05	04	09	1550	08	16	01

Addition of Apothecaries Weights.

l.	*oz.*	*dr.*	*ſc.*	*gr.*	*l.*	*oz.*	*dr.*	*ſc.*	*gr.*
41	07	1	0	14	60	03	4	0	10
74	05	5	2	10	48	10	6	0	14
64	10	7	1	6	34	08	2	1	15
17	08	1	0	11	18	11	2	[illegible]	11
34	09	6	1	09	160	07	1	1	5
					35	02	5	[illegible]	07
240	05	6	1	00	358	07	7	0	12

Addition of Averdupois Weight.

Tun.	*C.*	*qrs.*	*l.*
75	13	1	15
48	07	3	21
60	11	1	17
21	07	0	25
12	16	0	11
218	05	0	16

l.	*oun.*	*dr.*
36	10	12
22	01	13
11	07	04
15	04	10
20	00	09
106	03	00

Addition of Liquid Meaſure.

Tun.	*pipes*	*hdd.*	*gal.*
45	1	1	18
15	0	1	17
38	0	0	47
12	1	0	56
21	1	1	18
133	0	1	50

Tun.	*hdd.*	*gal.*	*pts.*
30	3	40	4
12	0	28	6
47	5	50	5
57	3	22	3
17	0	00	0
166	1	26	2

Addition of Dry Meaſure.

Chal.	*qrs.*	*buſh.*	*pec.*
48	3	7	3
13	1	4	0
54	0	6	2
16	3	6	1
4	1	0	1
173	3	0	3

qrs.	*buſh.*	*pec.*	*gal.*
17	3	1	1
50	1	3	0
14	5	3	1
40	2	0	1
30	0	3	0
152	5	3	1

Addition of Long Meaſure.

Yds.	*qrs.*	*Nails*
35	3	3
14	1	2
74	2	3
38	0	1
30	1	0
15	0	0
208	1	1

Els	*qrs.*	*Nails*
56	1	3
13	3	2
48	2	1
50	0	2
74	2	0
17	1	0
260	1	0

Addition of Land Meaſure.

Acre	*Rood*	*Perch*	*Acre*	*Rood*	*Perch*
12	3	18	86	1	36
14	0	24	47	3	24
30	2	19	73	2	28
48	3	30	60	1	07
28	1	38	04	2	08
50	3	26	14	1	14
185	3	35	286	3	37

The Proof of Addition.

6. *Addition* is proved after this Manner: When you have found out the Sum of the Number given, then ſeparate the uppermoſt Line from the reſt, with a Stroke or Daſh of the Pen, and then add them all up again as you did before, leaving out the uppermoſt Line; and having ſo done, add the new invented Sum to the uppermoſt Line you ſeparated, and if the Sum of thoſe two Lines be equal to the Sum firſt found out, then the Work is performed true, otherwiſe not. As for Example: Let us prove the firſt Example of *Addition of Money*, whoſe Sum we find to be 265 *l.* 9 *s.* 5 *d.* 2 *qrs.* and which we prove thus: Having ſeparated the uppermoſt Number from the reſt by a Line, as you ſee in the Margent, then I add the ſame together again, leaving out the ſaid uppermoſt Line, and the Sum thereof I ſet under the firſt Sum or true Sum, which doth amount to 128 *l.* 16 *s.* 1 *d.* 0 *qrs*, then again I add the new Sum to the uppermoſt Line that before was ſeparated from the reſt, and the Sum of thoſe two is 265 *l.* 09 *s.* 05 *d.* 2 *qrs.* the ſame with the firſt Sum, and therefore I conclude that the Operation was rightly performed.

l.	*s.*	*d.*	*qrs.*
136	13	04	2
79	07	10	3
33	18	09	1
15	09	05	0
265	09	05	2
128	16	01	0
265	09	05	2

7. The main End of *Addition* in Queſtion reſolvable thereby, is to know the Sum of ſeveral Debts, Parcels, Integers, &c. ſome Queſtions may be theſe that follow.

Queſt. 1. There was an old Man whoſe Age was re-uired; to which he replied, I have 7 Sons, each having wo Years between the Birth of each other, and in the 4th Year of my Age my eldeſt Son was born, which is ow the Age of the youngeſt. I demand, What was the ld Man's Age.

Now to reſolve this Queſtion, firſt ſet down the Father's Age at the Birth of his firſt Child, which was 44; then the Difference between the Oldeſt and the Youngeſt, which is 12 Years, and then the Age of the Youngeſt, which is 44; and then add them all together, and there Sum is 100, the compleat Age of their Father.

44
12
44
—
100

Queſt. 2. A Man lent his Friend at ſeveral Times, theſe ſeveral Sums, *viz.* at one Time 63 *l.* at another Time 50 *l.* at another Time 48 *l.* at another Time 156 *l.* Now I deſire to know how much was lent him in all?

Set the Sums lent one under another, as you ſee in the Margent, and then add them together, and you will find their Sum to amount to 317 *l.* which is the Total of all the ſeveral Sums lent, and ſo much is due to the Creditor.

63
50
48
156
—
317

Queſt. 3. There are two Numbers, the leaſt whereof is 40, and their Difference 14. I deſire to know what is the greater Number, and alſo what is the Sum of them both? Firſt ſet down the leaſt, *viz.* 40 and 14, the Difference, and add them together, and their Sum is 54 for the greateſt Number; then I ſet 40 (the leaſt) under 54 (the greateſt) and add them together, and their Sum is 94, equal to the greateſt and leaſt Numbers.

40
14
—
greateſt 54
leaſt 40
—
Sum 94

CHAP.

CHAP. V.

Of Subſtraction *of whole Numbers.*

S*Ubtraction*, is taking of a leſſer Number out out of a greater of a like Kind, whereby to find out a Third Number, being or declaring the Inequality, Exceſs, or Difference between the Numbers given; or *Subtraction* is that by which one Number is taken out of another Number given, to the End that the Reſidue or Remainder may be known, which the Remainder is alſo called the Reſt, Remainder, or Difference of the Numbers given.

2. The Number out of which *Subtraction* is to be made muſt be greater, or at leaſt equal with the other Number given; the higher Number is called the *Major*, and the lower, *Minor*; and the Operation of *Subtraction* being finiſhed, the Reſt or Remainder is called the *Difference* of the Numbers given,

3. In *Subtraction*, place the Numbers given reſpectively, the one under the other, in ſuch Sort as like Degrees, Places, or Denominations may ſtand in the ſame Series, *viz.* Units under Units, Tens under Tens, Pounds under Pounds, *&c.* Feet under Feet, and Parts under Parts, *&c.* This being done, draw a Line underneath, as in *Addition.*

4. Having placed the Numbers given as is before directed, and draw a Line under them, ſubtract the lower Number (which in this Caſe muſt always be leſs than the Uppermoſt) out of the higher Number, and ſubſcribe the Difference or Remainder reſpectively below the Line, and when the Work is finiſhed the Number below the Line, will give you the Remainder.

As for Example, Let 364521 be given to be ſubtracted from 795836, I ſet the leſſer under the greater as in the Margent, and draw a Line under them, then beginning at the right Hand, I ſay, one, out of 6 and there remains 5, which I ſet in order under the Line; then I proceed to the next, ſaying, 2 from 3 reſts 1, which I note alſo under the Line; and thus I go on till I have finiſhed the

795846
364521
———
431315

Work; and then I find the Remainder or Difference to be 431315.

5. But if it ſo happen (as commonly it doth) that the lowermoſt Number or Figures is greater than the uppermoſt, than in this Caſe add ten to the uppermoſt Number, and ſubtract the ſaid lowermoſt Number from their Sum, and the Remainder place under the Line, and when you go to the next Figure below, pay an Unit, by adding it thereto for the Ten you borrowed before, and ſubtract that from the higher Number of Figures, and thus go on till your Subtraction be finiſhed. As for Example, Let 437503 be given from whence it is required to ſubtract 153827, I diſpoſe of the Numbers as is before directed, and as you ſee in the Margent; then I begin, ſaying, 7 from 3 I cannot, but (adding 10 thereto) I ſay, 7 from 13 and there remains 6, which I ſet under the Line in order; then I proceed to the next Figure, ſaying, 1 that I borrowed and 2 is 3 from 0 I cannot, but 3 from 10 and there remains 7, which I likewiſe ſet down as before; then 1 that I borrowed and 8 is 9, from 5 I cannot, but 9 from 15 and there remains 6; then 1 I borrowed and 3 is 4 from 7, and there remains 3; then 5 from 3 I cannot, but 5 from 13, and there remain 8; then 1 borrowed and 1 are 2, from 4, and there reſt 2; and thus the Work is finiſhed: After theſe Numbers are ſubtracted one from another, the Inequality, Remainder, Exceſs, or Difference, is found to be 283676. Example for thy farther Experience may be theſe that follow.

```
437503
153827
──────
283676
```

From	3469916	From	361577
Take	738642	Take	5864
Reſt	2831274	Reſt	355713

6. If the Sum or Number to be ſubtracted is of ſeveral Denominations, place the leſſer Sum below the greater, and in the ſame Rank and Order, as is ſhewed in *Addition* of the ſame Numbers; then begin at the right Hand, and take the lower Number out of the uppermoſt, if it be leſſer; but if it be bigger than the uppermoſt, then borrow an Unit from the next greater Denomination, and

turn it into the Parts of the leſs Denomination, and ad thoſe Parts to the Uppermoſt, noting the Remainder belo the Line; then proceed and pay one to the next Denomin tion for that which you borrowed before, and proce in this Order till the Work be finiſhed. An Example this Rule followeth: Let 175 *l.* 13 *s.* 01 *d.* 1 *qr.* be giv from whence let it be required to ſubtract 57 *l.* 16 *s.* 03 2 *qrs.* In order whereunto, I place the Numbers as y ſee in the Margent; and thus I begin at the leaſt Deno nation, ſaying, 2 from 1 I cannot, therefore I borro one Penny from the next Denomination, and turn it into Farthings, which is 4, and adding 4 to 1, which is 5, I ſay, but 2 from 5, and there remain 3, which I put under the Line; then going on, I ſay, 1 that I borrow'd and 3 is 4 from 7, and there reſts 3; then going on, I ſay, 16 from 13 I cannot, but borrowing 1 Poun and turning it into 20 Shillings, I add to it 13, and th is (33) wherefore I ſay, 16 from 33 and there remains 1 which I ſet under the Line, and go on; ſaying, 1 that borrowed and 7 is 8, from 5 I cannot, but 8 from 1 and there remains 7; and the 1 that I borrowed and 5 6, from 7 there reſts 1, and 0 from 3 reſts 3, and the Wo is done. And I find the Remainder or Difference to 317 *l.* 17 *s.* 03 *d.* 3 *qrs.*

l.	*s.*	*d.*
375	13	07
57	16	03
317	17	03

Another Example of *Troy-weight*, may be this, would ſubtract 17 *l.* 10 *oz.* 11 *p.w.* 20 *gr.* from 24 5 *oz.* 00 *p.w.* 08 *gr.* I place the Numbers according to the Rule, and begin, ſaying 20 from 8 I cannot, but I borrow 1 penny-weight, which is 24 Grains, and add them to 8, and there are 32, wherefore I ſay 20 from 32 reſt 12; then 1 that I borrowed and 11 is 12, from 00 I cannot but 12 from 20 (borro ing an Ounce, which is 20 Penny-weight) and there main 8, then 1 that I borrowed and 10 is 11, from 5 cannot, but 11 from 17, and there reſts 6; then 1 that borrowed, and 7 is 8, from 4 I cannot, but 8 from

l.	*oz.*	*p w.*
24	05	00
17	10	11
06	06	08

a

d there reſts 6; then 1 that I borrowed and 1 is 2, from and there reſts nothing; ſo that I find the Remainder Difference to be 6 *l.* 6 *oz.* 8 *p.w.* 12 *gr.*

7. It many times happeneth that you have many Sums Numbers to be ſubtracted from one Number; as, ſuppoſe Man ſhould lend his Friend a certain Sum of Money, d his Friend hath paid him part of his Debt at ſeveral imes, then before you can conveniently know what is ſtill wing, you are to add the ſeveral Numbers or Sums of Payment together, and ſubtract their Sum from the whole Debt, and the Remainder is the Sum due to the Credi- or; as ſuppoſe A lendeth to B 564 *l.* 16 *s.* 10 *d.* and hath repaid him 79 *l.* 16 *s.* *d.* at one time, and 163 *l.* 8 *s.* 11 *d.* at another time, nd 241 *l.* 15 *s.* 8 *d.* at another time; and you would now how the Accompt tandeth between'em, or what s more due to A. In order hereunto I firſt ſet down he Sum which A lent, and raw a Line underneath it, hen under that Line I ſet he ſeveral Sums of Payment, as you ſee in the Margent; nd having brought the ſeveral Sums of Payment into one Total by the 5th Rule of the fourth Chapter foregoing, I find their Sum amounteth to 485 *l.* 11 *s.* 3 *d.* which I ubtract from the Sum firſt lent by A, by the 6th Rule of this Chapter, and I find the Remainder to be 79 *l.* 5 *s.* 7 *d.* nd ſo much is ſtill due to A.

	l.	*s.*	*d.*
Lent	564	16	10
Paid at ſeveral Payments.	79 163 241	16 18 15	08 11 08
Paid in all	485	11	03
Remain	79	05	07

When the Learner hath good Knowledge of what hath een already delivered in this and the foregoing Chapters, e will with Eaſe underſtand the Manner of working the ollowing Examples.

Subtraction of whole Numbers.

	l.	*s.*	*d.*
Borrowed	374	10	03
Paid	79	15	11
Remain	294	14	04

l.	*s.*	*d.*	*qrs.*
700	10	11	2
9	03	11	3
691	06	11	3

	l.	s.	d.	l.	s,	d.	qrs.
Borrowed	1000	00	00	711	03	00	0
Paid	19	00	06	11	13	00	1
Remain	680	19	06	699	09	11	3

	l.	s.	d.	qrs.
Borrowed	3300	00	00	0
Paid at ſeveral Payments	170	10	00	0
	361	13	10	1
	590	03	04	3
	73	04	11	3
Paid in all	1195	12	02	3
Remain due	2104	07	09	1

Subtraction of Troy-weight.

	l.	oz.	p. w.	gr.
Bought	174	00	13	00
Sold	78	04	16	15
Remain	95	07	16	09

	l.	oz.	p. w.	gr.
Bought	470	10	13	00
Sold at ſeveral Times	60	00	00	00
	35	10	18	00
	16	07	09	08
	48	04	00	00
	61	11	19	23
	23	00	00	00
Sold in all	245	10	07	07
Remain unſold	225	00	05	17

Subtraction of Apothecaries Weight.

	l.	oz.	dr.	ſc.	gr.	l.	oz.	dr.	ſc.	gr.
Bought	12	04	3	0	00	20	00	1	0	07
Sold	8	05	1	1	15	10	00	1	2	12
Remain	03	11	1	1	05	09	11	7	0	15

Subtraction of Averdupois-weight.

	C.	*qrs.*	*l.*	*tu.*	*C.*	*qrs.*	*l.*	*oz.*	*dr.*
Bought	35	0	15	5	07	1	10	10	15
Sold	16	2	20	3	17	1	16	09	13
Remain	18	1	23	1	09	3	22	00	08

Subtraction of Liquid Meaſure.

	tu.	*hhd.*	*gal.*	*tu.*	*hhds.*	*gal.*	*pints.*
Bought	40	1	30	60	3	42	4
Sold	16	1	40	15	3	46	6
Remain	23	3	53	44	3	58	6

Subtraction of Dry Meaſure.

	chal.	*qrs.*	*buſh.*	*pec.*	*cha.*	*qrs.*	*buſh.*	*pec.*
Bought	100	0	0	0	73	2	3	2
Sold	54	1	4	3	46	2	3	3
Remain	45	2	3	1	26	3	7	1

Subtraction of Long Meaſure.

	yds.	*qrs.*	*nails.*	*yds.*	*qrs.*	*nails.*
Bought	160	0	0	344	0	1
Sold	64	1	2	177	1	4
Remain	95	2	2	106	2	2

Subtraction of Land Meaſure.

	acres	*rood*	*perch*	*acres*	*rood*	*perch*
Bought	140	2	13	600	0	00
Sold	70	3	12	54	0	16
Remain	69	3	01	545	5	24

The Proof of Subtraction.

8. When your Subtraction is ended, if you deſire to prove the Work, whether it be true or no; then add the Remainder to the minor Number, and if the Aggregate or theſe two be equal to the major Number, then is your Operation true, otherwiſe falſe: Thus let us prove the firſt Example of the fifth Rule of this Chapter, where after Subtraction is ended, the Numbers ſtand as in the Margent,

the Remainder or Difference being 283676. Now to prove the Work, I add the ſaid Remainder 283976 to the Minor Number 153827, by the fourth Rule of the foregoing Chapter, and I find the Sum or Aggregate to be 437503, equal to the major Number, or Number from whence the leſſer is ſubtracted. Behold the Work in the Margent.

43750
15382
———
21367
———
43750

The Proof of another Example, may be of the firſt Example of the 6th Rule of this Chapter, where it is required to ſubtract 57 *l.* 16 *s.* 3 *d.* 2 *qrs.* from 375 *l.* 13 *s.* 7 *d.* 1 *qr.* and by the Rule I find the Remainder to be 317 *l.* 17 *s.* 03 *d.* 3 *qrs.* Now to prove it I add the ſaid Remainder 317 *l.* 17 *s.* 03 *d.* 3 *qrs.* to the minor Number 57 *l.* 16 *s.* 03 *d.* 2 *qrs.* and their Sum is 375 *l.* 13 *s.* 7 *d.* 1 *qr.* equal to the major Number, which proves the Work to be true; but if it had happened to have been either more or leſs than the ſaid major Number, then the Operation had been falſe.

l.	*s.*	*d.*	*qrs.*
375	13	07	
51	16	03	
317	17	03	
375	13	07	

9. The general Effect of Subtraction, is, to find the Difference or Exceſs between two Numbers, and the Reſt when a Payment is made in Part of a greater Sum, the Date of Books printed, the Age of any Thing, by knowing the preſent Year, and the Year wherein they are made, created, or built, and ſuch like.

The Queſtions appropriated to the Rule, are ſuch as follow.

Queſt. What Difference is there between one Thing of 125 Foot long, and another of 66 Foot long?

To reſolve this Queſtion, I firſt ſet down the major or greater Number 125, and under it the minor or leſſer Number 66, as is directed in the third Rule of this Chapter, and according to the fourth Rule of the ſame, I ſubtract the Minor from the Major, and the Remainder, Exceſs, or Difference I find to be 59. See the Work in the Margent.

125
66
—
59
—

Queſt. 2. A Gentleman hath owed a Merchant 365 *l.* whereof he hath paid 278 *l.* What more doth he owe;

To give an Anſwer to this Queſtion, I firſt ſet
down the major Number 365 *l.* and under it I place 365
278 the minor, and ſubtract the one from the other, 278
whereby I diſcover the Exceſs, Difference, or Remainder; —
to be 87; and ſo much is ſtill due to the 87
Creditor, as *per* Margent.

Queſt. 2. An Obligation was written, a Book printed, a Child born, a Church built or any other Thing made in the Year of our Lord 1572, and now we account
the Year of our Lord 1687, the Queſtion 1687
is to know the Age of the ſaid Things; that is, 1572
How many Years are paſſed ſince the ſaid Things —
were made? I ſay, if you ſubtract the leſſer Number 115
1572 from the greater 1687, the Remainder will be 115, and ſo many Years are paſſed ſince the Making of the ſaid Things; as by this Work in the Margent.

Queſt. 4. There are three Towns lie in a ſtraight Line, *viz.* *London*, *Huntingdon*, and *York*, now the Diſtance between the fartheſt of theſe Towns, *viz.* *London* and *York*, is 151 Miles, and from *London* to *Huntingdon* is 49 Miles. I demand how far it is from *Huntingdon* to *York*?

To reſolve this Queſtion, ſubtract 49 the Diſtance 151
between *London* and *Huntingdon*, from 151, the Di- 49
ſtance between *London* and *York*, and the Remainder —
is 102, for the true Diſtance between *Huntingdon* and 102
York. See the Work in the Margent.

CHAP. VI.

Of Multiplication of Whole Numbers.

1. Multiplication is performed by two Numbers of like Kind, for the Production of a Third, which ſhall have ſuch Reaſon to the one, as the other hath to the Unit, and in Effect is a moſt brief and artificial *Compound Addition*, of many equal Numbers of like kind into one Sum. Or, *Multiplication* is that by which we multiply two or more Numbers, the one into the other, to the End that their Product may come forth, or be diſcovered.

Or, *Multiplication* is the Increaſing of any one Number by any other, ſo often as there are Units in that Number, by which the other is increaſed ; or by having two Numbers given to find a Third, which ſhall contain one of the Numbers as many times as there are Units in the other.

2. *Multiplication* hath three Parts. Firſt, the Multiplicand or Number to be multiplied. Secondly, The Multiplier or Number given by which the Multiplicand is to be multiplied. And thirdly, The Product or Number produced by the other two, the one being multiplied by the other ; as if 8 were given to be multiplied by 4, I ſay 4 times 8 is 32 ; here 8 is the Multiplicand, and 4 is the Multiplier, and 32 is the Product.

$$\begin{array}{r} 8 \\ 4 \\ \hline 32 \end{array}$$

3. *Multiplication* is either *Single*, by one Figure ; or *Compound*, that conſiſts of many.

Single Multiplication is ſaid to conſiſt of one Figure, becauſe the Multiplicand and Multiplier conſiſts each of them of a Digit, and no more ; ſo that the greateſt *Product* that can ariſe by *Single Multiplication* is 81, being the Square of 9, and *Compound Multiplication* is ſaid to conſiſt of many Figures, becauſe the Multiplicand or Multiplier conſiſts of more Places than one ; as if I were to multiply 436 by 6 : It is called Compound, becauſe the Multiplicand 436 is of more Places than one, *viz.* 3 Places.

4. The Learner ought to have all the Varieties of *Single Multiplitation* by Heart, before he can well proceed any farther into this Art, it being of moſt excellent Uſe, and none of the following Rules in *Arithmetick*, but what have a principal Dependance thereupon, which may be learnt by the following Table.

Mul-

Multiplication TABLE.

1	2	3	4	5	6	7	8	9
2	4	6	8	10	12	14	16	18
3	6	9	12	15	18	21	24	27
4	8	12	16	20	24	28	32	36
5	10	15	20	25	30	35	40	45
6	12	18	24	30	36	42	48	54
7	14	21	28	35	42	49	56	63
8	16	24	32	40	48	56	64	72
9	18	27	36	45	54	63	72	81

The Uſe of the precedent Table is this : In the uppermoſt Line or Column you have expreſſed all the Digits from 1 to 9 ; and likewiſe beginning at 1, and going downwards in the ſide Column, you have the ſame ; ſo that if you would know the Product of any two ſingle Numbers multiplied by one another, look for one of them (which you pleaſe) in the uppermoſt Column, and for the other in the ſide Column, and running your Eye from each Figure along the reſpective Columns to the common Angle (or Place) where theſe two Columns meet, there is the Product required. As for Example, I would know how much is 8 times 7 ; Firſt I look for 8 in the uppermoſt Column, and 7 in the ſide Column ; then do I caſt my Eye from 8 along the Column downwards from the ſame, and likewiſe from 7 in the ſide Column, I caſt my Eye from thence toward the right Hand, and find it to meet with the firſt Column at 56, ſo that I conclude 56 to be the Product required, *&c.*

5. In *Compound Multiplication*, if the Multiplicand conſiſts of many Places, and the Multiplier of but one Figure ; firſt ſet down the Multiplicand, and under it place the Multiplier in the Place of Units, and draw a Line underneath them, begin then, and multiply the Multiplier into every particular Figure of the Multiplicand, beginning at the Place of Units, and ſo proceed towards the Left Hand, ſetting each particular Product under the Line, in order as you proceed : But if any of the Products exceed

ceeds 10, or any Number of Tens, ſet down the Exceſs, and for every 10 carry an Unit to be added to the next Product, always remembring to ſet down the total Product of the laſt Figure; which Work being finiſhed, the Sum or Number placed under the Line ſhall be true and total Product required. As for Example, I would multiply 478 by 6: Firſt ſet down 478 and underneath it 6, in the Place of Units, and draw a Line underneath them, as in the Margent; then I begin, ſaying, 6 times 8 is 48, which is 8 above four Tens, therefore I ſet down 8 (the Exceſs and bear 4 in Mind for the 4 Tens; then I proceed, ſaying, 6 times 7 is 42, and that I carrried is 46, I then ſet down 6 and carry 4, and go on, ſaying, 6 times 4 is 24, and 4 that I carried is 28, and becauſe it is the laſt Figure I ſet it all down, and ſo the Work is finiſhed, and the Product is found to be 2868, as was required.

$$\begin{array}{r} 418 \\ 6 \\ \hline 2868 \end{array}$$

6. When in *Compound Multiplication*, the Multiplier conſiſteth of diverſe Places, then begin with the Figure in the Place of Units in the Multiplier, and multiply it into all the Figures in the Multiplicand, placing the Product below the Line, as was directed in the laſt Example; then begin with the Figure of the ſecond Place of the Multiplier *viz.* the Place of Tens, and multiply it likewiſe into the whole Multiplicand, (as you did the firſt Figure) placing its Product under the Product of the firſt Figure; do in the ſame Manner by the Third, Fourth, and Fifth, *&c.* until you have multiplied all the Figures of the Multiplier particularly into the whole Multiplicand, ſtill placing the Product of each particular Figure under the Product of its precedent Figure; herein obſerving the following Caution.

A Caution.

In the placing of the Product of each particular Figure of the Multiplier, you are not to follow the 2d Rule of the 4th Chapter, *viz.* to place Units under Units, and Tens under Tens, &c. but to place the Figure or Cypher in the Place of Units of the ſecond Line under the ſecond Figure or Place of Tens in the Line above it, and the Figure or Cypher in the Place of Units in the third Line under the Place of Tens in the ſecond Line, &c. obſerving this Order, till you have finiſhed the Work, ſtill placing the firſt Figure of every Line or Product under the ſecond Figure or Place of Tens in that which was above it, and having ſo done, draw a Line under all theſe particular Products, and add them together; ſo ſhall the Sum of all theſe Products be the total Product required.

As it were required to multiply 764 by 27, I ſet them down the one under the other with a Line drawn underneath them; then I begin, ſaying, 7 times 4 is 28, then I ſet down 8 and carry 2; then I ſay, 7 times 6 is 42, and 2 that I carried is 44, that is 4 and go 4; then 7 times 7 is 49, and 4 that I carry is 53, which I ſet down, becauſe I have not another Figure to multiply; thus I have done with the 7, then I begin with the 2, ſaying 2 times 4 is 8, which I ſet down under (4) the ſecond Figure or Place of Tens in the Line above it, as you may ſee in the Margent; then I proceed, ſaying, 2 times 6 is 12, that is 2 and carry 1; then 2 times 7 is 14, and 1 that I carry is 15, which I ſet down, becauſe it is the Product of the laſt Figure; ſo that the Product of 764 by 7 is 5348, and by 2 is 1528, which being placed the one under the other, as before directed, as you ſee in the Margent, and a Line drawn under them, and they added together reſpectively, make 20628, the true Product required, being equal to 27 times 764.

$$\begin{array}{r}764\\27\\\hline 5348\\1528\\\hline 20628\end{array}$$

Another Example may be this; Let it be required to multiply 5486 by 465, I diſpoſe of the Multiplicand and Multiplier according to the Rule, and begin multiplying the firſt Figure of the Multiplier, which is (5) into the whole Multiplicand, and find the Product is 27430; then I proceed, and multiply the ſecond Figure (6) of the Multiplier into the Multiplicand, and find the Product to amount to 32916, which is ſubſcribed under the other Product reſpectively; then do I multiply the third and laſt Figure (4) of the Multiplier into the Multiplicand, and the Product is 21944 which is likewiſe placed under the ſecond Line reſpectively; then I draw a Line under the ſaid Product being placed the one under the

$$\begin{array}{r}5486\\465\\\hline 27430\\32916\\21944\\\hline 2550990\\\hline\end{array}$$

the other according to Rule) and add them together, and the Sum is 2450990, the true Product ſought, being equal to 5486 times 465, or 465 times 5486.

More Examples in this Rule are theſe following.

430865
4739
3877785
1292595
3016055
1723460
2041869235

6400758
37496
38404548
57606822
25603032
44805306
19202274
240002821968

Compendium in Multiplication.

7. Although the former Rules are ſufficient for all Caſes in *Multiplication*, yet becauſe in the Work of *Multiplication* many times great Labour may be ſaved, I ſhall acquaint the Learner with ſome Compendiumns in order thereunto, *viz.* If the Multiplicand or Multiplier, or both of them end with Cyphers then in your multiplying you may neglect the Cyphers, and multiply only the ſignificant Figures, and to the Product of thoſe ſignificant Figures, add ſo many Cyphers as the Numbers given to be multiplied did end with; that is, annex them on the right Hand of the ſaid Product, ſo ſhall that give you the true Product required. As if I were to multiply 32000 by 4300, I ſet them down in order to be multiplied, as you ſee in the Margent; but neglecting the Cyphers in both Numbers, I only multiply 32 by 43, and the Product I find to be 1376, to which I annex the 5 Cyphers in the Multiplicand and Multiplier, and

Si numeris prepoſitis unus vel uterque adjunctos habeat ad dextram circulos, omiſſis circulis fiat ipſorum numerorum multiplicatio, & facto demum tot inſuper integrorum loci accenſeantur quot ſunt omiſſi circuli in utroque factore. Clavis Mat. c. 4. 3.

32000
4300
96
128
137600000

and then it makes 137600000 for the true Product of 32000 by 4300.

8. If in the Multiplier, Cyphers are placed between ſignificant Figures, then multiply only by the ſignificant Figures neglecting the Cyphers; but here ſpecial Notice is to be taken of the true placing of the firſt Figure after the Neglect of ſuch Cypher or Cyphers; and therefore you muſt obſerve in what Place of the Multiplier the Figure you multiply by ſtandeth, and ſet the firſt Figure of that Product under the ſame Place of the Product of the ſame Figure of your Multiplier: As for Example, Let it be required to multiply 371568 by 40007. Firſt I multiply the Multiplicand by 7, and the Product it 2600976; then neglecting the Cyphers, I multiply by 4, and that Product is 1486272; now I conſider, that 4 is the 5th Figure in the Multiplier, therefore I place 2 (the firſt Figure of the Product by 4) under the fifth Place of the firſt Product by 7, and the reſt in order, and having added them together, the total Product is found to be 14865324976. Other Examples in this Rule, are theſe following.

Si intermedio multiplicantis loco circulus fuerit, ille negligitur. Alſted. c. 6. *De Arithm.*

371568
40007
2600976
1486272···
14865320969

327586
6030
9827580
1965516
1975343516

7864371
20604
31457484
47186226
15728742
162037500084

9. If you are to multiply any Number by an Unit with Cyphers, as by 10 100. 1000, &c. then annex ſo many Cyphers before the Multiplicand, and that Number when the Cyphers are annex'd, is the Product required. As if you would multiply 428 by 100, annex 2 Cyphers to 428, and it is 42800. If it were required to multiply 102. by 10000,

10000, annex 4 Cyphers, and it gives 1020000 for the Product required.

The Proof of Multiplication.

10. *Multiplication* is proved by *Diviſion*, and to ſpeak Truth, all other Ways are falſe, (according to *Friſius*) and therefore it will be neceſſary in the firſt Place to learn *Diviſion*, and by that to prove *Multiplication*. There are ſome other Way uſed indeed, but on a ſtrict *Examen*, there is not one in a Thouſand of their Products right: therefore we omit them.

11. The general Effect of *Multiplication* is contained in the Definition of the ſame, which is to find out a third Number, ſo often containing one of the two given Numbers, as the other containeth Units.

The ſecond Effect is, by having the Length and Bredth of any Thing (as a Parallelogram or long Plain) to find the ſuperficial Content of the ſame, and by having the ſuperficial Content of the Baſe, and the Length, to find out the Solidity of any Parallelopipedon, Cylinder, or other ſolid Figures.

The third Effect is, by the Contents, Price, Value, Buying, Selling, Expence, Wages, Exchange, Simple Intereſt, Gain or loſs of any one Thing, be it Money, Merchandize, &c. to find out the Value, Price, Expence, Buying, Selling, Exchange, or Intereſt, of any Number of Things of the like Name, Nature, and Kind.

The fourth Effect (is not much unlike the other) by the Contents, Value, or Price of any one Part of any Thing denominated, to find the Contents, Value, or Price of the whole Thing, all the Parts into which the whole is divided, multiplying the Price of one of thoſe Parts.

The fifth Effect is, to aid, to compound, and to make other Rules, as chiefly, the *Rule of Proportion*, called the *Golden Rule*, or *Rule of Three*; alſo by it, Things of one Denomination are reduced to another.

If you multiply any Number of Integars, to the Price of the Integar, the Product will diſcover the Price of the Quantity, or Number of Integers given.

In a Recangular Solid, if you multiply the Bredth of the Baſe by the Depth, and that Product by the Length the laſt Product will diſcover the Solidity or Content of the ſame Solid.

Some Queſtions proper to this Rule, may be theſe following:

Queſt. 1. What is the Content of a ſquare Piece of Ground, whoſe Length is 28 Perches, and Breadth 13?

Anſwer, 364 ſquare Perches; for multiplying 28 the Length by 13 the Breadth, the Product is ſo much.

Queſt. 2. There is a ſquare Battle, whoſe Flank is 47 Men, and the Files 19 deep, what Number of Men doth that Battle contain? *Facit.* 893; for multiplying 46 by 19, the Product is 893.

Queſt. 3. If any one Thing coſt 4 Shillings, what ſhall 9 Things coſt? *Anſw.* 36 Shillings; for multiplying 4 by 9, the Product is 36.

Queſt. 4. If a Piece of Money or Merchandize be worth or coſt 17 Shillings, what ſhall 19 ſuch Pieces of Money or Merchandize coſt? *Facit.* 323 Shillings, which is equal to 16 *l.* 3 *s.*

Queſt. 5. If a Soldier or Servant get or ſpend 14 *s. per* Month, what is the Wages or Charges of 49 Soldiers or Servants for the ſame Time? Multiply 49 by 14, the Product is 686 *s.* or 14 *l.* 6 *s.* for the Anſwer.

Queſt. 6. If in a Day there are 24 Hours, how many Hours are there in a Year, accounting 365 Days to conſtitute the Year? *Facit.* 8760 Hours; to which if you add the 6 Hours over and above 365 Days, as there is in a Year, then it will be 8766 Hours; now if you multiply this 8766 by 60, the Number of Minutes in an Hour, it will produce 525960, the Number of Minutes in a Year.

CAAP. VII

Diviſion of whole Numbers.

1. D*Iviſion*, is the ſeperating or parting of any Number or Quantity given, into any Part aſſigned, or to find how often one Number is contained in another; or from any two Numbers given, to find a third that ſhall conſiſt of ſo many Units, as the one of thoſe two Numbers given is comprehended or contained in the other.

2. *Diviſion* hath three Parts of Numbers remarkable, *viz.* Firſt, the Dividend; 2dly, The Diviſor; 3dly,

The Quotient. The Dividend is the Number given to be parted or divided. The Diviſor is the Number given by which the Dividend is divided, or it is the Number which ſheweth how many Parts the Dividend is to be divided into. And the Quotient is the Number produced by the Diviſion of the two given Numbers the one by the other.

So 12 being given to be divided by 3 or into three equal Parts, the Quotient will be 4; for 3 is containing in 12 four times, where 12 is the Dividend, and 3 is the Diviſor and 4 is the Quotient.

3. In *Diviſion* ſet down your Dividend, and draw a crooked Line at each End of it, and before the Line at the left Hand place the Diviſor, and behind that on the right Hand place the Figures of the Quotient, as in the Margent, where it is required to divide 12 by 3; Firſt, I ſet down 12 the Dividend, and on each Side of it, do I draw a crooked Line, and before that on the left Hand do I place 3 the Diviſor; then do I ſeek how often 3 is contained in 12; and becauſe I find it four times, I put 4 behind the crooked Line, on the right Hand of the Dividend, denoting the Quotient.

3) 12 (4

4. But if, when the Diviſor is a ſingle Figure, the Dividend conſiſteth of two or more Places, then having placed them for the Work (as before directed) put a Point under the firſt Figure of the left Hand of the Dividend, provided it be bigger than (or equal to) the Diviſor but if it be leſſer than the Diviſor, then put a Point under the ſecond Figure from the left Hand of the Dividend; which Figures, as far as the Point goeth from the left Hand, are to be reckoned by themſelves, as if they had no Dependance upon the other Part of the Dividend: And for Diſtinction ſake may be called the Dividual; then ask how often the Diviſor is contained in the Dividual; placing the Anſwer in the Quotient; then multiply the Diviſor by the Figure that you placed in the Quotient, and ſet the Product thereof under your Dividual; then draw a Line under the Product, and ſubtract the ſaid Product from the Dividual placing the Remainder under the ſaid Line; then put a Point under the next Figure in the Dividend on the right Hand of that to which you put the Point before, and

draw it down, placing it on the right Hand of the Remainder which you found by *Subtraction*; which Remainder with the ſaid Figure annex before it, ſhall be a new Dividual; then ſee again how often the Diviſor is contained in this new Dividual, and put the Anſwer in the Quotient on the right Hand of the Figure which you put there before; then multiply the Diviſor by the laſt Figure that you put in the Quotient, and ſubſcribe the Product under the Dividual, and make Subtraction, and to the Remainder draw down the next Figure from the grand Dividend, (having firſt put a Point under it) and put it on the Right Hand of the Remainder for a new Dividual as before and proceed thus till the Work is finiſhed.

Obſerving this general Rule in all Kinds of *Diviſion*. Firſt, to ſeek how often the Diviſor is contained in the Dividual; then (having put the anſwer in the Quotient) multiply the Diviſor thereby, and ſubtract the Product from the Dividual. An Example or two will make the Rule plain. Let it be required to divide 2184 by 6. I diſpoſe of the Numbers given as is before directed, and as you ſee in the Margent; in order to the Work, then becauſe 6 the Diviſor is more than 2 the firſt Figure of the Dividend, I put a Point under 1 the ſecond Figure, which makes the 21 for the Dividual, then do I ask how often 6 the Diviſor is contained in 21, and becauſe I cannot have it more than 3 times, I put 3 in the Quotient, and thereby do I multiply the Diviſor (6) and the Product is 18, which I ſet in order under the Dividual, and ſubtract it therefrom, and the Remainder (3) I place in order under the Line as you ſee in the Margent. Then do I make a Point under the next Figure of the Dividend, being 8, and draw it down, placing it before the Remainder 3, ſo have I 38 for a new Dividual, then do I ſeek how often 6 is contained in 38 and becauſe I can't have it more than 6 Times, I put 6 in the Quotient, and thereby do I multiply the Diviſor 6, and the Pro-

```
6)  2184 (3
     .
```

```
6) 2184 (3
    .
   18
   ----------
    3
```

```
6) 2184 (36
    ..
   18
   ----------
   31
   36
   ----------
```

Product (36) I put under the Dividual (38) and ſubtract it therefrom, and the Remainder 2 I put under the Line, as you ſee in the Margent.

Then I do put a Point under the next (and laſt) Figure of the Dividend (being 4) and draw it down to the Remainder 2, and putting it on the right Hand thereof, it maketh 24 for a new Dividual; then I ask how often 6 is contained in 24, and the Anſwer is 4, which I put in the Quotient, and multiply the Diviſor (6) thereby, and the Product (24) I put under the Dividual (24) and ſubtract it therefrom, and the Remainder is (0); and thus the Work is finiſhed, and I find the Quotient to be 364, that is 6 is contained in 2184, juſt 364 times, or 2184 being divided into 6 equal Parts, 364 is one of thoſe Parts.

```
6) 2184 (364
    •••
   18
   ——
   38
   36
   ——
    24
    24
    ——
    (0)
```

Again, If it were required to divide 2646 by 7, or into 7 equal Parts, the Quotient will be found to be 378, as by the following Operation appeareth.

```
7) 2646 (378
   •••
   21
   ——
   54
   49
   ——
    56
    56
    ——
    00
```

So if it be required to divide 949 by 8, the Quotient will be found to be 118, and 2 remaining after Diviſion is ended. The Work followeth:

8) 945

8) 946 (118
• • •
8
—
14
8
—
66
64
—
(2)

Many times the Dividend cannot exactly be divided by the Diviſor, but ſomething will remain, as in the laſt Example, where 946 was given to be divided by 6, the Quotient was 118, and there remained 2 after the Diviſion was ended: Now what is to be done in this Caſe with the Remainder, the Learner ſhall be taught when we come to treat of the Reducing (or Reduction) of Fractions.

And here note, That if after your Diviſion is ended, any Thing do remain, it muſt be leſſer than your Diviſor; for otherwiſe your Work is not rightly performed.

Other Examples are ſuch as follows.

8) 73464 (9183	9) 13758 (1528
• • • •	• • •
72	9
—	—
14	47
8	45
—	—
66	25
64	18
—	—
24	78
24	72
—	—
(0)	(6)

5. But if the Diviſor conſiſteth of more Places than one, then chuſe ſo many Figures from the left Side of the Dividend for a Dividual as there are Figures in the Diviſor, and put a Point under the fartheſt Figure of that Dividual

to the right Hand and ſeek how often the firſt Figure on the left Side of the Diviſor is contained in the firſt Figure on the left Side of the Dividual, and place the Anſwer in the Quotient, and thereby multiply your Diviſor, placing your Product under your Dividual, and ſubtract it therefrom placing the Remainder below the Line; then put a Point under the next Figure in the Dividend, and draw it down to the ſaid Remainder, and annex it on the right ſide thereof, which makes a new Dividual, and proceed as before, till the Work is finiſhed.

And if it ſo happen, that after you have choſen your firſt Dividual, (as it is before directed) you find it to be leſſer than the Diviſor, then put a Point under the Figure more near to the right Hand, and ſeek how often the firſt Figure on the left Side of the Diviſor is contained in the two firſt Figures on the left of the Dividual, and place the Anſwer in the Quotient, by which multiply the Diviſor, and place the Product thereof in order under the Dividual, and ſubtract it therefrom, and proceed as before.

Always remembering that in all Caſes of *Diviſion*, if after you have multiplied your Diviſor by the Figure firſt placed in the Quotient, the Product be greater than the Dividual, then you muſt cancel that Figure in the Quotient and inſtead thereof put a Figure leſſer by an Unit (or One) and multiply the Diviſor thereby, and if ſtill the Product be greater than the Dividual, make the Figure in the Quotient yet leſſer by an Unit, and thus do until your Product be leſſer than the Dividual, or at the moſt equal thereto, and then make Subtraction, *&c.*

So if you would divide 9464 by 24, the Quotient will be found to be 394; I firſt put down the given Number as is before directed in the 3d Rule. Now becauſe my Diviſor conſiſteth of two Figures, I therefore put a Point under the ſecond Figure from the left Hand of my Dividend, which there is 4, wherefore I ſeek how often 2 the firſt Figure (on the left Side of the Diviſior) is contained in 9 (the like firſt in the Dividual) the Anſwer is 4, which I put in the Quotient, and thereby multiply all the Diviſor, and find the Product to be 26, which is greater

```
24)9464(36
    •••
    72
  ————————
    226
    216
  ————————
     10
```

than the Dividual 94, wherefore I cancel the 4 in the Quotient, and inſtead therefore I put 3, (an Unit leſſer) and by it multiply the Diviſor 24, and the Product is 72, which I ſubtract from 94 the Dividual, and the Remainder is 22; then do I make a Point under the next Figure 6 in the Dividend, and draw it down, and place it on the right Side of the Remainder 22, and it makes 226 for a new Dividual; now becauſe the Dividual 226 conſiſteth of a Figure more than the Diviſor, therefore I ſeek how often 2 (the 1ſt Figure of the Diviſor) is contained in 22, the two firſt of the Dividual, and I ſay 9 times, wherefore I put 2 in the Quotient, and thereby multiply the Diviſor 24, the Pruduct (216) I place under the Dividual 226 and ſubtract it from it, and there remaineth 10.

```
24) 9464 (36
     ...
     72
    ----
     226
     216
      10
```

Then I go on and make a Point under the next and laſt, Figure (4) in the Dividend, and draw it down to the Remainder 10, and it makes 104 for a new Dividual, which is alſo a Figure more than the Diviſor; and therefore I ſeek how often 2 is contained in 10, I anſwer 5 times; but multiplying my Diviſor by 5, the Product is 120, which is greater than the Dividual, and therefore I make it but 4, and by it multiply the Diviſor, and the Product is 96, which being placed under, and ſubtracted from the Dividual, there remaineth 8; and thus the whole Work of this Diviſion is ended, and I find that 9464, being divided by 24, or into 24 equal Parts, is found to be 394, as was ſaid before; and the Remainder is 8, as you ſee in the Work following.

```
24) 9464 (394
    ....
    72
    ---
    226
    216
    ---
     104
      96
     ---
     (8)
```

Another Example may be this: Let there be required the Quotient of 183654 divided by 385: Firſt, I diſpoſe of the Numbers in order to their dividing, and becauſe 118, the three firſt Figures of the Dividend, is leſſer than the Diviſor 385, and therefore make a Point under the fourth Figure, which is 3, and ſee how often 3 (the firſt Figure of the Diviſor) is contained in 11: The Anſwer is 3, which I put in the Quotient, and thereby multiply the Diviſor 385, and the Product is 1155, which I ſubtract from the Dividual 183, and there remains 28. Then (as before) I draw down the next Figure which is 6, and place it before the Remainder 28; ſo have I 268 for a new Dividual, and becauſe it hath no more Figures than the Diviſor, I ſeek how often 3 (the firſt Figure of the Diviſor) is contained in 2 (the firſt Figure of the Dividual) and the Anſwer is 0; for a greater Number cannot be contained in a Leſſer; wherefore I put 0 in the Quotient, and thereby (according to the 5th Rule) I ſhould multiply the Diviſor; but if I do, the Product will be 0 and 0 ſubtracted from the Dividual 286, the Remainder is the ſame; wherefore I draw down the next Figure (5) from the Dividend, and put it before the ſaid Remainder 286, ſo have I 2865 for a new Dividual; and becauſe it conſiſteth of 4 Places, *viz.* a Place more than the Diviſor, I ſeek how often 3, the 1ſt Figure of the Diviſor, is contained in 28 the two firſt of the Dividual, and I ſay, there is 9 times 3 is 28; but multiplying my whole Diviſor (385) thereby, I find the Product to be 3465, which is greater than the Dividual 3465; wherefore I chuſe 8, which is leſſer by an Unit than 9, and thereby I multiply my Diviſor 385, and the Product is 3080, which ſtill is greater than the ſaid Dividual;

```
385) 1183653 (3
        .
     1155
     ————
       28
```

```
385) 1183653 (30
        ..
     1155
     ————
      286
```

```
385) 1183653 (307
        ...
     1155
     —————
      2865
      2695
     —————
       170
```

al; wherefore I chuſe another Number yet an Unit leſſer, *viz.* 7, and have multiplied my Diviſor thereby, the Product is 2695, which is leſſer than the Dividual 2865, wherefore I put 7 in the Quotient and ſubtract 2695 from the Dividual 2865, and there remain 170; then I draw down the laſt Figure (3) in the Dividend, and place it before the ſaid Remainder 170, and it makes 1703 for a new Dividual; then (for the Reaſon aboveſaid) I ſeek how often 3 is contained in 17, the Anſwer is 5, but multiplying the Diviſor thereby, the Product is 1925, greater than the Dividual, wherefore I ſay it will bear 4 (an Unit leſſer) and by it I multiply the Diviſor 385, and the Product is 1540 which is leſſer than the Dividual, and therefore I put 4 in the Quotient, and ſubtract the ſaid Product from the Dividual, and there remain 163; and thus the Work is finiſhed; and I find that 1183653 being divided by 385, or into 385 equal Shares or Parts, the Quotient, (or one of thoſe Parts) is 3074, and beſides there is 163 remaining.

```
385) 1183653 (3074
        ....
     1155
     ----
      2865
      2695
      ----
       1703
       1540
       ----
       (163)
```

And thus the Learner being well verſed in the Method of the foregoing Example, he may be ſufficiently qualified for the dividing of any greater Sum or Number into as many Parts as he pleaſeth; that is, he may underſtand the Method of dividing by a Diviſor, which conſiſteth of 4, or 5, or 6, or any greater Number of Places, the Method being the ſame with the foregoing Example in every Reſpect.

Other Examples in Diviſion.

27986) 835684790 (29860
• • • •

55972

275964
251874

40907
223888

170199
167916

Remain (22830)

196374) 473986018 (2413
• • • •

392748

812380
785496

268841
196374

714678
589122

Remain (15556)

So if you divide 47386473 by 58736, you will find the Quotient to be 806, and 45257 will remain after the Work is ended.

In like manner, If you would divide 3846739204 by 483064, the Quotient will be 7963, and the Remainder after Diviſion will be 100572.

Compendium in Diviſion.

1. IF any given Number be to be divided by another Number that hath Cyphers annexed on the right Side thereof, (omitting the Cyphers) you may cut off ſo many

any Figures from the right Hand of the Dividend, as here are Cyphers before the Diviſor, and let the remain-g Numbers in the Dividend, be divided by the remain-g Number, or Numbers of the Diviſor, obſerving this Caution: That if after your Diviſion is ended, any Thing emain, you are to annex thereto the Number or Numbers hat were cut off from the Dividend; and ſuch now found Number ſhall be the Remainder. (Se Mr. *Oughtred's* *lavis Mathemetica*, cap. 5. 3.) As for Example, Let it required to divide 46658 by co, now becauſe there are two Cyphers before the Diviſior, I cut f as many Figures from before e Dividend, *viz.* 58, ſo that then ere will remain only 466 to be ivided by 4, and the Quotient ill be 116, and there will re-ain 2, to which I annex the o Figures (58) which were cut ft from the Dividend, and it makes 58 from the true Remainder; ſo at I conclude 46658 being di-ided by 400, the Quotient will be 116, and 258 re-ain after the Work is ended; as by the Work in the argent.

```
4|00) 466|58 (116
      ..:
      4
      ——
      6
      ——
      26
      24
      ——
      (258)
```

2. And hence it followeth, that if the Diviſor be 1, or Unit with Cyphers annexed, you may cut off ſo many igures from before the Dividend, as there are Cyphers the Diviſor, and then the Figure or Figures that are on e left Hand will be the Quotient, and thoſe that are on e right Hand will be the Remainder after the Diviſion is ded. (*Vid.. Gem. Priſ. Arith. Par.* 1.) As thus; if 45783 ere to be divided by 10, I cut off the laſt Figure (3) with Daſh thus, 4678|3, and the Work is done, and the Quo-nt is 4578 (the Number on the left Hand of the Daſh) d the Remainder is 3 (on the right Hand.) In like man-r if the ſame Number 45783 were to be divided by 100, cut off two Figures from the End thus, (457|83) and e Quotient is 457, and the Remainder is 83. And if I n to divide the ſame Figures, by 1000, I cut off 3 from e End thus (45|783) and the Quotient is 45, and 783 is e Remainder, &c.

6. The general Effect of *Diviſion*, is contained in th Definition of the ſame, that is by having two unequal Numbers, to find a third Number in ſuch Proportion to the Dividend, as the Diviſor hath to a Unit or 1: It alſo diſcovers what Reaſon or Proportion there is between Numbers; fo if you divide 12 by 4, it quotes 3, which ſhews the Reaſon or Proportion of 4 to 12 is triple.

The ſecond Effect is, by the ſuperficial Meaſure or Content, and the Length of any Oblong, Rectangular, Parallelogram, or ſquare Plane known, to find out the Breadth thereby; or contrariwiſe, by having the Superficies and Breadth of the ſaid Figure, to find out the Length thereof, Alſo by having the Solidity and Length of a Solid, to find the Superficies of the Baſe, *& contra.*

The third Effect is, by the Contents, Reaſon, Price, Value, Buying, Selling, Expences, Wages, Exchange, Intereſt, Profit, or Loſs of any Number of Things, (be it Money, Merchandize, or what elſe) to find out the Contents, Reaſon, Price, Value, Buying, Selling, Expence, Wages, Exchange, Intereſt, Profit, of Loſs, or any one Thing o the like Kind.

The fourth Effect is, to aid, to compaſs, and to mak other Rules, but principally the Rule of *Proportion*, called the *Golden Rule*, or *Rule of Three*, and the Reduction o Monies, Weights, and Meaſures of one Denominatio into another, by it alſo Fractions are abbreviated, by finding common Meaſurer unto the Numerator and Denominator, thereby diſcovering commenſurable Numbers.

If you divide the Value of any certain Quantity by th ſame Quantity, the Quotient diſcovers the Rate or Valu of the Integer: as if 8 Yards of Cloth coſt 29 Shillings, i by (8) the ſame Quantity, the Quotient will be 128 you divide (96) the Value of 1 of thoſe Yards, &c.

If you divide the Value or Price of any unknown Quantity, by the Value of the Integer, it gives you in the Quotient that unknown Quantity, whoſe Price is thus divided as if 12 Shillings were the Value of a Yard, I would know how many Yards, are worth 96 Shillings: Here if you divide (69), the Price or Value of the unknown Quantity, b 12, the Rate of the Integer, or 1 Yard, the Quotient will b 8, which is the Number of Yards worth 96 *s.*

Some Queſtions anſwered by Diviſion may be theſe following.

Queſt. 1. If 22 Things coſt 66 Shillings, what will 1 ſuch Thing coſt? *Facit* 3 Shillings, for you divide 66 by 22, the Quotient is 3 for the Anſwer; ſo if 26 Yards or Ells of any Thing be bought or ſold for 108 *l.* how much will one Yard or Ell be bought or ſold for? *Facit* 3 *l.* for if you divide 108 by 26 Yards, the Quotient will be 3 *l.* the Price of the Integer.

Queſt. 2. If the Expence, Charges, or Wages of 7 Years, amount to 868 *l.* what is the Expence, Charges, or Wages of one Year? *Facit* 124 *l.* for if you divide 868 (the Wages of 7 Years) by 7 (the Number of Years) the Quotient will be 124 *l.* for the Anſwer. See the Work:

```
7) 868 (124
   ...
   7
   --
   16
   14
   --
    28
    28
    --
    (0)
```

Queſt. 3. If the Content of one ſuperficial Foot be 144 Inches, and the Breadth of a Board be 9 Inches, how many Inches of that Board in Length will make ſuch a Foot? *Facit* 16 Inches; for by dividing 144 (the Number of ſquare Inches in a ſquare Foot) by 9, (the Inches in the Breadth of a Board) the Quotient is 16 for the Number of Inches in Length of that Board to make a ſuperficial Foot.

```
9) 144 (16 Inches
   ..
   9
   --
   54
   54
   --
   (0)
```

Queſt. 4. If the Content of an Acre of Ground be16 ſquare Perches, and the Length of a Furlong (propounded be 80 Perches, how many Perches will there go in Breadth to make an Acre: *Facit* 2 Perches; for if you divide 160 the Number of Perches in an Acre, by 80, (the Length of the Furlong is Perches) the Quotient is 2 Perches; an ſo many in Breadth of that Furlong will make an Acre.

80) 160 (2 *Perches.*
160
(0)

Queſt. 5. If there be 893 Men to be made up into Battle, the Front conſiſting of 47 Men; what Number muſt there be in the File? *Facit*, 19 deep in the File; for if you divide 893 (the Number of Men) by 47, the Number in the Front, the Quotient will be 19 in Depth of the File. The Work followeth.

47) 893 (19 *Deep in File.*
47
423
423
(0)

Queſt. 6. There is a Table whoſe ſuperficial Contents i 72 Feet, and the Breadth of it at the End is 3 Feet; now I demand what is the Length of this Table? *Facit* 24 Feet long; for if you divide 72 (the Content of the Table in Feet) by 3 (the Breadth of it) the Quotient is 24 Feet for the Length thereof, which was required. See the Operation in the Margent.

3) 72 (2
6
12
12
(0)

The Proof of Multiplication and Diviſion.

Multiplication and *Diviſion* interchangeably prove eac other; for if you would prove a Sum in *Diviſion*, whether the Operation be right or no, multiply the Quotien

b

by the Diviſor; and if any Thing remain after Diviſion is ended, add it to the Product, which Product (if your Sum was rightly divided) will be equal to the Dividend. And contrariwiſe, if you would prove a Sum in Multiplication, divide the Product by the Multiplier, and if the Work was rightly performed, the Quotient will be equal to the Multiplicand. See the Example, where the Work is done and undone. Let 7654 be given to be multiplied by 3242, the Product will be 24814268, as by the Work appeareth.

```
    7654
    3242
--------
   15308
  30616
 15308
22962
--------
24814268
```

And then if you divide the ſaid Product 24814268 by 3242 the Multiplier, the Quotient will be 7654, equal to the given Multiplicand.

```
3241) 24814268 (7654
      ....
      22694
      -----
       21202
       19452
       -----
        17506
        16210
        -----
         12968
         12968
         -----
          (0)
```

In like Manner (to prove a Sum or Number in *Diviſion*) if 24814268 were divided by 3242, the Quotient will be found to be 7654; then for Proof, if you multiply 7654 the Quotient, by 3242 the Diviſor, the Product will amount to 24814268, equel to the Dividend.

Or, you may prove the laſt or any other Example in *Multiplication*, thus, *viz*. Divide the Product by the Multiplicand, and the Quotient will be equal to the Multiplier. See the Work.

7654

3232

15308

33616

15308

22962

7654) 24814268 (3242

22962

18522

15308

32146

30616

15308

15308

(0)

From whence there ariſes this Corollary, that any Operation in *Diviſion*, may be proved by *Diviſion*; for if after your *Diviſion* is ended, you divide the Dividend by the Quotient, the new Quotient thence ariſing will be equal to the *Diviſor* of the firſt Operation; for Tryal whereof, let the laſt Example be again repeated.

3242) 24814268 (7654

27694

21202

19452

17506

16210

12968

12968

(0)

For Proof whereof divide again 24814268 by the Quotient 7654, and the Quotient hence will be equal to the Diviſion 3244. See the Work:

```
7654) 24814268 (4242
       ....
      22962
      -----
       18522
        15308
       -----
        32146
         30616
        -----
          15308
           15308
          -----
           (0)
```

But in proving *Diviſion* by *Diviſion*, the Learner is to Obſerve this following Caution: That if after his Diviſion is ended, there be any Remainder, before you go about to prove your Work, ſubtract the Remainder out of your Dividend, and then work, as in the following Example, where it is required to divide 43876 by 765, the Quotient here is 57, and the Remainder is 271, See the Work following.

```
765) 43876 (57
       ..
     3825
     ----
      5622
       5355
      ----
      (271)
```

Now to prove this Work, ſubtract the Remainder 271 out of the Dividend 43876, and there remaineth 43605, for a new Dividend to be divided by the former Quotient 57, and the Quotient thence ariſing is 765, equal to the given Diviſor, which proveth the Operation to be right.

```
      43876
        271
     ------
  57)43905 (765
     ....
      399
     ------
       370
       342
     ------
        285
        285
     ------
        (0)
```

Thus have we gone through the four Species of *Arithmetick*, viz. *Addition*, *Subtraction*, *Multiplication*, and *Diviſion*, upon which all the following Rules, and all other Operation whatſoever that are poſſible to be wrought by Numbers, have their immediate Dependance, and by them are reſolved. (Vide *Gem. Friſ.* Arith. Part 1.) Therefore before the Learner make a farther Step in this Art, let him be well acquainted with what has been delivered in the foregoing Chapter.

CHAP. VIII.

Of Reduction.

1. R*Eduction* is that which brings together two or more Numbers of different Denominations into one Denominations, [*Hall's Arith.* c. 13. p. 152.] or it ſerveth to change or alter Number, Money, Weight, Meaſure of Time; from one Denomination to another; and likewiſe to abridge Fractions to the loweſt Terms. All which it doth ſo preciſely, that the firſt Proportion remaineth without the leaſt Job of Error or Wrong committed; ſo that it belongeth as well to the Fractions as Integers of which in the proper Place. *Reduction* is generally performed either by *Multiplication* or *Diviſion*; from whence we may gather, That,

2. *Reduction* is either Aſcending or Deſcending.

3. *Reduction* Deſcending, is when it required to reduce a Sum or Number of a greater Denomination, into a leſſer; which Number, when it is ſo reduced, ſhall be equal in Value to the Number firſt given in the greater Denomination; [*Wing Arith* 7, 2, 3, 4.] as if it were required to know how many Shillings, Pence, or Farthings, are equal in Value to 100 *l.* Or how many Ounces are contained in 4500 Weight. Or how many Days, Hours, or Minutes, there are in 240 Years, &c. And this Kind of Reduction is generally performed by Multiplication.

4. Reduction Aſcending is when it is requied to reduce or bring a Sum or Number of a ſmaller Denomination into greater, which will be equivalent to the given Number, as ſuppoſe it were required to find out how many Pounds, Shillings, or Pence are equal in Value to 43785 Farthings: Or how many Hundreds are equal to (or in) 3748 Pounds, &c. and this Kind of Reduction is always perform'd by Diviſion.

5. When any Sum or Number is given to be reduced into another Denomination, you are to conſider whether it ought be reſolved by the Rule Deſcending or Aſcending, &c. by Multiplication or Diviſion; if it be to be performed by Multiplication, conſider how many Parts of the Denomination into which you would reduce it, are contain'd in an Unit or Integer of the given Number and multiply the ſaid given Number thereby, and the Product thereof will be the Anſwer to the Queſtion. As if the Queſtion were in 38 Pounds how many Shillings; Here I conſider, that in 1 Pound are 20 Sillings, and that the Number of Shillings in 38 Pounds will be 20 times 38, wherefore I multiply 38 *l.* by 20 and the Product is 760, and ſo many Shillings are contained in 38 Pounds, as in the Margent.

38
20
——
760

But when there is a Denomination or Denominations between the Number given and the Number required, you may (if you pleaſe) reduce it into the next inferior Denomination, and then into the next lower than that, &c. until you have brought it into the Denomination required. As for Example, Let it be demanded in 132 Pounds how many Farthings? Firſt, I multiply 132 (the Number of Pounds given) by 20, to bring it into Shillings and it makes 2640 Shillings, then do I multiply the Shillings 2640 by 12, to bring them into Pence, and it produceth 31680, and ſo many Pence are contained in 2640 Shillings, or 132 Pounds; then do I multiply the Pence, *viz.* 31680 by 4 to bring them into Farthing (becauſe 4 Farthings is a Penny) and I find the Product thereof to be 126720, and ſo many Farthings are equal in Value to 132 Pounds. As by the Work in the Margent.

```
 132 Pounds
  20
 ————
 2640 Shill.
   12
 ————
  5280
 2640
 ————
 31680 Pence
     4
 ————
126720 Farth
```

6. And if the Number propounded to be reduced is to be divided, or wrought by the Rule aſcending, conſider how many of the given Numbers are equal to an Unit, or Integer in that Denomination to which you would reduce your given Number, and make that your Diviſor, and the given Number your Dividend; and the Quotient thence ariſing will be the Number ſought or required; As for Example, let it be required to reduce 2640 Shillings into Pounds. Here I conſider that 20 Shillings are equal to one Pound; wherefore I divide 2640 (the given Number) by 20, and the Quotient is 132, and ſo many Pounds are contained in 2640 Shillings. In Reduction deſcending and aſcending, the Learner is adviſed to take particular Notice of the Tables delivered in the ſecond Chapter of this Book, where he may be informed what Multipliers and Diviſors to make Uſe of in the reducing of any Number to any other Denomination whatſoever, eſpecially Engliſh Money, Weights, Meaſures, Time, and Motion; but in this Place it is not convenient to meddle with Foreign Coins, Weights or Meaſures,

```
                l.
2|0) 264|0 (132
 0    ..
      2
    ————
      6
      6
    ————
      4
      4
    ————
     (0)
```

But if in Reduction aſcending, it happen that there is a Denomination or Denominations between the Number given and the Number required, then you may reduce your

Number given into the next ſuperior Denomination, and when it is ſo reduced, bring it into the next above that, and ſo on until you have brought it into the Denomination required. As for Example, Let it be demanded in 126720 Farthings how many Pounds? Firſt I divide my given Number, being Farthing, by 4, to bring them into Pence, (becauſe 4 Farthings make one Penny) and there are 31680 Pence; then I divide 31680 Pence by 12, and the Quotient giveth 2640 Shillings, and then I divide 2640 Shillings by 20, and the Quotient giveh 132 Pounds, which are equal in Value to 126720 Farthings: See the whole Work as it followeth.

```
               12)      2|0)     l.
4) 126720  (21680   (264|0  (132
   .....      ...      ..
    12        24        2
   ----      ----     ----
     6        76        6
     4        72        6
   ----      ----     ----
    27        48        4
    24        48        4
   ----      ----     ----
     32      (0)       (0)
     32
    ----
    (0)
```

7. When the Number given to be reduced conſiſteth of diverſe Denominations, as *Pounds*, *Shillings*, *Pence*, and *Farthings*, or of *Hundreds*, *Quarters*, *Pounds*, and *Ounces*, &c. then you are to reduce the higheſt (or greateſt) Denomination into the next Inferior, and add thereunto the Number ſtanding in the Denomination, which your greateſt or higheſt Number is reduced to; then reduce the Sum into the next inferior Denomination; adding thereto the Number ſtanding in that Denomination; do ſo

```
        l.    s.   d.
       48    13   10
       20
   ---------------------
      960 Shill.
Add    13
   ---------------------
Sum   973 Shill.
       12
   ---------------------
     1946
     973
   ---------------------
    11676 Pence
Add    10
   ---------------------
Sum 11686
```

until you have brought the Number given into the Denomination propoſed. As if it were required to reduce 18 *l.* 13 *s.* 10 *d.* into *Pence*; firſt I bring 48 *l.* into *Shillings*, by multiplying it by 20, and the Product is 960 *Shillings*; to which I add the 13 *Shillings*, and they make 973; then I multiply 973 by 12, to bring the *Shillings* into *Pence*, and they make 11676 *Pence*, to which I add the 10 *d.* and they make 11686 *Pence* for the Anſwer. See the Work done.

8 If in Reduction Aſcending, after Diviſion is ended, any Thing remain, ſuch Remainder is of the ſame Denomination with the Dividend.

Example. In 4783 Farthings, I demand how many Pounds?

Firſt, I divide the given Number of Farthings, *viz.* (4783) by 4, to bring them into Pence, and the Quotient is 1195, and there remaineth 3 after the Work of Diviſion is ended, which is 3 Farthings.

Again, I divide 1195 Pence (the ſaid Quotient) by 12, to reduce them into Shillings, and the Quotient is 99 Shillings, and there is a Remainder of 7, which is 7 Pence.

And then I divide 99 Shillings (the laſt Quotient) by 20, to bring it into Pounds, and the Quotient is 4 *l.* and there remaineth 19 Shillings; ſo that I conclude that in 4783 (the propoſed Number of Farthings) there is 4 Pounds, 10 Shillings, 7 Pence, 3 Farthings: View the following Operation;

```
           12      2|0
4) 4783  (1195    (9|9  4 Pounds
   ....     ..
   4       108     8
   --      ---    --
   7        115  (19) Shillings
   4       108
   --      ---
   38 rem.  (7) Pence
   36
   --                        l.  s.  d.  qrs.
   23                 Facit  04  19  07  03
   20
   --
Rem. 3. Farthings.
```

More Examples in Reduction of Coin.

Queſt. 1. In 438 *l* how many Shillings? *Facit* 8760 Shillings; for by multip'ying the 438 by 20, the Product amounteth to ſo much. See the Work in the Margent.

438 *l.*
20

Facit 8760 *s.*

Queſt. 2. In 476 *l.* how many Pence? Firſt multiply the given Number of Pounds (467) by 20, to bring it into Shillings, and it makes 9340 Shillings, then multiply the Shillings by 12, and it produceth 112080 Pence, as in the Margent.

467 *Pounds*
20

9340 *Shill.*
12

18680
9340

Facit. 112080 *Pence*

Or it may be reſolved thus, *viz.* multiply the given Number of *Pounds* (467) by (240) the Number of *Pence* in a *Pound*, and the Product is the ſame, *viz.* 112080 Pence as by the Operation appeareth.

467 *Poun.*
240

18680
934

Facit. 112080 *Pence*

Queſt. 3. In 5673 *l.* how many Farthings? Firſt multiply the given Number by 20, to bring it into *Shillings*, and it produceth 113460 *Shillings*, then multiply that Product by 12, to bring it into *Pence*, and it produceth 1361520 *Pence*; then laſtly, multiply the Pence by 4, and it produceth 5446080 *Farthings*.

5673 *Pounds*
20

113460 *Shillings*
12

226920
113460

136520 *Pence*
4

Facit 5446080 *Farthings.*

Or this Queſtion might have been thus reſolved, *viz.* multiply 5673 the given Number of the Pounds by 960 (the Number of Farthings in a Pound) and it produceth the ſame Effect, as you may ſee by the Work.

5673 *Pounds*	20 *Shillings*
960	12
340380	240 *Pence*
51057	4
Facit 5446080 *Farth.*	960 *Farthings.*

Otherwiſe thus: Firſt bring the given Number 5673 *l.* into Shillings, and multiply the Shillings by 48, the Number of Farthings in a Shilling, and the ſame Effect is thereby likewiſe produced, *viz.*

5673 *Pounds*	12 *Pence*
20	4
113460 *Shillings*	48 *Farthings.*
48	
907680	
453840	

Fa. 5446080 *Farthings.*

Theſe various Ways of Operation are expreſſed to infrom the Judgment of the Learner, with the Reaſon of the Rule. More ways may be ſhewn, but theſe are ſufficient even for the meaneſt Capacities.

Queſt. 4. In 458 *l.* 16 *s.* 7 *d.* 3 *qrs.* how many Farthings? To reſolve this Queſtion, conſider the 7th Rule of this Chapter, and work as you are there directed, and you will find the aforeſaid given Number to amount to 440479 Farthings, *viz.*

	l.	*s.*	*d.*	*qrs.*
	458	16	7	3
	20			
Add	9160			
	16 *Shillings*			
Sum	9176 *Shillings*			
	12			
	18352			
	9176			
	110112 *Pence*			
Add	7			
Sum	110119 *Pence*			
	4			
	440476 *Farthing*			
Add	3			
Sum	440479 *Farthings*			

This laſt Queſtion, or any other of this Kind, may be more conciſely reſolved thus, *viz.* When you multiply the Pounds by 20, to bring them into Shillings, to the Product of the firſt Figure, add the Figure ſtanding in the Place of Units in the Denomination of Shillings; but becauſe the firſt Figure in the Multiplier is (0) I ſay, 0 times 8 is nothing, but 6 is 6, which I put down for the firſt Figure in the Product, then becauſe the Multiplier is 0, I go on no further with it; for if I ſhould, the whole Product will be 0, but proceed; and when I come to multiply by the ſecond Figure in the Multiplier, to the Product of it, I add the Figure ſtanding in the Place of Tens in the Denomination of Shillings, which is 1, ſaying, 2 times 8 is 16, and (the ſaid Figure) 1 is 17; then I ſet down 7, and carry the Unit to the Product of the next Figure, as is directed in the 5th Rule of the 6th Chapter foregoing, and finiſh the Work. So that now you may have the whole

Product and Sum of Shillings at one Operation, which is the ſame as before; and when you multiply the Shillings by 12, to bring them into Pence, (after the ſame Manner) add to the Product the Number ſtanding in the Denomination of Pence, and ſo when you multiply the Pence by 4, to bring them into Farthings, add to the Product the Number ſtanding under the Denomination of Farthings. See the laſt Queſtion thus wrought.

l.	*s.*	*d.*	*qrs.*
458	16	7	3

20

9176 *Shillings*

12

18359

9176

110119

4

Facit 440479 *Farthings.*

After the Method laſt preſcribed, are all the following Examples, that are of the ſame Nature, wrought and reſolved.

Queſt. 5. In 4375866 Farthings, I demand how many *Pounds*, *Shillings*, *Pence*, and *Farthings?*

To reſolve this Queſtion, Firſt, I divide the given Number of Farthings by 4, and the Quotient is 1093966 Pence, and their remaineth 2 after the Diviſion is ended, which (by the 8th Rule foregoing) is two Farthings; then I divide 1093966 Pence by 12, and the Quotient is 91163 Shillings, and there remaineth 10 after Diviſion, which by the ſaid 8th Rule is ſo many Pence, *viz.* 10 *d.* then I divide 91163 Shillings by 20, and the Quotient 4558 *l.* and there remaineth 3 Shillings; ſo the Work is finiſhed, and I find that in 4375866 Farthings, here are 4558 *l.* 3 *s.* 10 *d.* 2 *qrs.*

```
               (12           (2|0        l.
4) 4375866  (1093966   (9116|3  (4558
   .......    .....      ...

   4           108         8
   ---         ---         ---
   37          13          11
   36          12          10
   ---         ---         ---
   15          19          11
   12          12          10
   ---         ---         ---
   38          76          16
   36          72          16
   ---         ---         ---
    26          46         (3) s.
    24          36
   ---         ---
    26          10 d.
    24
   ---
    (2) qrs.    l.      s.    d.    qrs.
         Facit 4558     3     10    2
```

Queſt. 6. In 4386 *l.* I demand how many Groats?

To reſolve this Queſtion I reduce the given Number of Pounds into Shillings, and they are 87720 Shillings; now I conſider that in a Shilling are 3 Groats, therefore I multiply the Shillings by 3, and it produceth 263160 Groats. See the Work:

```
        4386 Pounds
          20
       -------
       87720 Shillings
           3
       -------
Facit 263160 Groats.
```

This Queſtion might have been otherwiſe reſolved thus, *viz.* conſidering that in a Pound (or 20 Shillings) there are three Times 20 Groats, which makes 60, by which I multiply the Number of Pounds given, and it produceth the ſame Effect at one Operation, as followeth.

4386

4486 *Pounds*
60 *Groats* in 20 *s*,

Facit 263160 *Groats* 4386 *l*.

Queſt. 7. In 43758 Three-pences, I deſire to know how many Pounds?

To reſolve this, and many ſuch like Queſtions: Firſt, I divide my given Number of Three-pences by 4, becauſe 4 Threeipences are in a Shilling, and the Quotient is 10939 Shillings, and there remaineth 2 after Diviſion is ended, which is two Three-pences (by the 8th Rule of this Chapter) which are equal in Value to 6 *d*. then I divide 10939 Shillings by 2, and the Quotient giveth 546 *l*. and 19 *s*. remains: So that I conclude in 43758 Pieces of Three-pence *per* Piece, there are 546 *l*. 19 *s*. 6 *d*. as by the Work appeareth:

```
4) 43758   2|0       l.   s.  d.
    ···:  (1093|9  (546  19  06
   4        ···
 ———        10
   37     ———
   36        9
 ———         8
    15    ———
    12       13
 ———         12
     38   ———
     36    19 Shillings
   ———
  (2) Three-pence or 6 d.
```

This Queſtion might have been otherwiſe reſolved thus, *viz.* Firſt multiply the given Number of Three-pences 43758, by 3 the Number of Pence in Three-pences, and the Product (*viz.* 131274) is the Number of Pence equa to the given Number of Three pences. which Number o Pence may be brought into Pounds by dividing by 12, an by 20, and the Quotient you will find to be equal to th former Work, 546 *l*. 19 *s*. 6 *d*.

```
         43758
             3
——  ————————  ——2|0      l.    s.   d.
12 ) ( 131274 (1093|9 (546   19   6
       .....    ...
        12      10
        ——      ——
        112      9
        108      8
        ———     ——
         47     13
         36     12
         ——    ———
        114 re. (19) Shillings
        108
        ———
        (6) Pence remains.
```

Or thus, Divide the given Number of 3 Pences by the Number of 3 Pences in a Pound, or 20 Shillings (which you will find to be 80, if you multiply 20 *s.* by 4, the Number of 3 Pences in a Shilling) and you will find the Quotient to 546 *l.* as before, and a Remainder of 78 Three-pences; and if you divide thoſe 78 Three pences by 4 (becauſe there are 4 Three-pences in a Shilling, you will find the Quotient to be 19 *s.* and 2 Three-pences remain, which are equal to 6 *d.* which is the ſame that was before ſound.

```
8|0) 4375|8 (546   19   6        20
     . . .                        4
   ---------                    ----
      40                         80
   ---------
      37
      31
   ---------
      55
      48
   ---------
4)    78 (19 s.
      . .
       4
   ---------
      38
      36
   ---------
```

(2) Three-pences or 6 *d.*

Queſt 8. In 4785 *l.* 13 *s.* how many Pieces of 13 *d.* ½ per Piece?

This Queſtion cannot be reſolved by Reduction Deſcending or Aſcending abſolutely, (becauſe 13 *d.* ½ is no even Part of a Pound) but rather by them both jointly, *viz.* by Multiplication and Diviſion, but if you bring the Number given into Half-pence, and divide the Half-pence by the Half-pence in 13 *d.* ½, *viz.* 27, the Quotient will be the Anſwer; for having brought 4785 *l.* 13 *s.* into Half-pence, I find it makes 2297112, which I divide by 27, (becauſe there are ſo many Half-pence in 13 *d.* ½) and the Quote gives 85078 Pieces of 13 *d.* ½, and 6 Half-pence remain over and above: Obſerve the Work following.

l. *s.* *d.*

4785 13 13 ½

20 2

95713 Shillings 27 Half-pence

24 Half-pence in a Shilling.

382852

191426

2297112 Half-pence in the given Number

27) 2297112 (85078 Pieces of 13 *d.* ½.

216

137

135

211

189

222

216

Remains (6) Half-pence.

It would have produced the ſame Anſwer, if you had reducedd your given Number into Farthings, and divided by the Farthings in 13 *d.* ½, *viz.* 54; (for always the Dividend and the Diviſor muſt be of one Denomination) and then you would have had a Remainder of 12 Farthings, which are equal in Value to the former Remainder of 6 Half-penee, as you may prove at your Leiſure.

Queſt. 9. In 540 Dollars at 4 *s.* 4 *d. per* Dollar, how many Pounds Sterling?

Firſt, bring your given Number of Dollars into Pence, and then your Pence into Pounds, according to the former Directions, Thus in 4 *s.* 4 *d.* (*viz.* a Dollar) you will find 52 Pence, by which multiply 540 Dollars, and it produceth 28080 Pence, which if you divide by 246 (the Pence in one Pound) the Quotient will give you 117 *l.* which are equal in Value to 540 Dollars, at 4 *s.* 6 *d. per* Dollar.

s. d.
540 4 4
51 12
1084 52
2700
24|0) 2808|0 (117
. . .
24
40
24
168
168
(0)

The foregoing Queſtion might have been otherwiſe wrought thus, *viz.* Multiply 540, your given Number of Dollars, by 13 the Number of Groats in a Dollar; or 4 *s.* 4 *d.* and it produceth 7020 Groats, which divide by 60, the Groats in one Pound, or 20 Shillings, and the Quote is 117, as before. See the Work.

s. d.
540 4 4
133 3
1620 13
540
6|0) 702|0 (117
. . .
6
10
6
42
42
(0)

Queſt. 10. In 547380 Pieces of 4 *d.* ½ *per* Piece, I demand how many Pounds, Shillings, and Pence?

Firſt bring your given Number Four-pence Half penny all into Half-pence, which you will do if you multiply by 9, the Number of Half-pence in 4 *d.* ½, and the Product is 4926474 Half-pence, which are brought into Pounds, if you divide them by 24, the Half-pence in a Shilling, and 20, the Shillings in a Pound, it makes 10263 *l.* 9 *s.* 9 *d.*

```
                                                      d.
                                                      4 d.
       547386                                         2
            9                                       ----
  ------------ 2|0        l.                          9 Half-pen.
24) 4926474 (20526|9 (10263
    .......  .......
    48        2
    ---      ---
    126       05
    120        4
    ----     ---
     61       12                                 l.     s.  d.
     48       12                         Facit 10263    9   9
    ---      ----
    167        6
    144        6
    ----     ---
     234 rem.  (9) Shillings.
     216
    ----
Rem. (18) Half-pence, or 9 d.
```

Queſt. 11. In 4386 *l.* I demand how many Pieces of 6 *d.* of 4 *d.* and of 2 *d.* of each an equal Number? That is to ſay, What Number of Six-pences, Groats, and Two-pences will make 4386 *l.* and the Number of each equal?

The Way to reſolve Queſtions of this Nature, is to add the ſeveral Pieces into which the given Number is to be brought into one Sum, and reduce the given Number into the ſame Denomination with their Sum, and to divide the ſaid given Number (ſo reduced) by the ſaid Sum, and the Quotient will give you the exact Number of each Piece. And after the ſame Method will we proceed to reſolve the preſent Queſtion, *viz.*

4386 Pounds
240 Pence

175440
8772

12) 1052640 (87720
96

92
84

86
84

24
24

(0)

6 *d.*
4 *d.*
2 *d.*

Sum 12 *d.*

d. *d.* *d.*
Facit 87720 Pieces of 6 4 2

So that I conclude by the Operation, that 87720 Six-pences, and 87720 Groats, and 87720 Two-pences, are juſt as much (or equal to) 4386 *l.* or if you admit of 5 *s.* to be thus divided, it is equal to 5 Six-pences, and 5 Four-pences or Groats, and 5 Two-pences.

Another Queſtion of the ſame Nature with the laſt, be this following, *viz.*

Queſt. 12. A Merchant is deſirous to change 148 *l.* into Pieces of 13 *d.* ½, of 12 *d.* of 9 *d.* and 6 *d.* of 4 *d.* and he will have of each ſort an equal Number of Pieces, I deſire to know the Number?

Do as you were taught in the laſt Queſtion, *viz.* add the ſeveral Pieces together, and reduce the Sum into Half-Pence, then reduce the Sum to be changed, *viz.* 148 *l.* into the ſame Denomination, and divide the Greater by the Leſſer, and in the Quotient you will find the Anſwer, *viz.* 798 is the Number of each of the Pieces required, and 18 remaineth, which is 18 Half-pence by the 8th Rule of this Chapter. See the Work as followeth;

l.	*d.*
148	13 ½
240 Pence in a Pound	12
	9
5920	6
296	4
35520 Pence in 148 *l.*	Sum 44
2	2 ½
71040 Half-pence	89 Half-pence.

89) 71040 (797 Pieces of each Sort

...

623

874

801

730

712

Rem. (18) Half-pence.

The Truth of the two foregoing Operations will thus e proved, *viz.* Multiply the Anſwer by the Parts or ieces into which the given Number was reduced, and aving added the ſeveral Products together, if their Sum e equal to the given Number, the Anſwer is right, other-ise not; ſo the Anſwer to the 11th Queſtion was 87720; hich is proved as followeth, *viz.*

		l.
87720	Six Pences make	2193
	Four Pences make	1462
	Two-pences make	731

The Total Sum of them 4386 which was the Sum given to be changed.

The Anſwer to the 12th Queſtion was 738, and 18 alf-pence remained after the Work was ended, now the ruth of the Work may be proved as the Former, *viz.*

798

		l.	*s.*	*d*
789	Pieces of 13 ½ make	44	17	09
	Pieces of 12 make	39	18	00
	Pieces of 9 make	29	18	0
	Pieces of 6 make	19	19	00
	Piece of 4 make	12	06	00
	and 18 Half-pence, or 9 *d.* remain	00	00	09
	The Total Sum of them	148	00	00

which total Sum is equal to the Number that was firſt given to be changed, and therefore the Operation was rightly performed.

Reduction of Troy weight.

We come now to give the Learner a few Examples in Troy-weight; in working whereof he muſt be mindfu of the Table of Troy-weight delivered in the ſecond Chapter of this Book.

Queſt. 13. In 482 *l.* 7 *oz.* 13 *p. w.* 21 *gr.* how man Grains?

Multiply by 12, by 20 and by 24, taking in the Figures ſtanding in the ſeveral Denominations, according to the Direction given in the Seventh Rule of this Chapter, and you will find the Product to be 2780013 Grains, which is the Number required, or Anſwer to the Queſtion. See the whole Work, as in the Margent.

```
  l.   oz. p.w. gr.
  482   7   13   21
   12
  ----
  971
 482
 -----
 5791 Ounces
   20
 ------
115833 Penny-weight
    24
 ------
 463333
231668
-------
Facit 2780013
```

Queſt. 14. 2780013 Grains, I demand how man Pounds, Ounces, Penny-weights, and Grains?

This is but the foregoing Queſtion inverted, and i reſolved by dividing by 24, by 20, and by 12, and th Anſwer is 482 *l.* 7 *oz.* 13 *p. w.* 21 *gr.*

```
                 2|0        12)
24) 2780013 (11583|3 (5791 (482 l.
     .......     ....     ...
    24          10       48
    --          --       --
    38          15       99
    24          14       96
    --          --       --
     140        18       31
     128        18       24
     ---        --       --
      200        3 Rem.  7 Ounces
      192        2
      ---
       81 Rem. 13 Penny-weight.
       72
       --
       93
       72
       --
```

	l.	oz.	p. w.	gr.
Facit	482	7	13	21

Remain 21 Grains.

Queſt. 15. A Merchant ſent to a Goldſmith 16 Ingots of Silver, each containing in Weight 2 *l.* 4 *oz.* and ordered it to be made into Bowls of 2 *l.* 8 *oz.* *per* Bowl, and Tankards of 1 *l.* 6 *oz.* *per* Piece, and Salts of 10 *oz.* 10 *p. w.* *per* Salt, and Spoons of 1 *oz.* 18 *p. w.* *per* Spoon, and of each an equal Number; I deſire to know how many of each Sort he muſt make?

This Queſtion is of the ſame Nature with the 11th and 12th Queſtion foregoing, and may be anſwered after the ſame Method, *viz.* Firſt, add the Weight of the ſeveral Veſſels, into which the Silver is to be made, into one Sum, and reduce to one Denomination, and they make 1248 Penny-weights; then reduce the Weight of the Ingot into the ſame Denomination, *viz.* Penny-weights, and it makes 560 Penny-weights, and multiply them by the Number of Ingots, *viz.* 16, and the Product will give you the Weight of the 16 Ingots, *viz.* 8960; then divide the Product by the Weight of the Veſſels, *viz.* 1248, and the Quotient giveth you the Anſwer to the Queſtion, *viz.* 7, and 224 *p. w.* remaineth over and above.

l.	oz.
2	4
12	
28	
20	

560 Penny-weights
16 Ingots

3560
560

1248)8960(7 Veſſels of each
8736

Rem. (224) Penny-weights

	l.	oz.	p.
	2	08	
	1	06	
	0	10	
	0	01	
Sum	5	02	
	12		
	62		
	20		
	1248		

The Proof of the Work as followeth, viz.

		l.	oz.	p w.		l.	oz. p.
7	Bowls of	2	08	00	*per* Bowl is	18	06
	Tank. of	1	06	00	*per* Tank. is	10	06
	Salts of	0	10	16	*per* Salt, is	06	16
	Spoons of	0	01	18	*per* Spoon, is	01	01
	224 Penny-weight remaining					00	11
						37	04

So that you ſee the Sum of the Weight of each Veſſ together with the Remainder, is 37 *l.* 4 *oz.* which equal to the Weight of the 16 Ingots delivered. For 37 *l.* 4 *oz.* be reduced to Penny-weights, it mak 8960.

Reduction of Averdupois-weight.

In reducing Averdupois-weight the Learner muſt have Recourſe to the Table of Averdupois-weight, delivered in the ſecond Chapter.

Queſt. 16. In 47 *C.* 2 *qrs.* 20 *l.* how many Ounces? Multiply by 4, by 28, and 16, and the laſt Product will be the Anſwer, *viz.* 84992 Ounces. See the Margent.

```
  C.  qr.  l.
  47   1   20
   4
 ----
 189 Quars.
  28
 ----
 2512
 380
 ----
 5312 l.
   16
 -----
 31872
 5312
 -----
Facit 84992 Ounces
```

Queſt. 17. In 84992 Ounces, I demand how many *C. qrs. l.* and *oz.*

This is the foregoing Queſtion inverted, and will be reſolved, if you divide by 16, by 28, and by 4, and the Anſwer is 47 *C.* 1 *qr.* 20 *l.* equal to the given Number in the foregoing Queſtion.

```
         28)     4)     C.  qr.  l.  oz.
16) 84992 (5312 (189 (47   1   20  00
    ....   ...   ..
     80    28    16
    ----  ----  ----
     49    251   29
     48    224   28
    ----  ----  ----
     19    272   (1) qr.
     16    252
    ----  ----
     32    (20) Pounds.
     32
    ----
    (0)
```

Reduction of Liquid Meaſure.

Queſt. 18. In 45 Tuns of Wine how many Gallons? Multiply by 4, and by 63, the Product is 11340 Gallons or the Anſwer.

```
  45
   4
 ---
 180
  63
 ---
 540
1080
----
```

Facit 11340 Gallons.

Queſt. 19. In 34 Rundlets of Wine, each containing 18 Gallons, I demand how many Hogſheads?

Firſt, find how many Gallons are in the 34 Rundlets, which you may do, if you multiply 34 by 18, the Content of a Rundlet, and the Product is 612 Gallons, which you may reduce into Hogſheads, if you divide them by 63, and the Quote will be 9 Hogſheads, and 45 Gallons, See the Work.

```
      (34
       18
      ---
      272
      34
63) 612 (9 hhds.

      567        Facit 9 hhds, 45 Gallons.
      ---
 Rem. 45 Gallons
```

Queſt. 20. In 12 Tun, how many Rundlets of 14 Gallons *per* Rundlet?

Reduce your Tuns into Gallons, and divide them by 14, the Gallons in a Rundlet, and the Quotient, 216 is your Anſwer. See the Work following.

12

12
4

48
63

144
28

14) 3024 (216 Rundlets.

28

22
14

84
84

(0) *Facit* 216 Rundlets.

Reduction of Long-Meaſure.

Queſt. 21. I demand how many Furlongs, Poles, Inches, and Barly-corns will reach from *London* to *York*, it being accounted 151 Miles?

151 Miles
8 Furlongs in a Mile

1208 Furlongs
40 Poles in a Furlong

48320 Poles
11 Half-yards in a Pole

48320
48320

531520 Half yards
18 Inches in Half a Yard

4252160
531520

9567360 Inches
3 Barly-corns in one Inch

Facit 28702080 Barly-corns in 151 Miles.

Queſt. 22. The Circumference of the Earth (as all othe Circles are) is divided into 360 Degrees, and each Degree into 60 Minutes, which (upon the Superficies of th Earth) are equal to 60 Miles; now I demand how man Miles, Furlongs, Perches, Yards, Feet, and Barly-corns will reach round the Globe of the Earth?

360 Degrees
60 Minutes or Miles in a Degree

21600 Miles about the Earth
8 Furlongs in a Mile

172800 Furlongs about the Earth
40 Perches in a Furlong

6912000 Poles or Perches about the Earth
11 Half-yards in a Perch

6912000
6912000

2)76032000 Half-Yards upon the Earth

(38016000 Yards, *viz.* the Half-yards
3 Divided by 2

114048000 Feet about the Earth
12 Inches in a Foot

228029000
114048000

1361576000 Inches about the Earth

3 Barly-corns in an Inch

Fa. 4105728000 Barly-corns.

And ſo many will reach round the World, the whole being about 21600 Miles; ſo that if any Perſon were to go round, and go 15 Miles every Day, he would go the whole Circumference in 1140 Days; which is 3 Years, 11 Months, and 15 Days.

Reduction of Time.

Queſt. 23. In 28 Years, 24 Weeks, 4 Days, 16 Hours, 30 Minutes, how many Minutes?

Years	*Weeks*	*Days*	*Hours*	*Minutes*
28	24	4	16	30

52 Weeks in a Year

60
142

1480 Weeks
7

10364 Days
24

41462
20729

248752 Hours
60

14925150 Minutes

Note, That in reſolving the laſt Queſtion after the Method expreſſed, there is loſt in every Year 30 Hours. For the Year conſiſteth of 365 Days and 6 Hours; but by multiplying the Year by 52 Weeks, which is 364 Days, you loſe 1 Day and 6 Hours every Year; wherefore to find an exact Anſwer, bring the odd Weeks, Days, and Hours into Hours, and then multiply the Years by the Number of Hours in the Year, *viz.* 8766, and to the Product add the Hours contained in the odd Time, and you have the exact Time in Hours, which bring into Minutes, as before. See the laſt Queſtion thus reſolved:

```
                                        Weeks   Days   Hours
                                          24      4      16
                                           7
                                        ----
                 Days   Hours             172
        28       365      6                24
      8766        24                      ----
      ----       ----                     694
       172       1466                     345
       172       730                      ----
       197       ----                     4144 Hours
       228       8766 Hours in a Year.
      ------
      249592 Hours
      ------
          60
    --------
    14975520 Minutes in 28 Years, and 4144 Hours.
```

So you ſee that according to the Method firſt uſed to reſolve this Queſtion, the Hours contained in the given Time are 248752, but according to the laſt, beſt, or trueſt Method, they are 249592, which exceeds the former by 840 Hours.

But for moſt Occaſions it will be ſufficient to multiply the given Years by 365, and to the Product add the Days in the odd Time, if there be any, and then there will be only a Loſs of ſix Hours in every Year, which may be ſupplied by taking a fourth Part of the given Years, and adding it to the contained Days, and you have your Deſire.

Queſt. 24. In 438657540 Minutes, how many Years? *Facit* 834 Years, 4 Days, 19 Hours.

```
                      8766       Years   Days   Hours
6|0) 43865754|0 (7310659 (834    4      19
     .......        ...
   42              70128
   --              -----
   18               29815
   18               26298
   --               -----
    6               35199
    6               35064
   --               -----
   57          24) 115 (4 Days
   54                .
   --               96
    35              --
    30        Rem. (19) Hours
    --
     54
     54
     --
     (0)
```

Queſt. 25. I deſire to know how many Hours and Minutes it is ſince the Birth of our Saviour Jeſus, being accounted 1722 Years?

This Queſtion is of the ſame Nature with the 24th foregoing, and after the ſame Manner is reſolved. *viz.* multiply the given Number of Years by 8766, the Product is 15095052 Hours; and that by 60, and the Product is 905703120 Minutes. See the Work.

```
      41722 Years
       8766 Hours in a Year
    --------
      10332
     10332
    12054
   13776
   --------
   15095052 Hours in in 1722 Years.
         60
   ---------
  905703120 Minutes in 1722 Years.
```

Note. That as Multiplication and Diviſion do interchangeably prove each other, ſo Reduction Deſcending and Aſcending, prove each other by inverting the Queſtion, as the 13th and 14th, and likewiſe the 16th and 17th Queſtions foregoing by Inverſion, do interchangeably prove each other. The like may be performed for the Proof of any Queſtion in Reduction whatſoever.

CHAP. IX.

Of Comparative Arithmetick; viz. The Relation of Numbers one to another.

1. COmparative Arithmetick, is that which is wrought by Numbers, as they are conſidered to have Relating one to another, and this conſiſts either in Quantity or in Quality. Vide *Boetiu*'s Arith. Lib. 1. cap. 21.

2. Relation of Numbers in Quantity, is the Reference or Reſpect that the Numbers themſelves have to one another, where the Terms of Numbers propounded are always too, the firſt called the Antecedent, and the other the Conſequent. (See *Wing*. Arithm.)

3. The Relation of Numbers in Quantity conſiſts in the Differences, or in the Rate or Reaſon that is found betwixt the Terms propounded, the Differences of two Numbers being the Remainder found by Subtraction, (according to *Alſtead*) but the Rate or Reaſon betwixt two Numbers is the Quotient of the Antecedent divided by the Conſequent, ſo 21 and 7 being given, the Difference betwixt them will be found to be 14, but the rate or Reaſon that is betwixt 21 and 7, will be found to be triple Reaſon, for 21 divided by 7, quotes 3, the Reaſon or Rate.

4. The Relation of Numbers in Quality (otherwiſe called Proportion) is the Reference or Reſpect that the Reaſon of Numbers have one unto another; therefore the Terms given ought to be more than two, Now the Proportion or Reaſon between Numbers relating one to another, is either Arithmetical or Geometrical.

5. Arithmetical Proportion is, when diverſe Numbers differ one from another by equal Reaſon; that is, have equal Differences.

So this Rank of Numbers, 3, 5, 7, 9, 21, 13, 15, 17, differ by equal Reaſon, *viz.* by 2, as you may prove.

6. In a Rank of Numbers that differ by Arithmetical Proportion, the Sum of the firſt and laſt Term being multiplied by half the Number of Terms, the Product is the total Sum of all the Terms.

Or, if you multiply the Number of the Terms by the half Sum of the firſt and laſt Terms, the Product is the total Sum of all their Terms.

So in the former Progreſſion given, 3 and 17 is 20, which multiplied by 4, *viz.* Half the Number of Terms, the Product gives 80, the Sum of all the Terms; or multiply 8 (the Number of Terms by 10) half the Sum of the firſt and laſt Term, the Product gives 80 as before.

So alſo, 21, 18, 15, 12, 9, 6, 3, being given, the Sum of all the Terms will be found to be 84; for here the Number of Terms is 7, and the Sum of the firſt and laſt (*viz.* 21 and 3) is 24, half whereof, (*viz.* 12) multiplied by 4, produceth 84, the Sum of the Terms ſought.

7. Three Numbers that differ by Arithmetical Proportion, the Double of the Mean (or middle Number) is equal to the Sum of the Extreams.

So 9, 12, and 15, being given, the Double of the Mean 12, (*viz.* 24) is equal to the Sum of the two Extreams 9 and 25.

8. Four Numbers that differ by Arithmetical Proportion (either contained or interupted) the Sum of the two Means is equal to the Sum of the two Extreams.

So 9, 12, 18, 21, being given, the Sum of 12 and 18, will be equal to the Sum of 9 and 21, *viz.* 30; alſo 6, 8, 14, 16, being given, the Sum of 8 and 14 is equal to the Sum of 6 and 16, *viz.* 22, &c. See *Wingate*'s Arith. c. 35.

9. Geometrical Proportion (by ſome called Geometrical Progreſſion) is when diverſe Numbers differ, according right Reaſon.

So 1, 2, 4, 8, 16, 32, 64, &c. differ by Double Reaſon; and 3, 9, 27, 81, 243, 729 differ by triple Reaſon; 4, 17, 64, 256, &c. diffes by quadruple Reaſon, &c.

10. In any Number that increaſe by Geometrical Proportion, if you multiply the laſt Term by the Quotient of any one of the Terms divided by another of the Terms which being leſs is next unto it, and having deducted, or ſubtracted the firſt Term out of that Product, divide the Remainder by a Number that is an Unit leſs than the ſaid Quotient, the laſt Quote will be the Sum of all the Term.

So 1, 2, 4, 8, 16, 32, 64 being given, firſt I take one of the Terms, *viz.* 8, and divide it by the Term which is leſs, and next to it (*viz.* by 4) and the Quotient is 2, by which multiply the laſt Term by 64, and the Product is 128 from whence I ſubtract the firſt Term, (*viz.* 1.) the Remainder is 127, which divided by the Quotient 2 made leſs by 1, *viz.* 1. the Quotes is 127, for the Sum of all given Trems, as by the Work in the Margent.

64
4) 8 (2
128
1
1) 127 (127

So if 4, 16, 64, 256, 1024. were given, the Sum of all the Terms will be found to be 1364. For firſt, I divide 64, one of the Terms, by the next leſſer Term, and the Quotient is 4, by which I multiply the laſt Term 1024 and it produceth 4096; from whence I ſubtract the firſt Term 4, and the Remainder is 4092, which I divide by the Quote leſs by 1, *viz.* 3 and the Quote is 1364, for the total Sum of all the Terms as *per* Margent.

1024
16) 64 (6
4096
4
3) 4092 (364

11. Three Geometrical Proportionals given' the Square of the Mean is equal to the Rectangle, or Product of the Extreams.

So 8, 16, 32, being given, the Square of the Mean, *viz.* 16, is 256, which is equal to the Product of the Extreams 8 and 32, for 8 times 32 is equal to 256.

12 Of Four Geometrical proportionable Numbers given, the Product of the two Means is equal to the Product of the two Extreams.

So 8, 16, 32, 64, being given, I ſay, that the Product of the two Means, *viz.* 19 Times 32, which is 512, is equal to 8 times 64, the Product of the Extreams.

Alſo if 3, 9, 21, 63, were given, which are inturrupted, I ſay, 9 Times 21 is equal to 3 Times 63, which is equal to 189.

From hence ariſeth that precious Gem in Arithmetick, which for the Excellency thereof is called the *Golden Rule*, or *Rule of Three*.

CHAP. X.

The Single Rule of Three Direct.

1. THE Rule of Three (not underſervedly called the Golden Rule (is that by which we find out a fourth Number in Proportion unto three given Numbers, ſo as this fourth Number that is ſought may bear the ſame Rate, Reaſon, and Proportion to the third (given) Number, as the ſecond doth to the firſt, from whence it is called the Rule of Proportion.

2. Four Numbers are ſaid to be proportional, when the firſt containeth, or is contained by the ſecond, as often as the third containeth, or is contained by the fourth. Vide *Wingate*'s Arith. Chap. 8. Sect. 4.

So theſe Numbers are ſaid to be Proportionals, *viz.* 3, 6, 9, 11, for as often as the firſt Number is contained in the ſecond, ſo often is the third contained in the fourth, *viz.* twice. Alſo, 9 3, 15, 5, are ſaid to be Proportionals; for often as the firſt Number containeth the ſecond, ſo often the third Number containeth the fourth, *viz.* 3 Times.

3. The Rule of Three is either Simple or Compound.

4. The Simple (or Single) Rule of Three, conſiſteth of 4 Numbers, that is to ſay, it hath 3 Numbers given to find out a Fourth, and this is either Direct or Inverſe, Vide *Alſtead Math.* lib. 2 c. 13.

5. The Single Rule of Three Direct, is when the Proportion of the firſt Term is to the ſecond, as the third is to the fourth, or when it is required that the Number ſought, (*viz.*) the fourth Number muſt have the ſame Proportion to the ſecond, as the third hath to the firſt.

6. In the Rule of Three, the greateſt Difficulty is to diſcover the Order of the 3 Terms of the Queſtion pro-

pounded, *viz.* which is the firſt, ſecond, and the third; which that you may underſtand; obſerve, that of the Three given Numbers, two always are of one Kind, and the other as of the ſame Kind, with the proportional Number that is ſought; as in this Queſtion, *viz.* If 4 Yards of Cloth coſt 12 Shillings, what will 6 Yards coſt at that Rate? Here the two Numbers of one Kind are 4 and 6, *viz.* they both ſignify ſo many Yards, and 12 *s.* is the ſame Kind with the Number ſought, for the Price of 6 Yards is ſought.

Again obſerve, That of the 3 given Numbers, thoſe two that are of the ſame Kind, one of them muſt be the firſt, and the other the third, and that which is of the ſame Kind with the Number ſought, muſt be the ſecond Number in the Rule of Three; and that you may know which of the ſaid Numbers to make your firſt, and which your third, know this, that to one of theſe two Numbers, there is always affixed a Demand, and that Number upon which the Demand lieth, muſt always be reckoned the third Number. As in the forementioned Queſtion, the Demand is affixed to the Number 6, for it is demanded, what 6 Yards will coſt, and therefore 6 muſt be the third Number, and 4 (which is of the ſame Denomination or Kind with it) muſt be the firſt, and conſequently the Number 12 muſt be the ſecond; and then the Number being placed in the forementioned Order, will ſtand as followeth *viz.*

yards	*s.*	yards
4	12	6

7. The next Thing is, to find out the fourth Number in Proportion; which that you may do, multiply the ſecond Number by the third, and divide the Product thereof by the firſt, or (which is all one) multiply the 3d Term (or Number) by the ſecond, and divide the Product thereof by the firſt, and the Quotient thence ariſing is the 4th Number in a direct Proportion and is the Number ſought or Anſwer to the Queſtion, and is of the ſame Denomination that the ſecond Number is of. As thus; Let the ſame Queſtion be again repeated, *viz.* If 4 Yards of Cloth coſt 12 Shillings, what will 6 Yards coſt?

Having placed my Numbers according to the ſixth Rule (of this Chapter) foregoing, I multiply (the ſecond Number) 12, by (the third Number) 6, and the Product is 72, which Product I divide by the firſt Number 4, and the Quotient thence ariſing is 18, which is the 4th Proportional or Number ſought, *viz.* 18 Shillings, (becauſe the ſecond Number is Shillings) which is the Price of 6 Yards, as was required by the Queſtion. See the Work following.

	yds	s.	yds	s.
If	4	12	6	18

6

4) 72 (18 Shillings

4

32

32

(0)

Queſt. 2. Another Queſtion may be this, *viz.* If 7 C. of Pepper coſt 28 *l.* how much willl 16 *C.* coſt at that Rate?

To reſolve which Queſtion, I conſider that (according to the ſixth Rule of this Chapter) the Terms or Numbers ought to be placed thus, *viz.* the Demand lying upon 16 C. it muſt be the third Number, and that of the ſame Kind with it muſt be the firſt, *viz.* 7 C. and 21 *l.* (being of the ſame Kind with the Number ſought) muſt be the ſecond Number in this Queſtion; then I proceed according to this ſeventh Rule, and multiply the ſecond Number, by the third, *viz.* 21 by 16, and the Product is 337 which I divide by the firſt Number 7, and the Quotient is 48 *l.* which is the Value of 16 *C.* of Pepper at the Rate of 21 *l.* for 7 *C.* See the Work following.

```
C.    l.    C.
7     21    16
      16
     ---
     126
      21
     ---
  7) 336 (48 l
     ..
      28
     ---
      56
      56 Facit 48 l.
     ---
     (0)
```

8. If when you have divided the Product of the 2d and 3d Numbers by the firſt, any Thing remain after Diviſion is ended, ſuch Remainder may be multiplied by the Parts of the next inferior Denomination, that are equal to an Unit (or Integer) of the ſecond Number in the Queſtion, and the Product thereof divide by the firſt Number in the Queſtion, and the Quotient is of the ſame Denomination with the Parts by which you multiplied the Remainder, and is Part of the 4th Number which is ſought, And furthermore, if any Thing remain, after this laſt Diviſion is ended, multiply it by the Parts of the next inferior Denomination equal to an Unit of the laſt Quotient, and divide the Product by the ſame Diviſor, *viz.* The firſt Number in the Queſtion) and the Quote is ſtill of the ſame Denomination with your Multiplier ; follow this Method until you have reduced your Remainder into the loweſt Denomination, *&c.* An Example or two will make this Rule very plain, which may be the following.

Queſt. 3. If 13 Yards of Velvet, *&c.* coſt 21 *l.* what will 27 Yards of the ſame coſt at that Rate?

Having ordered and wrought my Numbers according to the 6th and 7th Rule of this Chapter, I find the Quotient to be 43 *l.* and there is a Remainder of 8, ſo that I conclude the Price of 27 Yards to be more than 43 *l.* and to the Intent that I may know how much more, I Work according to the foregoing Rule, *viz.* I multiply the ſaid Remainder 8 by 20 *s.* (becauſe the ſecond Number in the Queſtion was Pounds) and the Product is 160, which divided by the firſt Number, *viz.* 13, it quotes 12, which are 12 Shillings; and there is yet a Remainder of 4, which I multiply by 12 Pence (becauſe the laſt Quotient was Shillings) and the Product is 48, which I divide by 13 (the firſt Number) and the Quotient is 3 *d.* and yet there remaineth 9, which I multiply by 4 Farthings, and the Product is 36, which I divide by 13 again, it quotes 2 Farthings, and there is yet a Remainder of 10, which (becauſe it cometh not to the Value of a Farthing) may be neglected, or rather ſet after the 2 Farthings over the Diviſor, with a Line between them; and then (by the 21ſt and 22d Definitions of the firſt Chapter of this Book) it will be $\frac{10}{13}$ of a Farthing, ſo that I conclude, that if 13 Yards of Velvet coſt 21 *l.* 27 Yards of the ſame will coſt 43 *l.* 12 *s.* 3 *d.* 2$\frac{10}{13}$ *qrs.* which Fraction is 10 Thirteens of a Farthing. See the Operation as followeth;

If

yds. *l.* yds.
If 13 21 27
27

147
42

13) 567 (43 *l.*
· ·
52

47
39

Remain (8)
Multiply 20

13) 160 (12
· · ·
13

30
26

Remain (4)
Multiply 12

13) 48 (3 *d.*
39

Remain (9)
Multiply 4
qrs.
13) 36 (2 $\frac{10}{13}$
26 *l.* *s.* *d.* *qrs.*
Remain 10 *Facit* 43 12 3 2 $\frac{10}{13}$.

Queſt. 4. Another Example may be this following, *viz.* If 14 Pound of Tobacco coſt 27 *s.* what will 478 Pound coſt at that Rate?

Work according to the laſt Rule, and you will find it to amount to 921 *s.* 10 *d.* 1 $\frac{1}{14}$ *qrs.* and by the 5th Rule of the 8th Chapter 921 *s.* may be reduced to 46 *l.* 1 *s.* So that then the whole Worth or Value of the 478 *l.* will be 46 *l.* 1 *s.* 10 *d.* $\frac{2}{14}$. The Work followeth.

```
             l.   s.   d.
          If 14   27   478
                        27
                      ----
                      3346
                       956
                      ----
         ---------1|0
    14) 12906 (92|1 (46 l.
         126      8
         ---     ---
          30      12
          28      12
         ---     ---
          26     (1) s.
          14
         ---
 Remains (12)
 Multiply 12
         ---
          24
          12
         ---
    14) 144 (10 d.
         14
         ---
 Remains (4)
 Multiply 4
    14) (16) 1 2/14
         14
         ---
 Remains (2)
    Facit 46   1   10   1 2/14.
          l.   s.  d.   qrs.
```

9. In the Rule of Three it many times happens, that although the firſt and third Numbers be one Kind, as both Money, Weight, Meaſure, &c. yet they may not be of one Denomination, or perhaps they may both conſiſt of many Denominations; in which Caſe you are to reduce both Numbers to one Denomination; and likewiſe your ſecond Number (if it conſiſteth at any Time of diverſe Denominations) muſt be reduced to the leaſt Name mentioned, or lower if you pleaſe, which being done, multiply the ſecond and third together, and divide by the firſt, as is directed in the 7th Rule of this Chapter.

And note, that always the Anſwer to the Queſtion is in the ſame Denomination that your ſecond Number is of, or is reduced to, as was hinted before.

Queſt. 5. If 15 Ounces of Silver be worth 3 *l.* 15 *s.* what are 86 Ounces worth at that rate?

In this Queſtion the Numbers being ordered according to the 6th Rule of this Chapter, the firſt and third Numbers are Ounces, and the ſecond Number is of diverſe Denominations, *viz.* 3 *l.* 15 *s,* which muſt be reduced to Shillings, and the Shillings multiplied by the third Number, and the Product divided by the firſt, gives you the Anſwer in Shillings, *viz.* 430 Shillings, which are reduced to 21 *l.* 10 *s.*

```
       oz.   s.   d.   oz.
    If 15    3    15   86
       20
    ------
       75
       86
    ------
      450
     600
    ------ (2|0    l.  s.
  15)6450  (43|0  (21 10
     ...
      60          4
    ------      ----
      45          3
      (0)       (10) s.
```

In reſolving the laſt Queſtion the Work would have been the ſame, if you had reduced your ſecond Number into Pence, for then the Anſwer would have been 5160 Pence, equal to 21 *l.* 10 *s.* or if you had reduced the ſecond Number into Farthings, the Quotient or Anſwer would have been 20640 Farthings, equal to the ſame, as you may prove at your Leiſure.

Queſt. 6. If 8 *l.* of Pepper coſt 4 *s.* 8 *d.* what will 7 *C.* 3 *qrs.* 14 *l.* coſt?

In this Queſtion the firſt Number is 8 *l.* and the third is 7 *C.* 3 *qrs.* 14 *l.* which muſt be reduced to the ſame Denomination with the firſt, *viz.* into Pounds, and the ſecond Number muſt be reduced into Pence; then multiply and divide according to the 7th Rule foregoing, and you will find the Anſwer to be 6174 Pence, which is reduced into 25 *l.* 14 *s.* 6 *d.*

```
   l.     s.  d.            C.  qrs.   l.
If 8 coſt 4   8 what will   7    3     14 coſt?
         12                      4
        ----                   -----
         56                     31
                                28
                              ------
                               152
                                63
                             -------
                               882
                                56 ſecond Number.
                            --------
                              5292
                             4410
                             ------   12)       2|0    l.    s.   d.
                         8)  49322  (6174     (41|0  (25    14    6
                              ....    ...       ...
                             48       60         4
                          ------------------------------
                             18       17        11
                              8       12        10
                          -------   -------   --------
                             59       54       (14) s.
                             56       48
                          -------   -------
                             32      (6) d.
                             32
                          -------      l.   s.   d.
                             (0) Facit 25   14   6
```

Queſt. 7. If 3 *C.* 1 *qr.* 14 *l.* of Raiſins coſt 9 *l.* 9 what will 6 *C.* 3 *qrs* 20 *l.* of the ſame coſt?

Here the firſt and third Numbers each conſiſt of dive Denominations, but muſt be brought both into one Denomination, &c. as you ſee in the Operation that followeth, the Anſwer is 388 *s.* which is reduced into 19 *l.* 8 *s.*

```
    C. qr.  l.      l.   s.          C.  qr.. l.
If  3   1   14 coſt 9    9 what will 6   3    20 coſt
    4               20               4
  -----           -----             -----
    13              189              27
    28                                2
  -----                             -----
  1 8                                216
  27                                 56
  -----                             -----
  378 Pounds                         776 Pounds
                                     189 Second Number
                                    -----
                                     6984
                                    6208
                                   776
                                   -----      2|0        l.   s.
                            378)   146664    (38|8      (19   8
                                                 2
                                    1134     -----
                                   -----       18
                                     3326      18
                                     3024     ----
                                   -----      (8)
                                     3024
                  l.  s.             3204
         Facit   19   8             -----
                                     (0)
```

Queſt. 8. If in 4 Weeks I ſpend 13 *s.* 4 *d.* how long will 53 *l.* 6 *s.* laſt me at that rate?

Anſwer 2238 Days, equal to 6 Years, 48 Days, See the Work.

```
   s. d.          w.          l.  s.
If 3  4 require   4 what will 53  6 cost?
  12              7           20
 ---             ---         ----
  30             28 Days     1066
 13                            12
 ---                         ----
 400                         2132
                            1066
                            -----
                            12792 Pence
                               28 Second Number
                           ------
                           102336
                          25584
                          ------- 395
                 16|0) 35817|6 (2238 (6 Years
                        ...     2190
                        32      ----
                       ---- Rem. (48) Days
                        38
                        32
                       ----
                        61         ye      days
                        48   Facit 6       48 96/100
                       ----
                        137
                        128
                       ----
              Remain (96)
```

Quest. 9. Suppose the yearly Rent of a House, a yearly ersion or Wages, be 73 *l.* I desire to know how much is *per* Day?

Here you are to bring the Year into Days, and say, if 65 Days require 73 *l.* what will one Day require?

Now when you come to multiply 73 by 1, the Product the same; for one neither multiplieth nor divideth, and 3 cannot be divided by 363, because the Divisor is bigger han the Dividend; wherefore bring the 73 *l.* into Shillngs, and they make 1460, which divide by the first

Number 365, and the Quote is 4 Shillings for the Anſwer: As you ſee in the Work:

Days	*l.*	Day
If 365	73	1
	20	

365) 1460 (4 *s.*
1460
——— *Facit* 4 *s. per* Day.
(0)

Queſt. 10. A Merchant bought 14 Pieces of Broad-Cloth, each Piece containing 28 Yards, for which he gave after the Rate of 13 *s.* 6 *d.* ½ *per* Yard; now I deſire to know how much he gave for the 14 Pieces at that Rate?

Firſt find out how many Yards are in the 14 Pieces, which you will do if you multiply the 14 Pieces by 28 (the Number of Yards in a Piece) and it makes 392; then ſay, If a Yard coſt 13 *s.* 6 *d.* ½, what will 392 Yards coſt Work as followeth, and the Anſwer you will find to be 127400 Half-pence, which reduced, make 265 *l.* 8 *s.* 4 *d.* For after you have multiplied your ſecond and third Numbers together, the Product is 127400, which, (according to the ſeventh Rule) ſhould be divided by the firſt Number; but the firſt Number is 1, which neither multiplieth nor divideth, and therefore the Quotient or 4th Number is the ſame with the Product of the Second and Third; which is in Half-pence, becauſe the Second Number was ſo reduced. See the Work as followeth.

```
                    28
                    14
                   ----
                   112
                   28
                   ----
                   392 Yards in the 14 Pieces
     Yds.    s. d.           Yds.
If  1 coſt  13 6½, what will 392 coſt ?
            12                325
           ----              -----
            32               1960
            13                784
           ----             1176
           162              --------2|0
             2        24) 127400 (530|8 (265 l.
           ----           ....    ...
half-pennies 325           120     4
                          -----   ----
                            74     13
                            72     12
                          -----   ----
                            200    10
                            192    10
                          -----   ----
                                  (8) Shillings
      l.   s.   d.      Rem. (8) Half-pence, or 4 d.
Facit 265  8    4
```

Queſt. 11. A Draper bought 420 Yards of Broad-cloth and gave for it after the Rate of 14 *s.* 10 *d.* ½ per Ell *Engliſh*, now I demand how much he paid for the Whole after, that Rate?

Bring your Ells into Quarters, and your given Yards into Quarters, the Ell is 5 Quarters, and in 420 Yards, are 1680 Quarters; then ſay, if 5 Quarters coſt 14 *s.* 10 *d.* ¾ (or 715 Farthings) what will 1680 Quarters coſt? *Facit* 250 *l.* 5 *s.* See the Operation.

Ells Yards
1 420
5 20

5 1680

qrs. *s.* *d.*
If 5 10 10 $\frac{3}{4}$
12

28
15

178 *d.*
4

715 qrs.

1680
715

8400
1680
11760

96|0
5) 1201200 (24024|0 (250 *l.*

10 192

20 482
20 480

12 *rem.* (240) *qrs.* or 5 *s.*
10

20
20

(0)

l. *s.* *d.*
Facit 250 5 0

Queſt. 12. A Draper bought of a Merchant 50 Piece of Kerſey, each Piece containing 34 Ells *Engliſh*, (the El *Flemiſh* being three Quarters of a Yard) to pay after th Rate of 8 *s.* 4 *d. per* Ell *Flemiſh*, I demand how much the 50 Pieces coſt him at that Rate?

Firſt find out how many Ells *Flemiſh* are in the 5 Pieces, by multiplying 50 by 34, the Product is 1700 which bring into Quarters by 3, it makes 5100 Quarters then proceed as in the laſt Queſtion, and the Anſwer yo will find to be 102000 Pence, or 425 *l.* See the Operation as followeth.

qrs. s. d.
It 5 8 4 5100 50
12 100 34
——— ——— d. ———
100 d. 5) 5 10000 (10200 200
.... 150
5 ———
——— 1700 Ells Fl.
10 3
10 ———
——— 5100
(0) (2|0)
12) 102000 (850|2 (425 l.
.. .
96 8
——— ———
60 5
60 4
——— ———
(0) 10
10
———
Facit 425 *l.* (0)

Queſt. 13. A Goldſmith bought a Wedge of Gold, which weighed 14 *l.* 3 *oz.* 18 *p. w.* for the Sum of 514 *l.* 4 *s.* I demand what it ſtood him in *per* Ounce? *Anſwer*, 60 *s.* or 3 *l.*

l. *oz.* *p w.* *l.* *s.* *oz.*
If 14 3 8 514 4 1
12 20 Shillings 20
——— ——— ———
31 10284 20 *p.w.*
14 20 *p.w.*
——— ———2|0)
171 (oz. 5428) 205680 (6|0 (3 *l.*
20 .. .
——— 205680 ———
3428 *p. w.* ——— (0) *Facit* 60 *s.* or 3 *l.*

Queſt. 14. A Grocer bought 4 Hogſheads of Sugar, each weighing near 6 *C.* 2 *qrs.* 14 *l.* which coſt him 2 *l.* 8 *s.* 6 *d. per C.* I demand the Value of the 4 Hdds at that Rate?

Firſt I find the Weight of the 4 Hhds, which you may do by reducing the Weight of one of them into Pounds, and multiply them by 4 (the Number of Hhds) and they make 2968 *l.* Then ſay, If 1 *C.* or 112 *l.* coſt 2 *l.* 8 *s.* 6 *d.* what will 2968 *l.* coſt? *Facit* 64 *l.* 5 *s.* 3 *d.* As by the Operation.

```
                                  C.    qrs.    l.
                                  6      2      14
                                  4
                                ----
                                 26
                                  2
                                ----
   l.    l.   s.   d.     l.     212
If 112   2    8    6     2968     53
         20               582   ----
        ----            ------   742 l. in 1 hhd.
         48               5936    4 hogſheaps.
         12              23744  --------
        ----             14840   2968 l. in 4 hhds.
        102             ------      12)       2|0)
         48   112)     1727376 (15413)     128|5 (64 l.
        ----            .....      ...       ..
        582               112       12       12
                         ----      ----     ----
                          607       34        8
                          560       24        8
                         ----      ----     ----
                          472      102      (5) Shillings.
                          448       96
                         ----      ----
                          257       63
                          224       60
                         ----      ----
                          336      (3) Pence.
                          336
                         ----           l.    s.    d.
                          (0)   Facit   64    5     3
```

Queſt. 15. A Draper bought of a Merchant 8 Packs of Cloth, each cantaining 4 Parcels, and each Parcel 10 Pieces, and each Piece 26 Yards, and gave after the Rate of 4 *l.* 16 *s.* for 6 Yards, now I deſire to know how much he gave for the Whole? Anſwer 6656 *l.*

Firſt find out how many Yards there were in the 8 Packs, and by the ſollowing Work you will find there are 8320 Yards; then ſay, it 6 Yards coſt 4 *l.* 16 *s.* what will 8320 Yards coſt, &c.

```
                                        8 Packs.
                                        4
                                     -------
                                       32 Parcels
                                       10
                                     -------
                                      320 Pieces
                                       26
                                     -------
Yds.  l.   s.   Yds.                  1920
 6    4    16   8320                  640
      20          96                 -------
    -----     -------                 8320 Yards.
      96       49920
              74880
             -------
      6) 798720 (13312|0 (6656 l.
         .....     ..
         6         12
        ---       ---
         19        13
         18        12
        ---       ---
         18        11
         18        10
        ---       ---
          7        12
          6        12
        ---       ---
         12        (0)
         12
Facit 656 l. ---
         (0)
```

By this time the Learner is, as I ſuppoſe well exerciſed i the Prectick and Theorick of the *Rule of Three Direct*; bu at his Leaſure he may look over the following Queſtions, whoſe Anſwers were given, but the Operation purpoſely omitted as a Touchſtone for the Learner, thereby to try his Ability in what hath been deliver'd in the former Rules.

Queſt. 16. If 24 *l.* of Raiſins coſt 6 *s.* 6. *d.* what will 38 Frails coſt, each weighing neat 3 *qrs.* 18 *l.* *Anſ.* 24 *l.* 17 *s.* 5 *d.*

Queſt. 17. If an Ounce of Silver be worth 5 Shillings, what is the Price of 14 Ingots, each Ingot weighing 7 *l.* 5 *oz.* 10 *p. w.* *Anſwer* 313 *l.* 5 *s.*

Queſt. 18. If Piece a ot Cloth coſt 10 *l.* 16 *s.* 8 *d.* I demand how many Ells *Engl.* there are in the ſame, which Ell at that Rate is worth 8 *s.* 4 *d.* *Anſwer*, 26 Ells *Engliſh*.

Queſt. 19. A Factor bought 84 Pieces of Stuffs, which coſt him in all 537 *l.* 12 *s.* at 5 *s.* 4 *d.* *per* Yard, I demand how many Yards there were in all, and how many Ells *Engliſh* were contained in a Piece of the ſame? *Anſwer*, 2016 Yards in all, and 19 $\frac{1}{2}$ Ells of *Engliſh per* Piece.

Queſt. 20. A Draper bought 242 Yards of Broad-cloth, which coſt him in all 254 *l.* 10 *s.* for 86 Yards, of which he gave after the Rate of 11 *s.* 4 *d.* *per* Yard. I demand how much he gave *per* Yard for the Remainder? *Anſwer* 20 *s.* 9 *d.* $\frac{46}{151}$ *per* Yard.

Queſt. 21. A Factor bought a certain Quantity of Serge and Shalloon, which together coſt him 126 *l.* 14. *s.* 10 *d.* the Quantity of Serge he bought was 48 Yards, at 4 *s.* 4 *d. per* Yard; and for every two Yards of Serge he had 5 Yards of Shalloon; I demand how many Yards of Shalloon he had, and how much the Shalloon coſt him *per* Yard? *Anſw.* 120 Yards of Shalloon at 1 *l.* 15 *s.* 5 *d.* $\frac{58}{120}$ *per* yd.

Queſt. 22. An Oilman bought three Tuns of Oil, which coſt him 151 *l.* 14 *s.* and ſo it chanced that it leaked out 85 Gallons; but he is minded to ſell it again, ſo that he may be no Loſer by it; I demand how he muſt ſell it *per* Gallon? *Anſwer*, at 4 *s.* 6 *d.* $\frac{174}{601}$ *d. per* Gallon.

Queſt. 23. Bought 9 Packs of Cloth, each Pack containing 12 Cloths, which at 8 *s.* 4 *d.* Ell *Flemiſh*, coſt 1080 *l.* I demand how many Yards there were in each Cloth? *Anſwer* 27 Yards in each Cloth.

Queſt. 24. A Gentleman hath 539 *l. per Ann.* and his Expences are, one Day with another 18 *s.* 10 *d.* 3 *qrs.* I deſire to know how much he layeth up at the Year's End? *Anſwer* 191 *l.* 3 *s.* 8 *d.* 1 *qr.*

Queſt. 25. A Gentleman expendeth daily one Day with another 27 *s.* 10 *d.*$\frac{1}{2}$, and at the Year's End layeth up 340 *l.* I demand how much is his yearly Income? *Anſwer* 848 *l.* 14 *s.* 4 *d.* $\frac{1}{2}$.

Queſt. 26. If I ſell 24 Yards for 10 *l.* 10 *s.* how many Ells *Flemiſh* ſhall I ſell for 283 *l.* 17 *s.* 6 *d.* at that Rate *Anſwer* 504$\frac{2}{3}$ Ells *Flemiſh.*

Queſt. 27. If 100 *l.* in 12 Months, gain 6 *l.* Intereſt, how much will 75 *l.* gain in the ſame Time, and at the ſame Rate? *Anſwer* 4 *l.* 10 *s.*

Queſt. 28. If 100 *l.* in 12 Months gain 6 *l.* Intereſt, how much will it gain in 7 Months at that Rate? *Anſwer* 3 *l.* 10 *s.*

Queſt. 29. A certain Uſurer put out 73 *l.* for 12 Months, and received Principal and Intereſt 81 *l.* I demand what Rate *per Cent.* he received Intereſt? *Anſwer* 8 *l. per Cent.*

Queſt. 30. A Grocer bought 2 Cheſts of Sugar. the one weigh'd near 18 *C.* 3 *qrs.* 14 *l.* at 2 *l.* 6 *s.* 8 *d. per C.* the other weigh'd near 18 *C.* 1 *qr.* at 4 *d.* $\frac{1}{2}$ *per l.* which he mingled together; now I deſire to know how much a *C. wt.* of this Mixture is worth? *Anſ.* 2 *l.* 4 *s.* 2$\frac{5067}{5587}$ *qrs.*

Queſt. 31. Two Men, *viz.* *A* and *B* departed both from one Place, the one goes *Eaſt*, and the other *Weſt*; the one travelleth 4 Miles a Day, and the other 5 Miles a Day, how far are they diſtant the 9th Day after their Departure? *Anſwer* 81 Miles.

Queſt. 32. *A* flying every Day 40 Miles, is purſued the fourth Day after by *B*, poſting 50 Miles a Day; now the Queſtion is, in how many Days, and after how many Miles Travel, will *A* be overtaken?

Anſw. *B* overtakes him 32 Days, when they have travelled 600 Miles. See *More*'s Arithm. cap. 8. *qr.* 7.

.11. The general Effect of the Rule of Three Direct, is contained in the Definition of the ſame, that is, to find a fourth Number in Proportion, conſiſting of two equal Reaſons; as hath been fully ſhewn in all the foregoing Examples.

The ſecond Effect is, by the Price or Value of one Thing, to find the Price and Value of many Things of like Kind.

The third Effect is, by the Price or Value of many Things, to find the Price of one; or by the Price of many Things, (the ſaid Price being one) to find the Price of many Things of like Kind.

The 4th Effect is, by the Price or Value of many Things, to find the Price or Value of many Things of like Kind.

The 5th Effect is thereby to reduce any Number of Monies, Weights, Meaſures, the one Sort into the other, as in the Rules of Reduction contained in the 8th Chapter foregoing. Examples of its various Effect have been already anſwered.

12. The Rule of Three Direct, is thus proved, viz. Multiply the firſt Number by the 4th, [*The Proof of the Rule of Three Direct.*] and note the Product; then multiply the 2d Number by the 3d, and if this Product is equal to the Product of the 1ſt and 4th, then the Work is rightly performed, otherwiſe it is erroneous.

So the firſt Queſtion of the Chapter (whoſe Anſwer or 4th Number we found to be 18 *s.*) is thus proved, *viz.* the firſt Number is 4, which multiplied by 18 (the 4th) produceth 72, and the 2d and 3d Numbers are 13 and 16, which multiplied together produceth 72, equal to the Product of the 1ſt and 4th, and therefore I conclude the Work to be rightly performed.

Always obſerving, That if any Thing remain after you have divided the Product of the 2d and 3d Numbers by the firſt, ſuch Remainder in proving the ſame, muſt be added to the Product of the 1ſt and 4th Numbers, whoſe Sum will be equal to the Product of the ſecond and third, the ſecond Number being of the ſame Denomination with the fourth, and the firſt of the ſame Denomination with the third.

So the fourth Queſtion of this Chapter being again repeated, *viz.* If 142 *l.* of Tobacco coſt 27 *s.* what will 478 *l.* coſt at that Rate? The Anſwer, (or fourth Number) was 46 *l.* 1 *s.* 10 *d.* 1 *qr.* $\frac{1}{14}$, which is thus proved; *viz* bring the 4th Number into Farthings, and it makes 44294, which multiplied by the firſt Number 14, produceth 619488 (the ſecond which remaineth being added thereto:) then (becauſe I reduce my fourth Number into Farthings (I reduce my ſecond,(*viz.* 27 *s.*) into Farthings, and they are 1296, which multiplied by the 3d Number 478, their Product is 617488, equal to the Product of the firſt and fourth Numbers. Whereſore I conclude the Operation to be true. This is an infallible Way to prove the Rule of Three Direct, and it is reduced from the 12th Section of the 9th Chapter of this Book.

And thus much for this ineſtimable Rule of Three Direct, the Demonſtration of which may be ſeen in *Rerſey*'s Appendix to *Wingate*'s Arithm. and in the 7th Chapter of *Oughtred's Clavis Mathemetica.*

CHAP. XI.

The Single Rule of Three Inverſe.

1. THE Golden Rule, or Rule of Three Inverſe, is when there are 3 Numbers, given to find a 4th in ſuch Proportion to the 3 given Numbers, ſo as the 4th proceeds from the 2d according to the ſame Rate, Reaſon or Proportion, that the firſt proceeds from the third, or the Proportion is,

As the 5th Number is in Proportion to the 2d, ſo is the 1ſt to the 4th, See *Alſtead Math.* l. 2. c. 14.

So if the 3 Numbers given were 8, 12, and 16, and it were required to find a fourth Number in an inverted Proportion to theſe, I ſay, that as 16 (the third Number) is the Double of the firſt Term or Number (8) ſo muſt 12, the ſecond Number, by the double of the fourth; ſo will you find the fourth Term or Number to be 6. (And as in the Rule of Three Direct) you multiply the ſecond and third together, and divide their Product for a fourth proportional Number.

2. In the Rule of Three Inverſe, you muſt multiply the ſecond Term by the firſt, or firſt, Term by ſecond, and divide the Product thereof by the firſt Term, ſo the Quotient will give you the 4th Term ſought in an inverted Proportion. The ſame Order being obſerved in this Rule, as in the Rule of Three Direct, for placing and diſpoſing of the

given Numbers, and after your Number are placed in order, that you may know whether your Queſtion be to be reſolved by the Rule Direct or Inverſe, obſerve the general Rule ſollowing.

3. When your Queſtion is ſtated, and your Numbers orderly diſpoſed, Conſider in the firſt Place, whether the fourth Term or Number ſought, ought to be more or leſs than the ſecond Term; which you may eaſily do: And if it is required to be more or greater then the 2d Term, then the leſſer Extream muſt be your Diviſor; but if it requires leſs, then the higheſt Extream muſt be your Diviſor; in this Caſe, the 1ſt and 3d Numbers are called Extreams (in reſpect of the ſecond) and having ſound out your Diviſor, you may know whether your Queſtion belong to the Rule Direct or Inverſe; for if the 3d Term be your Diviſor, then it is Inverſe; but if the 1ſt Term be your Diviſor, then it is a direct Rule. As in the ſollowing Queſtions.

Queſt. 1. If 8 Labourers can do a certain Piece of Work in 12 Days, in how many Days will 16 Labourers do the ſame? *Anſwer*, in 6 Days.

Having placed the Numbers according to the 6th Rule of the 10th Chapter, I conſider, that if 8 Men can finiſh the Work in 12 Days, 16 Men will do it in leſſor (or fewer Days) than 12, therefore the biggeſt Extream muſt be the Diviſor, which is 16, and therefore it is the Rule of Three Inverſe; wherefore I multiply the 1ſt and 2d Numbers together, *viz.* 8 by 12, and their Product is 96, which divided by 16, quotes 6 Days for the Anſwer; and in ſo many Days will 16 Labourers perform a Piece of Work, when 8 Men can do it in 12 Days.

lab.	Days	lab.
1	12	16
	8	

16) 96 (6 Days
96
(0)
Facit 6 Days

Queſt. 2. If when the Meaſure, *viz.* (a Peck) of Wheat coſt 2 *s.* the Penny-loaf weighed (according to the Stanard Statute or Law of *England*) 8 Ounces, I demand how much it will weigh when the Peck is worth 1 *s.* 6 *d.* according to the ſame Rate or Proportion? *Anſwer* 10 *oz.* 13 *p. w.* 8 *gr.*

Having placed and reduced the given Numbers according to the 6th and 9th Rules of the 10th Chapter, I conſider that at 1 s. 6 *d. per* Peck, the Penny-loaf will weigh more than at 2 *s. per* Peck: for as the Price increaſeth, ſo the Weight increaſeth; and as the Price increaſeth, ſo the Weight diminiſhes; wherefore becauſe the firſt Term requires more than the ſecond, the leſſer Extream muſt be the Diviſor, *viz.* 1 *s.* 6 *d.* or 18 *d.* and having finiſhed the Work, I find the Anſwer to be 10 *oz.* 13 *p. w.* 1 *gr.* and ſo much will the Penny-loaf weigh when the Peck of Wheat is worth 1 *s.* 6. *d.* according to the given Rate of 8 Ounces, when the Peck is worth two Shillings. The Work is plain in the following Operation.

```
         d.       oz.      gr.
      If 24       8        18
         8
      ———— oz. p. w. gr.
   18) 192 (10 13  8 Anſw.
        .
       18
      ————
       12
       20
      ———— p. w.
       240 ( 13
        .
       18
      ————
       60
       54
      ————
       (6)
       24
      —————
       144 (8 gr.
       144
      ————
       (0)
```

Queſt. 3. How many Pieces of Money or Merchandize at 20 *s. per* Piece, are to be given or received for 240 Pieces, the Value or Price of every Piece being 12 Shillings? Anſwer 144 Pieces. For if 12 *s.* required 240 Pieces, then 20 *s.* will require leſs; therefore the bigger Extream muſt be the Diviſor, which is the the third Number, *&c.* See the Work as in the Margent.

s. *pes.* *s.*
If 12 240 20
12
480
240
2|0) 288|0 (144 *pes.* *at*
..
20 *s. per* pe
2
8
8
8
8
(0)

Queſt. 4. How many Yards of 3 Quarters broad are required to double, or be equal in Meaſure to 30 Yards, that are 5 Quarters broad? *Anſwer* 50 Yards. For ſay, if 5 Quarters will require 30 Yards long, what Length will 3 Quarters broad require? Here I conſider that 3 Quarters broad will require more Yards than 30; for the narrower the Cloth is, the more in length will go to make equal Meaſure with a broader Piece.

qrs. *long* *qrs.*
3 30 5
5
3) 250 (50 *yds*
.
15
(0)

Queſt. 5. At the Requeſt of a Friend, I lent him 300 *l.* for 12 Months; promiſing to do me the like Courteſy at my Neceſſity; but when I came to requeſt it of him, he could let me have but 150 *l.* now I deſire to know how long I may keep this Money to my plenty Satisfaction for my former Kindneſs to my Friend; *Anſwer* 16 Months, I ſay, If 200 *l.* will require more Time than 12 Months, therefore the leſſer Extream, viz. 150) muſt be the Diviſor; multiply and divide, and you will find the fourth inverted proportional to be 16, and ſo many Months I ought to keep the 350 *l.* for Satisfaction.

Queſt. 6. If for 24 *s.* I have 1200 *l.* Weight carried 36 Miles, how many Miles ſhall 1800 *l.* be carried for the ſame? *Anſwer* 24 Miles.

Queſt. 7. If for 24 *s.* I have 1200 *l. wt.* carried 36 Miles; how many *l. wt.* ſhall I have carried 24 Miles for the ſame Money? *Anſwer* 1800 *l.* weight.

Queſt 8. If 100 Workmen in 12 Days finiſh a Piece of Work or Service, how many Workmen are ſufficient to do the ſame in 3 Days? *Anſwer* 400 Workmen.

Queſt. 9. A Colonel is beſieged in a Town, in which are 1000 Soldiers, with Proviſion of Victuals only for three Months; the Queſtion is, How many of his Soldiers muſt he diſmiſs, that his Victuals may laſt the remaining Soldiers 6 Months? *Anſwer* 500 he muſt keep, and diſmiſs as many.

Queſt. 10. If 20 *l.* worth of Wine is ſufficient for the Ordinary of 100 Men, when the Tun is ſolid for 20 *l* how many Men will the ſame 20 *l.* worth ſuffice when the Tun is worth 25 *l.* *Anſwer* 125 Men.

Queſt. 11. How much Pluſh is ſufficient for the Cloak, which hath in it 4 Yards of 7 Quarters wide, when the Pluſh is but 3 Quarters wide? *Anſwer* 9 $\frac{1}{2}$ Yards of Pluſh.

Queſt. 12, How many Yards of Canvas that is Ell wide will be ſufficient to line 20 Yards of Say, that is 3 Quarters wide? *Anſwer* 12 Yards.

Queſt. 13. How many Yards of Matting that is 2 Foot wide, will cover a Floor that is 24 Foot long, and 20 Foot broad? *Anſwer* 140 Foot.

Queſt. 14. A Regiment of Soldiers, conſiſteth of 1000, and to have new Coats, and each Coat to contain two Yards two Quarters of Cloth that is 5 Quarters wide, and they are to be lined with Shalloon that is 2 Quarters wide, I demand how many Yards of Shalloon will line them? *Anſwer* 16666 $\frac{1}{2}$ Quarters, or 4166 $\frac{1}{4}$ Yards.

Queſt. 15. A Meſſenger makes a Journey in 24 Days, when the Day is 12 Hours long: I deſire to know in how many Days he will go the ſame when the Day is 16 Hours long; *Anſwer* in 18 Days.

Queſt. 16. I borrowed of my Friend 60 *l.* for 8 Months, and he hath Occaſion another Time to borrow of me for 12 Months. I deſire to know how much I muſt lend to make good his former Kindneſs to me? *Anſwer*, 42 *l.* 13 *s.* 4 *d.*

4. The general Effect of the Rule of Three Inverſe, is contained in the Definition of the ſame, that is, to find a fourth Term in a Reciprocal Proportion inverted to the Proportion given.

The 2d Effect is, by two Pieces, or Value of two ſeveral Pieces of Money and Merchandize known, to find how many Pieces of the one Price is to be given for ſo many of the other. And ſo to reduce and exchange one Sort of Money or Merchandize into another. Or elſe to find the Price unknown of any Piece given to exchange in reciprocal Proportion.

The 3d Effect is, by two different Prices of a Meaſure of Wheat bought or ſold, and the Weight of a Loaf of Bread, made anſwerable to one of the Prices of the Meaſure given, to find out the Weight of the ſame Loaf anſwerable to the other Price of the ſaid Meaſure given.

Or elſe, by the two ſeveral Weights of the ſame priced Loaf, and the Price of the Meaſure of Wheat anſwerable to one of thoſe Weights given, to find out the other Price of the Meaſure anſwerable to the other Weight of the ſame Loaf.

The 4th Effect is, by two Lengths, and one Breadth of two Rectangular Planes known, to find out another Breadth unknown. Or, by 2 Breadths, and one Length given, to find out another Length unknown in an inverted Proportion.

The 5th Effect is, by double Time, and a capital Sum of Money borrowed or lent, to find out another capital Sum anſwerable to one of the given Times; or otherwiſe, by two capital Sums, and a Time anſwerable to one of them given, to find out a Time anſwerable to the other capital Sum in reciprocal Reaſon.

The 6th Effect is, by two different Weights of Carriage, and the Diſtance of the Place in Miles or Leagues given, to find another Diſtance in Miles anſwerable to the ſame Price of Payment. Or otherwiſe, by two Diſtance in Miles, and the Weight anſwerable to one of the Diſtance in Miles, carried for a certain Price) to find out the Weight anſwerable to the other Diſtance for the ſame Price.

The 7th Effect is, by double Workmen, and the Time anſwerable to one of the Numbers of Workman given, to find out the Time anſwerable to the other Number of Workmen, in the Performance of any Work or Service. Or contrariwiſe, by double Time, and the Workman anſwerable to one of thoſe Times given, to find out the Number of Workman anſwerable to the other Time, in the Performance of any Work or Service.

Alſo by a double Price of Proviſion, and the Number of Men, or other Creatures, nouriſhed for a certain Time anſwerable to one of the Prices of Proviſions given, to find out another Number of Men or other Creatures anſwerable to the other Price of the Proviſion for the ſame Time. Or contrariwiſe, by two Numbers of Men, or other Creatures nouriſhed, and one Price of Proviſion anſwerable to one of the Numbers of Creatures given, to find out the other Price of the ſame Proviſion anſwerable to the other Number of Creatures, both being ſuppoſed to be nouriſhed for the ſame, *&c.*

To prove the Operation of the Rule of Three Inverſe, multiply the 3d and 4th Terms together, and note their Product; and multiply the 1ſt and 2d together, and if their Product is equal to the Product of the 3d and 4th, then is the Work truly wrought, but if it falleth out otherwiſe, then it is erroneous.

As in the firſt Queſtion of this Chapter 16 (the 3d Number) being multiplied by 6 (the 4th Number) the Product is 96, and the Product of 8, (the firſt Number) multiplied by 12, (the 2d Number) is 96, equal to the firſt Product, which proves the Work to be right.

And note. That if in Diviſion any Thing remain, ſuch Remainder muſt be added to the Product of the third and fourth Terms, and if the Sum be equal to the Product of the firſt and ſecond (the Homogeneal Terms being of one Denomination) the Work is right.

CAAP. XII.

The Double Rule of Three Direct.

WE have already delivered the Rule of ſingle Proportion, and we come now to lay down the Rules of Plural Proportion.

1. Plural Proportion is, when more Operations in the Rule of Three than one are required before a Solution can be given to the Queſtion propounded. Therefore in Queſtions that require Plurality in Proportion, there are always given more then three Numbers.

2. When there are given five Numbers, and a ſixth is required in Proportion thereunto, then the ſixth Proportion is ſaid to be found out by the Double Rule of Three, as in the Queſtion following, *viz.*

If 100 *l.* in 12 Months gain 6 *l.* Intereſt, how much will 75 *l.* gain in 9 Months?

3. Queſtions in the Double Rule of Three, may be reſolved either by 2 Single Rules of Three, or by 1 Single Rule of Three, compounded of the Five given Numbers.

4. The Double Rule of Three, is either Direct or elſe Inverſe.

5. The Double Rule of Three Direct is, when unto 5 given Numbers, a 6th proportional may be found out by two ſingle Rule of Three Direct.

6. The five given Numbers in the Double Rule of Three Direct conſiſteth of two Parts, *viz.* 1. A Suppoſition, and 2dly, of a Demand; the Suppoſition is contained in the three firſt of the five given Numbers, and the Demand lies in the two laſt; as in the Example of the Second Rule of this Chapter, *viz.* If 100 *l.* in 12 Months gain 6 *l.* Intereſt what will 75 *l.* gain in 9 Months? Here the Suppoſition is expreſſed in 100, 12, and 6, for it is ſaid if 100 *l.* in 12 Months gain 6 *l.* Intereſt: And the Demand lieth in 75 and 9, for it is demanded, How much 75 *l.* will gain in 9 Months.

7. When your Queſtion is ſtated, the next Thing will be to diſpoſe of the given Numbers in due Order and Place as a Preparative for Reſolution: Which that you may do; Firſt, Obſerve which of the given Numbers in the Suppoſition is of the ſame Denominatian with the Number required, for that muſt be the 2d Number (in the firſt Operation) of the Single Ruleof Three, and one of the other Numbers in the Suppoſition (it matters not which) muſt be the firſt Number, and that Number in the Demand, which is of the ſame Denomination with the firſt, muſt be the third Number; which three Numbers being thus

placed, will make one perfect Queſtion in the Single Rule of Three, as in the formentioned Example: Firſt, I conſider, that the Number required in the Queſtion, is in the Intereſt or Gain of 75 *l.* therefore that Number in the Suppoſition which hath the ſame Name, *viz.* 6 *l.* which is the Intereſt or Gain of 100 *l.* muſt be the ſecond Number in the firſt Operation, and either 100 and 12, (it matters not which) muſt be the firſt Number; but I will take a 100; and then for the third Number, I put that Number in the Demand, which hath the ſame Denomination with 100, which is 75; for they both ſignify Pounds Principal, and then the Numbers will ſtand as you ſee in the Margent.

100	6	75

But if I had for the firſt Number put the other Number in the Suppoſition, *viz.* 12. which ſignifies 12 Months, then the third Number muſt have been 9, which is the Number in the Demand which hath the ſame Denomination with the firſt, *viz.* 9 Months, and they will ſtand as in the Margent.

100	6	9

There yet remain two Numbers to be diſpoſed of, and thoſe are one in the Suppoſition, and another in the Demand; that which is of the Suppoſition, I place under the firſt of the three Numbers; and the other which is the Demand, I place under the third Number; and then two of the Terms in the Suppoſition will ſtand (one over the other) in the firſt Place, and the two Terms in the Demand will ſtand (one over the other) in the third Place, as in the Margent.

190	6	75.
12		9

Or this,

12	6	9
100		75

8. Having diſpoſed or ordered the given Numbers, according to the laſt Rule, we may proceed to a Roſolution; and firſt I work with the 3 uppermoſt Numbers, which according to the firſt Diſpoſition, are 100, 6, and 75; which is as much as to ſay, If 100 *l.* requires 6 *l.* Intereſt, how much will 75 Pounds require? which by the 3d Rule of the 11th Chap. I find to be Direct; and by the 7th and 8th Rule of the 10th Chapter, I find the 4th proportional Number to be 4 *l.* 10 *s.* ſo that by the foregoing ſingle Queſtion I have diſcoverd how muſt Intereſt 75 *l.* will gain in 12 Months; the Operation whereof followeth on the left Hand under the Letter A, and having

diſcovered how much it will gain in 12 Months, we may by another Queſtion eaſily diſcover how much it will gain in 9 Months; for this 4th Number (thus found) I put in the middle between the loweſt Numbers of the 5, after they are placed according to the 7th Rule of this Chapter; and then it will be a 2d Number, in another Queſtion in the Rule of Three. The Number being $\overset{m.}{12}\ \ \overset{l.}{4}\ \ \overset{s.}{10}\ \ \overset{m.}{9}$ the firſt and third Numbers being of one Denomination, *viz.* both Months. and may be thus expreſſed; it 12 Months require 4 *l.* 10 *s.* Intereſt, what will 9 Months require? And by the 3d Rule of the 11th Chapter, I find it to be the Direct Rule, and by working according to the Directions laid down in the 7th, 8th, and 9th Rules of the 10th Chapter, I find the fourth proportional Number to laſt ſingle Queſtion, to be 3 *l.* 7 *s.* 6 *d.* which is the ſixth proportional Number to the 5 given Numbers, and is the Anſwer to the general Queſtion. The Work of the laſt ſingle Queſtion is expreſſed on the right Side of the Page under the Letter B, as followeth.

```
                     100
   A                  12
        If 100    6   75
            75
           ----
            30
            40
           ----
   1|00)  4|50  (4   10
           .
            4
           ----
   Rem.   (50)
   Mult.   20
           ----
   1|00)  10|00 (10 s.

                  l.  s.
            Facit 4   10
```

```
——6——75
     9            B
   Then ſay,
         m.  l.  s.  m.
      If 12  4   10  9
             20
           ------
             90 Shillings
             12
           ------
            180
             90
           ------
           1080  Pence
              9
————————12)  2|0     l. s. d.
12)  9720(810  (67  (3 7 6
     ...    .
     99     72————
     ——     —— 7 s.
     12     90
     12     84
     ————————
     (0)    (6) d.
Facit 3 l. 7 s. 6 d.
```

So that by the foregoing Operation, I conclude, that if 30 *l.* in 12 Months gain 6 *l.* Intereſt, 75 *l.* will gain 3 *l.* 7 *s.* 6 *d.* in 9 Months, after the ſame Rate.

The Anſwer would have been the ſame if the 5 given Numbers had been ordered according to the ſecond Method, *viz.* as you ſee in the Margent.

12 9 9
105 75

For firſt, I ſay, if twelve Months gain 6 *l.* what will 9 Months gain? This Queſtion I find to be Direct, by the 3d Rule of the 11th Chapter, and by the 7th and 8th Rules of the 10th Chapter, I find the fourth proportional Number to theſe three to be 4 *l.* 10 *s.*

Thus have I found out what is the Intereſt 100 *l.* for 6 Months, and I am now to find the Intereſt of 75 *l.* for 6 Months; to effect which, I make this 4th Number (found as before) to be my ſecond Number in the next Queſtion, I ſay, If 100 *l.* require 4 *l.* 10 *s.* what will 75 *l.* require? This Queſtion, I find (by the ſaid 3d Rule of the 11th Chapter) to be Direct, and by the ſaid 7th, 8th, and 9th Rules of the 10th Chapter, I find the Anſwer to be as before, *viz.* 3 *l.* 7 *s.* 6 *d.*

The Operation of this Rule in the following Queſtions, are purpoſely omitted, to try the Learners Capacity.

Queſt. 3. A 2d Example in this Rule may be as followeth *viz.* A Carrier receiving 42 Shilling for the Carriage of 40 0 Weight 150 Miles, I demand how much he ought to receive for the Carriage of 7 *C.* 3 *qrs.* 4 *l.* 50 Miles at that Rate? *Anſwer* 36 *s.* 9 *d.*

Queſt. 3. A Regiment of 136 Soldiers eat up 351 Quarters of Wheat in 108 Day, I demand how many Quarter of Wheat 11232 Soldiers will eat in 56 Days at that Rate? *Anſwer* 1404 Quarters.

Queſt. 4 If 40 Acree of Graſs be moved by 8 Men in 7 Days. how many Acres ſhall be mowed by 24 Men in 28 Days? *Anſwer* 480 Acres.

Queſt. 5. If 48 Buſhels of Corn (or other Seed) yeild 576 Buſhels in a Year, how much will 240 Buſhels yeild in 6 Years at that Rate? That is to ſay, if they were ſowed 240 Buſhels every one of the 6 Years? *Anſwer* 17280 Buſhels.

Queſt. 6. If 40 Shillings is the Wages of 8 Men for Days, what will be the Wages of 32 Men for 24 Days? *Anſwer* 768 Shillings, or 38 *l.* 8 *s.*

Queſt. 7. If 14 Horſes eat 46 Buſhels of Provender in 16 Days, how many Buſhels will 20 Horſes eat in 2 Days? *Anſwer* 120 Buſhels.

Queſt. 8. If 8 Cannons in one Day ſpend 48 Barrels of Powder, I demand how many Barrels 24 Cannons will ſpend in 22 Days at rate? *Anſwer* 1728 Barrels.

Queſt. 9. If in a Family conſiſting of 7 Perſons, there are drunk out 2 Kilderkins of Beer in 12 Days, how many Kilderkins will there be drunk out in 8 Days, by another Family conſiſting of 14 Perſons? *Anſwer* 48 Gallons, or 2 Kilderkins and 12 Gallons.

Queſt. 10. An Uſurer put 75 *l.* out, to receive Intereſt for the ſame, and when it had continued 9 Months, he received for Principle and Intereſt 78 *l.* 7 *s.* 6 *d.* I demand at what Rate *per Cent. per Annum*, he received Intereſt? *Anſwer* 6 *l.* *per Cent. per Annum.*

CHAP. XIII.

The Double Rule of Three Inverſe.

THE Double Rule of Three Inverſe, is, when a Queſtion in the Double Rule of Three is reſolved by two Single Rules of Three, and one of thoſe ſingle Rules falls out to be Inverſe, or requires a fourth Number in Proportion reciprocal (for both Queſtions are never Inverſe.)

2. In all Queſtions of the Double Rule of Three (as well Inverſe as Direct) you are in the diſpoſing of the 5 given Number, to obſerve the 7th Rule of the 12th Chapter, and in reſolving of it by two ſingle Rules, obſerve to make Choice of your Numbers for the firſt and ſingle Queſtions, according to the Directions given in the 8th Rule of the ſame Chapter, and in the Example following, *viz.*

Queſt. 1. If 100 *l.* Principal in 12 Months gain 9 *l.* Intereſt what Principal will gain 3 *l.* 7 *s.* 6 *d.* in 9 Months?

This Queſtion is an Inverſion of the firſt Queſtion of the 12th Chapter, and may ſerve for a Proof thereof.

In order to a Reſolution, I diſpoſe of the 5 given Numbers, according to the 9th Rule of the laſt Chapter; and being ſo diſpoſed, they will ſtand as followeth.

```
12     100     9     l.  s.  d.
 6                   3   7   6
```

Or thus,

```
                 l.  s.  d.
 6      100      3   7   6
12               9
```

Here obſerve, That according to the 8th Rule of the 12th Chapter, the firſt Queſtion (if you take it from the 5 Numbers) as they are ordered or placed firſt (will be) if 12 Months require 100 *l.* Principal, what will 9 Months require to make the ſame Intereſt? This (according to the 3d Rule of the 12th Chapter) is Inverſe, and the Anſwer will be found (by the 2d Rule of the 11th Chapter) to be 133 *l.* 6 *s.* 8 *d.* The 2d Queſtion then will be, If 6 *l.* Intereſt require 133 *l* 6 *s.* 8 *d.* Principal; how much Principal will 3 *l.* 7 *s.* 6 *d.* require? This is a direct Rule, and the Anſwer in a direct Proportion, 75 *l.* See the Work.

First I ſay,

```
 m      l      m
12     100     9
        12
———————————        l.    s.   d.
9)   1200  (133    6    8
      ...
      9                 l.    s.   d.
———       Facit  133    6    8
     30
     27
     ———
     30
     27
     ———
     (3)
     20
9)   60 (6 s.
     54
     ———
     (6)
     12
     ———
9)   72 (8 d.
     72
     ———
     (0)
```

Then I ſay,

	l.	l.	s.	d.	l.	s.	d.
If	6	133	6	8	3	7	6
	240	20			20		
	1440 d.	2666			67		
		12			12		
		5340			140		
		2666			67		
		32000			810 d.		
		810					
		320000					
		256					

24|0

144|0) 2592000|0 (18000|4 d. or 75 l.

144 168

1152 120

1152 120

(0) (0)

So that by the foregoing Work I find, that if 6 *l.* Intereſt be gained by 100 *l.* in 12 Months, 3 *l.* 7 *s.* 6 *d.* will be gained by 75 *l.* in 9 Months.

But if the Reſolution had been found out by the Number as they are ranked in the ſecond Place, then the ſecond Queſtion in the Single Rule would have been Inverſe, and the firſt Queſtion Direct, and the Concluſion the ſame with the firſt Method, *viz.* 75 *l.*

Queſt. 2. If a Regiment conſiſting of 939 Soldiers, can eat up 351 Quarters of Wheat in 168 Days, how many Soldiers will eat up 1404 Quarters in 56 Days at that Rate? *Anſwer* 11232 Soldiers.

Queſt. 3. If 12 Students in 8 Weeks ſpend 48 *l.* I demand how many Students will ſpend 288 *l.* in 18 Weeks? *Anſwer* 32 Students.

Queſt. 4. If 48 *l.* ſerve 12 Students 8 Weeks, how many Weeks will 288 *l.* ſerve 4 Students? *Anſwer* 144 Weeks.

Queſt. 5. If when a Buſhel of Wheat coſt 3 *s.* 4 *d.* the Penny Loaf weigheth 12 Ounces, I demand the Weight of the Loaf worth 9 *d.* when the Buſhel coſt 10 *s.* *Anſwer* 36 Ounces.

Queſt. 6. If 48 Pioneers in 12 Days caſt a Trench 24 Yards long, how many Pioneers will caſt a Trench 168 Yards long in 16 Days? *Anſwer* 252 Pioneers.

Queſt. 7. If 12 *C.* weight being carried 100 Miles, coſt 5 *l.* 11 *s.* I deſire to know how many *C.* weight may be carried 150 Miles for 12 *l.* 12 *s.* at that Rate? *Anſ.* 18 *C.*

Queſt. 8. If when Wine is worth 30 *l. per* Tun, 20 *l.* worth is ſufficient for the Ordinary of 100 Men, how many Men will 4 *l.* worth ſuffice, when it is worth 24 *l. per* Ton? *Anſwer* 25 Men.

Queſt. 9. If 6 Men in 24 Days mow 72 Acres; in how many Days will 8 Men mowe 24 Acres? *Anſ.* in 6 Days.

Queſt. 10. If when the Ton of Wine is worth 30 *l.* 100 Men will be ſatisfied with 20 *l.* worth, I deſire to know what the Ton is worth, when 4 *l.* worth will ſatisfy 25 Men at the ſame Rate? *Anſwer* 24 *l. per* Ton.

CHAP. XIV.

The Rule of Three compoſed of Five Numbers.

THE Rule of Three compoſed, is when Queſtions (wherein there are 5 Numbers given to find a 6th in Proportion thereunto) are reſolved by one ſingle Rule of Three compoſed of the 5 given Numbers.

2. When Queſtions may be performed by the Double Rule of Three Direct, and it is required to reſolve them by the Rule of Three compoſed; firſt order or rank your Numbers according to the 7th Rule of the 12th Chap. then

The Rule is,

Multiply the Terms or Numbers (that ſtand one over the other in the firſt Place) the one by the other, and make their Product the firſt Term in the Rule of Three Direct; then multiply the Terms that ſtand one over the other in the third Place, and place their Product for the

3d Term, in the Rule of Three Direct, and put the middle Term of the 7 uppermoſt for a ſecond Term; then having found a 4th Proportion Direct to theſe three, this 4 Proportional ſo found ſhall be the Anſwer required.

So the firſt Queſtion of the 12th Chapter being propo ed, *viz.* If 100 *l.* in 12 Months gain 6 *l.* Intereſt, wh will 75 *l.* gain in 9 Months? The Numbers being ranke (or placed) as is there directed and done.

Then I multiply the two firſt Terms, 100 and 12, th one by the other, and their Product is 1200 for the fir Term; then I multiply the two laſt Terms 75 and 9 toge ther, and their Product is 675 for the third Term. The I ſay, as 1200 is to 6, ſo is 675 to the Anſwer, which b the Rule of Three Direct, will be found to be 3 *l.* 7 *s* 6 as was before found.

3. But if the Queſtion be to be anſwered by the Doubl Rule of Three Inverſe, then (having placed the five give Terms as before) multiply the lowermoſt Term of the fir Place, by the uppermoſt Term of the third Place, and pu the Product for the firſt Term; then multiply the upper moſt Term of the firſt Place, by the lowermoſt Term o the third Place, and put the Product for the third Term and the ſecond Term of the three higheſt Numbers fo the middle Term to thoſe two; then if the Inverſe Pro portion is found in the uppermoſt three Numbers, th fourth Proportional Direct to theſe three ſhall be the An ſwer. So the firſt Queſtion to the 13th Chapter being ſta ted, *viz.* If 100 *l.* Principal in 12 Months gain 6 *l.* Intereſt what Principal will gain 3 *l.* 7 *s.* 6 *d.* in 9 Months? Stat the Number as there directed in the firſt Order, *viz.*

l.	l.	m.		
12	100	9		
l.		l.	s.	d.
6		3	7	5

Then reduce the 6 *l.* and 3 *l.* 7 *s.* 6 *d.* into Pence, the 6 *l.* 1440 *d.* and 3 *l.* 7 *s.* 6 *d.* is 810 *d.* then multiply 1440 b 9, the Product is 12960 for the firſt Term in the Rule Three Direct, and multiply 810 by 12, the Product 9720 for the third Term; then I ſay, as 12960 is to 130 ſo is 9720 to the Anſwer, *viz.* 75 *l.* as before. But the Terms had been placed after the ſecond Order, *viz*

l.

l.	*l.*	*l.*	*s.*	*d.*
6	100	3	7	6
m		m		
12		9		

Then the Inverſe Proportion is found in the loweſt Numbers, and having compoſed the Numbers for a ſingle Rule of Three, as in the ſecond Rule forgoing; then the Anſwer muſt be found by a ſingle Rule of Three Inverſe; for here it falls out to multiply 810 by 12 for the firſt Number, 1440 by 9 for the third Number; and then you muſt ſay, As 9720 is to 100 *l.* ſo is 12960 to the Anſwer, which by Inverſe Proportion will be found to be 75 *l.* as before.

The Queſtion in the 12th and 13th Chapters may ſerve for thy farther Experience.

CHAP. XV.

Single Fellowſhip.

FEllowſhip is that Rule of Plural Proportion, whereby we ballance Accompts depending between diverſe Perſons having put together a general Stock, ſo that they may every Man have his proportional Part of Gain, or ſuſtain his proportional Part of Loſs.

2. The Rule of Fellowſhip is either ſingle, or it is Double.

3. The Single Rule is, when the Stocks propounded are ſingle Numbers, without any Reſpect or Relation to Time each Partner continuing his Money in Stock for the ſame Time.

4. In the Single Rule of Fellowſhip, the Proportion is, as the whole Stock of all the Partners is in Proportion to the total Gain or Loſs, ſo is each Man's particular Share in the Stock, to his particular Share in the Gain or Loſs. Therefore take the Total of all the Stocks for the firſt Term in the Rule of Three, and the whole Gain or Loſs for the ſecond Term, and the particular Stock of any one of the Partners for the third Term; then multiply and divide according to the ſeventh Rule of the ninth Chapter, and the fourth proportional Number is the particular Loſs or Gain of him whoſe Stock you made your

ſecond Number, wherefore repeat the Rule of Three a often as there are particular Stocks or Partners in th Queſtion, and the fourth Terms produced upon the ſeveral Operations are the reſpective Gain or Loſs of thoſe particular Stocks given, as in the Example following.

Queſt. 1. Two Perſons, *viz.* A and B bought a Ton o Wine for 20 *l.* of which A paid 12 *l.* and B paid 8 *l.* an they gained in the Sale thereof 5 *l.* now I demand eac Man's Share in the Gains, according to his Stock.

Firſt, I find the Sum of all their Stocks, by adding them together, *viz.* 12 *l.* and 8 *l.* which are 20 *l.* then according to this Rule, I ſay firſt, if 20 *l.* (the Sum of their Stocks) require 5 *l.* the total Gain, how much will 12 *l.* (the Stock of A) require? Multiply and divide by the 7th Rule of the 9th Chapter, and the Anſwer is 3 *l.* for the Share of A in the Gains; then again I ſay, If 20 *l.* require 5 *l.* what will 8 *l.* require? The Anſwer is 2 *l.* which is the Gain of B, ſo I conclude on the Share o A to the Gain is 3 *l.* and the Share of B in the Gain i 2 *l.* which in all is 5 *l.*

12
8
——
20 *l.*

l. *l.* *l.*
If 20 5 12
12
——
20) 60 (3 *l.*
60
——
(0)

l. *l.* *l.*
If 20 5 8
8
——
20) 42 (*l.*

Queſt. 2. Three Merchants, *viz.* A, B, and C, ente upon a joint Adventure, A put into the common Stoc 78 *l.* B put in 117 *l.* and C put in 234 *l.* and they fin (when they make up their Accompts) that they have gai ed in all 264 *l.* now I deſire to know each Man's particular Share in the Gain.

Firſt, I add their particular Stocks together, and their Sum is 429 *l.* then ſay, If 429 *l.* gain 264 *l.* what will 78 *l.* gain? and what will 117 *l.* and what will 234 (the Stocks of A, B, and C) gain? Work by three ſeveral Rules of Three, and you will find that

78
117
234
——
Sum 29

The Gain of A, B, C is 48, 72, 144

The Gain of		is
	A	48
	B	72
	C	144
	Sum	264

Queſt. 3. Four Partners, *viz.* A, B, C and D, amongſt them built a Ship, which coſt 1730 *l.* of which A paid 346 *l.* B 519 *l.* C 692 *l.* and D 173 *l.* and her Freight, for a certain Voyage is 370 *l.* which is due to the Owners or Builders. I demand each Man's Share therein according to his Charge in Building her.

Anſwer,	
A	74
B	111
C	148
D	37
	370

Queſt. 4. A, B, and C enter into Partnerſhip for a certain Time. A put into a common Stock 364 *l.* B put in 482 *l.* C put in 500 *l.* and they gained 867 *l.* Now I demand each Man's Share in the Gain, proportionable to his Stock? *Anſwer,*

	l.	*s.*	*d.*	
A	234	09	3	$\frac{156}{1338}$
B	310	09	5	$\frac{612}{1346}$
C	322	00	3	$\frac{930}{1345}$
Sum	867	00	0	

5. To prove the ſingle Rule of Fellowſhip. add each Man's particular Gain or Loſs together, [*The Proof of the Rule of Single Fellowſhip*] and if the total Sum is equal to the general Gain or Loſs, then is the Work rightly performed; but otherwiſe it is erroneous. *Example,* In the firſt Queſtion of this Chapter, the Anſwer was. That the Gain of A was 3 *l.* and the Gain of B 2 *l.* which added together, makes 5 *l.* equal to the total Gain given.

If in finding out the particular Shares of the ſeveral Partners, any Thing remain after Diviſion is ended, ſuch Remainders muſt be added together, (they being all Fractions of the ſame Denomination;) and their Sum divided by the common Diviſor in each Queſtion, *viz.* The total Stock, and the Quotient added to the particular Gains, and then if the total Sum is equal to the total Gain, the Work is right, otherwiſe not.

As in the 4th Queſtion, the Remainder were 354, 62, and 930, which added together, make 1346, which divided by 1346, (the Sum of their Stocks) the Quotient is 1 *d.* which I add to the Pence, &c. and the Sum of their Share is 897 *l.* equal to the total Gain, wherefore I conclude the Work is right.

CHAP. XVI.

Double Fellowſhip.

DOuble Fellowſhip, is when ſeveral Perſons enter into Partnerſhip for unequal Time; that is, when every Man's particular Stock hath Relation to a particular Time.

2. In the Double Rule of Fellowſhip, multiply each particular Stock by its reſpective Time, and having added the ſeveral Products together, make their Sum the firſt Number (or Term) in the *Rule of Three,* and the total Gain or Loſs the ſecond Number and the Product of any one's particular Stock by his Time, the third Term, and the fourth Number in Proportion thereunto is his particular Gain or Loſs, whoſe Product of Stock and Time is your third Number.

Then repeat (as in *Single Fellowſhip*) the *Rule of Three* as often as there are Products (or Partners) and the four Terms thereby invented, and the Numbers required.

Example.

Queſt, 1. *A* and *B.* enter Partnerſhip; *A* put in 40 *l.* for 6 Months, *B.* put in 75 *l.* for 4 Months, and they gained 70 *l.* Now I demand each Man's Share in the Gain, proportional to his Stock and Time? *Anſwer A.* 20 *l* *B.* 50 *l.*

To reſo've this Queſtion, I firſt multiply the Stock of A. (*viz*. 40 *l*.) by its Time (3 Months) and the Product is 120; then I multiply the Stock of B by its Time, *viz*. 75 *l*. by 4 and it produceth 300, which I add to the Product of A, his Stock and Time, and the Sum is 420. Then by the Rule of Three direct, I ſay, as 420 (the Sum of the Product) is to 70, (the total Gain) ſo is 120 (the Product of A his Stock and Time) to 20 *l*. (the Share of A in the Gains.) Then I ſay again, as 420 is to 70, ſo is 300 (the Product of B his Stock and Time) to 50 *l*. (the Share of B in the Gains;) And that each is to have for his Share.

l.		*l*.
40		75
3		4
A 120	B	300
		120
	Sum	420

Queſt. 2. A, B, and C make a Stock for 12 Months, A put in at firſt 364 *l*. and 4 Months after that he put in 40 *l*. B put in at firſt 408 *l*. and the End of the 7 Months he took out 86 *l*. C puts in at firſt 148 *l*. and 3 Months after he put in 86 *l* more, and 5 Months after that he put in 100 *l*. more, and at the End of 12 Months their Gain is found to be 1436 *l*. I deſire to know each Man's Share in the Gains, according to his Stock and Time?

Firſt, I conſider that the whole Time of their Partnerſhip is 12 Months. Then I proceed to find out the ſeveral Products or Stock and Time as followeth:

A had at firſt 364 *l*. for 4 Months, wherefore that Product is —— 1456

Then he put in 40 *l*. which with the firſt Sum makes 404 *l*. which continued the Remainder of the Time, *viz*. 8 Months, and that Product is —— 3233

The Sum of the Products of the Stock and Time of A is —— 4688

B had 408 *l*. in 7 Months, whoſe Product is —— 2856

And then took out 86 *l*. therefore he left in Stock 322 *l*. which continued the reſt of the Time, *viz*. 5 Months, whoſe Product is —— 1610

The Sum of the Products of the Stock and Time of B is —— 4466

C put in 148 *l*. for 3 Months, whoſe Product being multiplied by 3, is —— 444

Then he put in 86 *l.* which, added to the firſt (*viz.* 148 *l.*) makes 234 *l.* which lay in Stock 5 Months, and their Product is———— 1170

Then he put in 100 *l.* more, ſo then he had in Stock 334 *l.* which continued the Remainder of the Time, 4 Months, which multiplied together, produces———— 1336

The Sum of the Product of the Money and Time of C is————	2950
B	4466
C	4688
The total Sum of all the Products is————	12104

Then I ſay, as 12104 is to 1426 (the total Gain) ſo is 4688 to the Share of A in the total Gain, &c. go on as in the foregoing Examples, and you will find their Shares in the Gain to be as followeth, *viz.* *Anſwer,*

The Share of				
A	is	556	03	6 $\frac{6191}{12104}$
B		520	16	9 $\frac{5496}{12103}$
C		349	19	8 $\frac{416}{12104}$
		1436	00	0

Queſt. 3. Three Graſiers, A, C. and C, take a Piece of Ground for 46 *l.* 10 *s.* in which A put 12 Oxen for 8 Months, B put in 16 Oxen for 5 Months, and C put 18 Oxen for 4 Months; now the Queſtion is, what each Man ſhall pay for the 46 *l.* 10 *s.* for his Share in that Charge.

Anſwer,

		l.	s.
A	ſhall pay	18	00
B		15	00
C		13	10

3. The Proof of this Rule is the ſame with that of Single Fellowſhip, laid down in the 5th Rule of the 15th Chapter; and note, that

If a Loſs be ſuſtained inſtead of a Gain among Partners, every Man's Share to be born in the Loſs, is to be found after the ſame Method as their Gain, whether their Stocks be for equal or unequal Time.

CHAP. XVII.

Alligation Medial.

1. THE Rule of Alligation is that Rule in Plural Proportion by which we reſolve Queſtions, wherein is a Compoſition or Mixture of diverſe Simples, as alſo it is uſeful in Compoſition of Medicines, both for Quantity, Quality, or Price: And its Species are two, *viz.* Medial and Alternate.

2. Alligation Medial, is, when having the ſeveral Quantities and Prices of ſeveral Simples propounded, we diſcover the mean Price or Rate of any Quantity of the Mixture compounded of thoſe Simples, and the Proportion is,

As the Sum of the Simples to be mingled is to the total Value of all the Simples, ſo is any Part or Quantity of the Compoſition or Mixture to its mean Rate or Price.

Queſt. 1. A Farmer mingled 20 Buſhels of Wheat at 5 *s. per* Buſhel, and 36 Buſhels of Rye at 3 *s. per* Buſhel, with 40 Buſhels of Barley at 2 *s. per* Buſhel, now I deſire to know what one Buſhel of that Mixture is worth?

To reſolve this Queſtion, add together the given Quantities, and their Value, which is 96 Buſhels, whoſe total Value is 14 *l.* 8 *s.* as appeareth by the Work following. For,

	Buſhels		*l.*	*s.*
	20	of Wheat, at 5 *s. per* Buſhel, is	5	0
	36	of Rye, at 3 *s. per* Buſhel, is	5	8
	40	of Barley, at 2 *s. per* Buſhel, is	4	0
The Sum of their given Quantities is	96,	and their Value is,	14	8

Then ſay, by the Rule of Three Direct, if 96 Buſhels coſt, or is worth 14 *l.* 8 *s.* what is one Buſhel worth?

bush. l. s. bush.
96 14 8 1 bush.
20

96) 288 (3 *s.*

288 *Facit* 3 *s. per* Bushel.

(0)

Queſt. 2. A Vintner mingled 15 Gallons of Canary at 8 *s. per* Gallon, with 20 Gallons of *Malaga*, at 7 *s.* 6 *d. per* Gallons, with 10 Gallons of *Malaga*, at 6 *s.* 8 *d. per* Gallon, and 24 Gallons of White wine at 4 *s. per* Gallon: Now I demand what a Gallon of this Mixture is worth? Work as in the laſt Queſtion, and you will find the Anſwer to be 6 *s.* 2 *d.* 2 *qrs.* $\frac{46}{69}$.

Queſt. 3. A Grocer hath mingled 3 *C.* of Sugar at 56 *s. per C.* with 3 *C.* of Sugar at 3 *l.* 14 *s.* 8 *d. per C* and with 6 *C.* at 1 *l.* 17 4 *d. per C.* I deſire to know the Price of a *C. wt.* of that Mixture.

Anſwer 2 *l.* 13 *s.* 1 *d.* $\frac{7}{12}$.

3. The Proof of this Operation, is by the Price of any Quantity of the Mixture, to find out the total Value of the whole Compoſition, and if it is equal to the total Value of the ſeveral Simples, the Work is right, otherwiſe not. [*The Proof of Alligation Medial.*] As in the firſt Example, the Anſwer to the Queſtion was that 3 *s.* is the Price of 1 Buſhel; wherefore I ſay, by the Rule of Proportion, if 1 Buſhel be 3 *s.* what is 96 Buſhels? *Anſwer* 14 *l.* 8 *s.* which is the total Value of the ſeveral Simples: Wherefore the Work is right.

CHAP. XVIII.

Alligation Alternate

1. ALligation Alternate is, when there are given the particular Prices of ſeveral Simples, and thereby we diſcover ſuch Quantities of thoſe Simples, as being mingled together, ſhall bear a certain Rate propounded.

2. When ſuch a Queſtion is ſtated, place the given Prices of the Simple one over the other, and the propounded Price of the Compoſition againſt them in ſuch Sort, that it may repreſent a Root and they as ſo many Branches ſpringing from it, as in the following Example.

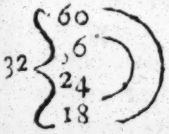
Queſt. 1. A certain Farmer is deſirous to mix 20 Buſhels of Wheat at 5 *s.* or 60 *d. per* Buſhel, with Rye at 3 *s.* or 36 *d. per* Buſhel, and with Barley at 2 *s.* or 24 *d. per* Buſhel, and Oats at 1 *s.* 6 *d. per* Buſhel, and deſireth to mix ſuch a Quantity of Rye, Barley and Oats, with the 20 Buſhels of Wheat, as that the whole Compoſition may be worth 2 *s.* 8 *d.* or 32 *d. per* Buſhel.

The Prices of the Simples being placed according to the laſt Rule (with the Price of the Compoſition propounded as a Root to them) will ſtand as followeth.

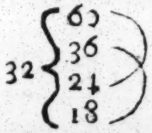
$$32\begin{cases}60 \text{ Pence}\\36\\24\\18\end{cases}$$

3. Having thus placed the given Numbers, you are to link the ſeveral Rates of the Simples one to the other, by certain Arches, in ſuch Sort, that one that is leſſer than the mean Rate, may be coupled to another that is greater than the mean Rate; ſo the Queſtion laſt propounded will ſtand,

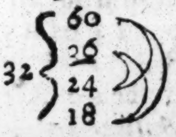
1. *Thus,*



2. *Or thus,*



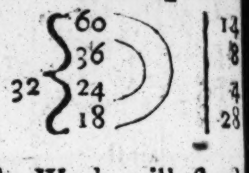
3. *Or thus,*



4. Then take the Difference between the Root and the ſeveral Branches and place the Difference of each againſt the Number or Branch with which it is coupled or linked, and having taken all the Differences and placed them as aforeſaid, than thoſe Differences ſo placed, will ſhew you the Number of each Simple to be taken to make a Compoſition to bear the mean Rate propounded.

So the Branches of the laſt Queſtion being linked together, as in the Manner, I ſay, the Difference between 32 and 60, is 28; which I put againſt 18, becauſe 60 is linked with 18, then the Difference between 32 and 36 is 4, which I put againſt 24, becauſe 36 is linked or

coupled



coupled with 24, then I ſay, the Difference between 32 and 24 is 8, which I place againſt 36, (for the Reaſon aforeſaid) then I ſay, the Difference between 32 and 18 is 14, which I place againſt 60; and then the Work will ſtand as you ſee in the Margent.

So I conclude that a Compoſition made of 14 Buſhels of Wheat at 9 *d. per* Buſhel, and 8 Buſhels of Rye at 36 *d. per* Buſhel, and 5 Buſhels of Barley at 24 *d. per* Buſhel, and 28 Buſhels of Oats at 18 *d. per* Buſhel, will bear the mean Price of 32 *d.* or 2 *s.* 8 *d. per* Buſhel. And here obſerve, That in the Compoſition there is but 14 Buſhels of Wheat; but I would mingle 20 Buſhels, and this Kind (or rather Caſe) of Alligation Alternate, *viz.*) when there is given a certain Quantity of one of the Simples, and the Quantities of the reſt ſought to mingle with this given Quantity, (that the whole may bear a Price propounded) is called Alternation Partiel.

And the Proportion to find out the ſeveral Quantities to be mingled with the given Quantity, is thus.

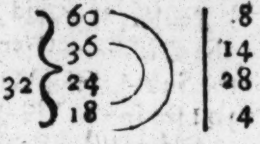
As the Difference annexed to the Branch, that is, the Value of an Integer of the given Quantity, is to the other particular Differences, ſo is the Quantity given to the ſeveral Quantities required.

So here, to find how much Rye, Barley, and Oats, muſt be mingled with the 20 Buſhels of Wheat, I ſay, by the Rule of Three direct, if 14 Buſhels of Wheat require 8 Buſhels of Rye, what will 20 Buſhels of Wheat require? *Anſwer* $11\frac{6}{14}$ Buſhels of Rye.

Again, If 14 Buſhels of Wheat require 4 Buſhels of Barley, what will 20 Buſhels of Wheat require? *Anſ.* $5\frac{10}{14}$ Buſhels of Barley. Again I ſay, If 14 Buſhels of Wheat require 28 Buſhels of Oats, what will 20 Buſhels of Wheat require? *Anſwer* 40 Buſhels of Oats.

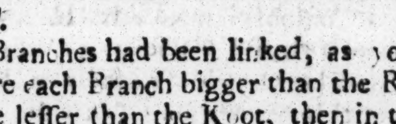
And now I ſay, that 20 Buſhels of Wheat mingled with $11\frac{6}{14}$ Buſhels of Rye, and $5\frac{10}{14}$ Buſhels of Barley and 40 Buſhels of Oats, each bearing the Rate as aforeſaid, will make a Compoſition or Heap of Corn, that may yeild 32 *per* Buſhel.

But if the Branches had been coupled according to the ſecond Order, or Manner, the Differences would have been thus placed, *viz.* the Difference between 33 and 60 is 28, which I ſet againſt 24, becauſe 60 is linked thereto; and the Difference between 32 and 36 is 4, which I ſet againſt 18; and the Difference between 32 and 24 is 18, which I ſet againſt 60; then the Difference between 32 and 18 is 14 which I ſet againſt his Yoke fellow 36; and then I conclude, that if you mix 8 Buſhels of Wheat with 14 Buſhels of Rye, 28 Buſhels of Barley, and 4 Buſhels of Oats, each bearing the aforeſaid Prices, the whole Mixture may be ſold for 32 *d.* *per* Buſhel, as by the Work in the Margent.



You ſee by this Work we have found how many Buſhels of Rye, Barley, and Oats, ought to be mixed with 8 Buſhels of Wheat, and to find out how many of each ought to be mixed with 20 Buſhels of Wheat, I ſay, as 1 is to 14, ſo is 20 to 35 Buſhels of Rye. As 1 is to 28, ſo is 20 to 70 Buſhels of Barley. As 8 is to 4, ſo is 20 to 10 Buſhels of Oats; whereby I conclude that if to 20 Buſhels of Wheat I put 35 Buſhels of Rye, 70 Buſhels of Barley, and 10 Buſhels of Oats, bearing each the aforeſaid Price *per* Buſhel, that then a Buſhel of this Mixture will be worth 32 *d.* 2 *s.* 8 *d.*

And if the Branches had been linked, as you ſee in the 3d Place, where each Branch bigger than the Root is link'd to two that are leſſer than the Root, then in this Caſe you muſt have placed the ſeveral Differences between the Root and Branches, againſt thoſe two with which each is coupled as firſt, the Difference between 32 and 60 is 28, which I ſet againſt 24 and 18, becauſe it is coupled with them both, then the Difference between 32 and 36 is 4, which I ſet likewiſe againſt 3, and 18, becauſe 36 is linked to them both, then the Difference between 22 and 24 is 8, which I put againſt 60 and 35, becauſe 24 is linked to them



them both, then the Difference between 32 and 18 is 14, which I put againſt 60 and 36, the Yoke-Fellows of 18.

Laſtly, I draw a Line behind the Differences, and add the Differences which ſtand againſt each Branch, and put the Sum behind the ſaid Line againſt its proper Branch, as you ſee in the Margent.

And now by this Work, I find that 22 Buſhels of Wheat mingled with 22 Buſhels of Rye, and 32 Buſhels of Barley, and 22 Buſhels of Oats, each bearing the ſaid Price, will make a Mixture bearing the mean Rate of 32 *d. per* Buſhel.

And to find how much of each of the reſt muſt be mingled with 20 Buſhels of Wheat; I ſay,

As 22 is to 32, ſo is 20 to 29 Buſhels of Rye. As 22 is to 32, ſo is 20 to 19 $\frac{1}{11}$ Buſhels of Barley. As 22 is to 32, ſo is 20 to 29 $\frac{1}{11}$ Buſhels of Oats.

Whereby you ſee the Queſtions of Alligation Alternate, will admit of more true Anſwers than one; for we have found 3 ſeveral Anſwers to this 1ſt Queſtion.

The Proof of Alternation *Partiel.*

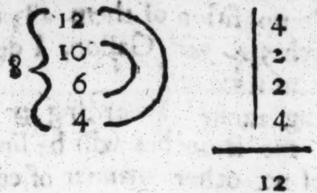
Queſtions of Alligation Partiel are proved the ſame Way with Queſtions in Alligation Medial, which you may ſee in the 3d Rule of the 17th Chapter.

Queſt 3. A Grocer hath 4 Sorts of Sugar, *viz.* of 12 *d. per l.* of 10 *d. per l.* of 6 *d. per l.* and of 4 *d. per l.* and would have a Compoſition worth 8 *d. per l.* the whole Quantity whereof ſhould contain 144 *l.* made of theſe four Sorts, I demand how much of each he muſt take.

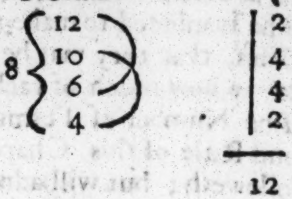
Queſtions of this Nature are reſolved by that Part of Alligation Alternate, called by Arithmeticians Alligation Total, *viz.* where there is given the Sum and Price of ſeveral Simples, to find out how much of each Simple ought to be taken to make the ſaid Sum or Quantity, ſo that it may bear a certain Rate propounded.

To reſolve this Queſtion, I place the ſeveral Prices of the Simples and Mean Rate propounded, and link them together as is directed in the 2d and 3d Rules of this Chapter, and place the Difference between the Root and Branches, according to the 4th Rule of this Chapter, which will then ſtand one of theſe 3 Ways, *viz.*

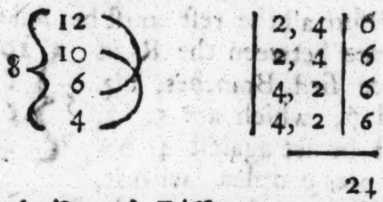
Firſt



Second



Third



5. Then add the ſeveral Differences together, which I have done, and the Sums of the firſt and ſecond Order are 12 *l.* and of the 3d. 24 *l.* as you ſee above. But it required that there ſhould be 144 *l.* of the Compoſition, therefore to find the Quantity of each Simple to make the whole Compoſition 144 *l.* Obſerve this general Rule, *viz.*

As the Sum of the Differences is to the ſeveral Differences, ſo is the total Quantity of the Compoſition to the Quantity of each Simple.

So to find how much of each Sort of Sugar I ought to take to make 144 *l.* at 8 *d. per l.*

As 12 is to 4, ſo is 144 to 48 *l.* at 12 *d. per l.*
As 12 is to 2, ſo is 144 to 24 *l.* at 10 *d. per l.*
As 12 is to 2, ſo is 144 to 24 *l.* at 6 *d. per l.*
As 12 is to 4, ſo is 144 to 48 *l.* at 8 *d. per l.*

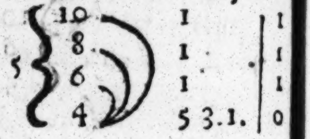
Whereby I find that 48 *l.* at 12 *d. per l.* and 24 *l.* at 10 *d. per l.* and 24 *l.* at 6 *d. per l.* and 48 *l.* at 4 *d. per l.* will make a Compoſition of Sugar containing 144 *l* worth 8 *d. per l.*

But as the Branches are linked in the 2d Order, the Anſwer will be 24 *l.* at 12 *d. per l.* and 48 *l.* at 10 *d. per l.* and 48 *l.* at 6 *d. per l.* and 24 *l.* at 4 *d per l.* to make the ſaid Quantity, and to bear the ſaid Price.

And if you had worked as the Branches are linked from the third Order, then you would have found the Quantity of 36 *l.* of each.

Queſt. 3. A Vintner hath four ſorts of Wine, *viz.* Canary at 10 *s. per* Gallon, Malaga at 8 *s. per* Gallon, Rheniſh-wine at 6 *s. per* Gallon, and White wine at 4 *s. per* Gallon, and he is minded to make a Compoſition of them all of 60 Gallons, that they may be worth 5 *s. per* Gallon, I deſire to know how much of each he muſt have?

The Number of Terms being ranked according to the ſecond Rule of this Chapter, the Branches will be linked as followeth; but will admit of no other manner of coupling, becauſe there is but one Branch that is leſſer than the Root; therefore all the reſt muſt be linked unto it; and the Difference between the Root and the three firſt Branches, *viz.* 10, 8, and 6, which are 5, 3, and 1, muſt be ſet againſt 4, becauſe they are coupled with it, and the Difference between the Root, (*viz.*) 5 and 4, which is 1, muſt be ſet againſt the 3 others, becauſe it is linked to them all; ſo I find 1 Gallon of Canary, 1 Gallon of Malaga, 1 Gallon of Rheniſh-wine and 9 Gallons of White-wine, prized as above, being mingled together will be worth 5 *s. per* Gallon, the Sum being 12 Gallons; but there muſt be 60 Gallons; whereof I ſay,

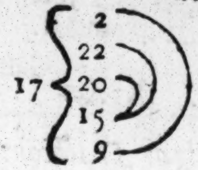


As 12 is to 1, ſo is 60 to 5 Gallons of Canary.
As 12 is to 1, ſo is 60 to 5 Gallons of Malaga.
As 12 is to 1, ſo is 60 to 5 Gallons of Rheniſh.
As 12 is to 9, ſo is 60 to 45 Gal. of White-wine,

ſo that 5 Gallons of Canary, 5 Gallons of Malaga, 5 Gallons of Rheniſh, and 45 of White-wine, mingled together, will be in all 60 Gallons worth 5 *s. per* Gallon, which was required.

Queſt 4. A Goldſmith hath Gold of four ſeveral Sorts of Fineneſs, *viz.* of 24 Carects fine, and of 22 Carects fine, of 20 Carects fine, and of 15 Carects fine. [*Read Chap.* 2. *Def.* 2. *of this Book*] And he would mingle ſo much of each with Allay, that the whole Maſs of 28 Ounces of Gold ſo mingled, may bear 17 Carects fine. I demand how much ſo mingled, may bear 17 Carects fine. I demand how much of each he muſt take? The 2d and 3d Rules of this Chapter being obſerved; (for inſtead of the Alley I put o because it bears no Fineneſs, but it makes a Branch in the Operation) the Terms may be alligated, and the Differences added by any of theſe 4 Ways following. *viz.*

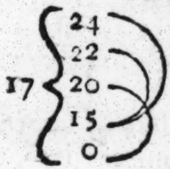
First thus,



17		17
2		2
2,	17	19
5,	3	8
7,	3	10

Sum 56

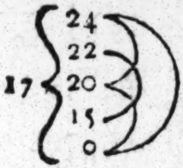
Secondly thus,



2		2
17		17
2,	17	19
7,	3	10
5,	3	8

Sum 56

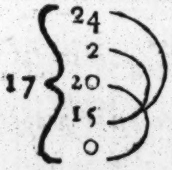
Thirdly thus,



3		2
2		2
2,	17	19
7,5	3.	15
3,		3

Sum 41

Fourthly thus,



2,		17,	19
2,		17.	19
2,		17,	19
7,	5,	3,	15
7,	5,	3,	19

Sum 87

More Ways may be given for the alligating or linking of the Terms in this Queſtion, but theſe, if well practiſed, are ſufficient for underſtanding the Rules of Alligation.

In Queſtions of Alligation Total the Anſwer is given true, when the Sum of each of the Quantities of Simples found, [*The Proof of Alternation Total*] agrees with the Sum or Quantity propounded; as in the laſt Queſtion, the Anſwer was 8 *oz.* 10 *p. w.* of 24 Carects fine, 10 *oz.* of 22 Carects fine, 9 *oz.* 10 *p. w.* of 20 Carects fine, 4 of

25 Carects fine, and 3 *oz.* of Alloy, which added together, make 28 *oz.* the Quantity propounded.

CHAP. XIX.

Reduction of Vulgar Fractions.

1. WHAT a Vulgar Fraction is, hath been already ſhewed, in the firſt Chapter of this Book, to which I refer the Reader to look cautiouſly into.

2. To reduce a Vulgar Fraction, obſerve carefully theſe 8 following Rules.

1. To reduce a mixt Number into an improper Fraction.

2. To reduce a whole Number into an improper Fraction.

3. To reduce an improper Fraction into its equivalent Whole, (or Mixt) Number.

3. To reduce a Fraction into the loweſt Terms equivalent to the Fraction given.

5. To find the Value of a Fraction in the known Parts of Coin, Weight, Meaſure, *&c.*

6. To reduce a Compound Fraction to a Simple-one of the ſame Value.

7. To reduce diverſe Fractions having unequal Denominations to Fractions of the ſame Value, having an equal Denominator.

8. To reduce a Fraction of one Denomination to another of the ſame Value.

I. *To reduce a mixt Number to an improper Fractions.*

The Rule is,

Multiply the Integer Part (or whole Number) by the Denominator of the Fraction [*Vid. Chap.* 1. *Defin.* 31.] and to the Product add the Numerator, and that Sum place over the Denominator for a new Numerator, ſo this new Fraction ſhall be equal to the mixt Number given. As for Example.

1. Reduce 18 $\frac{3}{7}$ into an improper Fraction, multiply the whole Number 18 by 7 the Denominator, and to the Product add the Numerator 3, the Sum is 129 which put over the Denominator 7, and it makes $\frac{129}{7}$ for the Anſwer as followeth.

$18\frac{3}{7}$
7

Facit $\frac{129}{7}$

2. Reduce $113\frac{5}{21}$ to an improper Fraction *facit*, $\frac{2205}{21}$
3. Reduce $50\frac{2}{21}$ to an improper Fraction, *facit*, $\frac{1180}{21}$

II. *To reduce a Whole Number into an improper Fraction.*

The Rule is, Multiply the given Number by the intended Denominator, and place the Product for the Numerator over it. [*Vide Chap.* 1. *Defin.* 23.] As for Example.

1. Let it be required to reduce 14 into a Fraction, whoſe Denominator ſhall be 12 To effect which I multiply 15 by the intended Denominator (12) the Product is 180, which I place over 12 as a Numerator, and it makes $\frac{180}{12}$, which is equal to 15 *Facit* $\frac{180}{12}$ as was required; as *per* Mergent.

15
12

30
15

180

2. Reduce 36 into an improper Fraction, whoſe Denominator ſhall be 26 *Facit* $\frac{936}{26}$.

3. Reduce 135 into an improper Fraction, whoſe Denominator ſhall be 16 *Facit* $\frac{2160}{16}$.

III. *To reduce an improper Fraction int into its equivalent whole or mixt Number.*

The Rule is, Divide the Numerator by the Denominator, and the Quotient is the whole Number equal to the Fraction, and if any Thing remain, put it for a Numerator over the Diviſor. *Example*,

1. Reduce $\frac{436}{8}$ into its equivalent mixt Number, Divide the Numerator 435 by the Denominator 8, and the Quotient is 54, and 3 remains, which put for a Numerator over the Diviſor 8, the Anſwer is $54\frac{3}{8}$, as followeth.

8) 436 (54
40

---

36 *Facit* $54\frac{4}{8}$,
32

---

(4)

2. Reduce $\frac{1476}{75}$ to a mixt Number, *Facit* 231 $\frac{1}{15}$.
3. Reduce $\frac{25576}{138}$ to a mixt Number. *Facit* 114, $\frac{72}{38}$.

IV. *To reduce a Fraction into its loweſt Terms equivalent to the Fraction given.*

The Rule is, 1. If the Numerator and Denominator are even Numbers, take half the one and half of the other, as often as may be, and when either of them falls out to be an odd Number, then divide them by any Number that you can diſcover, will divide both Numerator and Denominator without any Remainder; and when you have thus proceeded as low as you can reduce them, then this new Fraction ſo found out, ſhall be the Fraction you deſire, and will be in Value to the given Fraction.

Example 1. Let it be required to reduce $\frac{192}{336}$ into its loweſt Terms. Firſt I take the Half of the Numerator 192, and it is 96, then Half of the Denominators, and it is 168, ſo that it brought to $\frac{96}{168}$, anp next to $\frac{48}{84}$, and by halfing ſtill, to $\frac{24}{48}$ and their half is $\frac{12}{21}$, and now I can no longer half it it, becauſe 21 is an odd Number, wherefore I try to divide them by 3, 4. 5. 6, &c. and I find 3 divides them both without any Remainder, and brings them $\frac{4}{7}$, as *per* Margeat.

129	96	48	14	12	4
336	168	84	42	21	7

So I conclude $\frac{4}{7}$, thus found to be equal in Value to the given Fraction $\frac{192}{336}$.

2. What is $\frac{1036}{1084}$ in its loweſt Terms? *Anſ.* $\frac{7}{1}$.
3. What is $\frac{1342}{1586}$ in its loweſt Terms? *Anſ.* $\frac{1}{1}$.

The beſt Way to reduce a Fraction into its loweſt Terms, is, by finding a common Meaſure, *viz.* the greateſt Number that will divide the Numerator and Denominator without any Remainder, and by that Means reduce a Fraction to its loweſt Terms at the firſt Work; and to find out this common Meaſure, divide the Denominator by the Numerator, and if any thing remain, divide your Diviſor thereby; and if any Thing remain, then divide your laſt Diviſor by it; do ſo until you find nothing remaining: Then this laſt Diviſor ſhall be your greateſt common Meaſurer, which will divide both Numerator and Denominator, and reduce them both into their loweſt Terms at one Work. Ex-

Example 4. Reduce $\frac{228}{634}$ into its loweſt Terms by a common Meaſurer; to Effect which, I divide the Denominator 304 by the Numerator 228, and there remains 76, then I divide 228 (the firſt Diviſor) by 76 (the Remainder) and it quotes 3, and nothing remains; wherefore the laſt Diviſor 76 is the common Meaſurer; by which I divide the Numerator of the given Fraction, *viz.* 228 it quotes 3 for a new Numerator, then I divide the Denominator 304 by 76, and it quotes 4 for a new Denominator, ſo that now I have found $\frac{3}{4}$ equal to $\frac{228}{304}$.

5. Reduce $\frac{6048}{7892}$ into its loweſt Terms by a common Meaſurer, *Facit*, $\frac{9}{12}$.

6. Reduce $\frac{3081}{20382}$ into its loweſt Terms by a common Meaſurer, *Facit*, $\frac{12}{88}$.

A Compendium.

Note, That if the Numerator or Denominator of a Fraction, end each with a Cypher or Cyphers, then cut off as many Cyphers from the one as from the other, and the remaining Figures will be a Fraction of the ſame Value, *viz.* $\frac{3400}{7100}$ will be found to be reduced to $\frac{34}{71}$, by cutting off the two Cyphers from the Numerator and Denominator with a Daſh of the Pen thus, $\frac{34|00}{71|00}$, and $\frac{4600}{7000}$ will be $\frac{46}{70}$, thus, $\frac{46|0}{70|0}$, &c.

V. *To find the Value of a Fraction in the known Parts of Coin, Weights, &c.*

The Rule is, Multiply the Numerator by the Parts of the next inferior Denomination that are equal to an Unit of the ſame Denomination with the Fraction; then divide that Product by the Denominator, and the Quote gives you its Value in the ſame Parts you multiply'd by, and if any Thing remain, multiply it by the Parts of the next inferior Denomination, and divide as before; do ſo till you can bring it no lower, and the ſeveral Quotients, will give you the Value of the Fraction as was required; and if any at laſt remain, place it for a Numerator over the former Denominator. Some few Examples will make the Rule plain.

1. What is the Value of $\frac{27}{29}$ *l. Sterling*? To anſwer this Queſtion, I multiply the Numerator 27 by 20, (the Shillings in a Pound) the Product is 540, which I divide by 29 (the Denominator) and the Quotient is 18 *s.* and there remains 18, which I multiplied by 12 Pence, and the Product (216) I divide by the Denominator 29, the Quotient is 7 *d.* and 13 remains, which I multiply by 4 Farthings, the Product is 52, which I ſtill divide by 29, the Quotient is 1 *qr.* and there remaineth 23, which I put for a Numerator over the Denominator 29, ſo I find the Value of $\frac{27}{29}$ *l.* to be 18 *s.* 7 *d.* 1 *qr.* $\frac{23}{29}$, as by the Work in the Margent, and after the ſame Manner are the Values of the Fractions in the ſeveral Examples following found out.

```
                  27/29 l.
                  27
       Multiply   20
                ------
           29)  540   18s. 7d. 1 23/29
                 ..
                 29
                ----
                250
                232
                ----
       Rem.     (18)
       Mul.      12)
                ----
                 35
                 18
                ----
            29 (216   7 d.
                203
                ----
       Rem.     (13)
       Mult.      4
                ----qr.
           29)   52 (1  23/29
                 29
                ----
       Rem.     (23)
                  s.   d.   qr.
          Facit  18    7    1  23/29
```

And ſo likewiſe you may find the Value of any Fraction, either in Weight or Time, &c.

VI. *To reduce a Compound Fraction to a Simple of the ſame Value.*

What a Compound Fraction is hath been ſhewn in Chap. 1. Definition 24 and to reduce it to a Simple Fraction of the ſame Value.

The Rule is, Multiply the Numerators continually, and place the laſt Product for a new Numerator, then multiply the Denominators continually, and place the laſt Product for a new Denominator. So this ſingle Fraction ſhall be equal to the compound Fraction. *Example.*

1. Reduce $\frac{2}{3}$ of $\frac{3}{5}$ of $\frac{5}{8}$ to a ſimple Fraction.

Multiply the Numerators 2, 3, and 5 together, they make 30 for a new Numerator; then I multiply the Denominators 3, 5, and 8 together, and their Product is 120 for a Denominator, ſo the ſimple Fraction is $\frac{30}{120}$, and cutting off the Cyphers, it is $\frac{3}{12}$, equal to $\frac{1}{4}$ by the 4th Rule following.

$$\begin{array}{cc} 5 & 3 \\ 3 & 2 \\ \hline 15 & 6 \\ 8 & 5 \\ \hline 120 & 30 \end{array}$$

Facit $\frac{30}{120}$, or $\frac{3}{12}$, or $\frac{1}{4}$.

2. What is $\frac{7}{10}$ of $\frac{5}{9}$ of $\frac{4}{7}$ of $\frac{11}{12}$? *Anſwer* $\frac{1540}{7560}$, or $\frac{154}{756}$, or $\frac{77}{378}$ in its loweſt Terms.

3. What is $\frac{11}{12}$ of $\frac{13}{14}$ of $\frac{21}{19}$? *Anſwer* $\frac{3003}{4872}$.

By this you may know how to find the Value of a compound Fraction, *viz.* Firſt reduce it in a Simple one, and then find out his Value by the 5th Rule foregoing.

Example 4. What is the Value of $\frac{3}{4}$ of $\frac{5}{8}$, of $\frac{9}{12}$ of a Pound? *Anſwer* 12 *s.* 3 *d.*

VII. *To reduce Fractions of unequal Denominations to Fractions of the ſame Value, having equal Denominators.*

The Rule is, Multiply all the Denominators together, and the Product ſhall be the common Denominator. Then multiply each Numerator into all the Denominators, except its own, and the laſt Product put for a Numerator over the Denominator, found out as before: So this new Fraction is equal to that Fraction whoſe Numerator you multiply into the ſaid Denominator. Do ſo by all the Numerators given, and you have your Deſire.

Example.] 1. Reduce $\frac{3}{4}$ $\frac{4}{5}$ $\frac{5}{6}$ and $\frac{7}{8}$ to a common Denominator. Multiply the Denominators 4, 5, 6, and 8 together continually, and put the Products 960 for the common Denominator; then multiply the Numerator 3 into the Denominators 5, 6, and 8 and the Product is 720, which is a Numerator to 960 (found as before) ſo $\frac{720}{960}$ is equal to the firſt Fraction $\frac{3}{4}$; then I proceed to find a new Numerator to the 2d Fraction, *viz.* $\frac{4}{5}$, and I multiply 4 (into all the Denominators except its own, *viz.*) into 4, 6, and 8, which produceth $\frac{108}{960}$ equal to $\frac{4}{5}$, then multiply the Numerator 5 into the Denominators 4, 5, and 8, the Product is $\frac{800}{960}$ equal to $\frac{5}{6}$. Then multiply the Numerator 7 into the Denominators 4, 5, and 6, the Product is $\frac{840}{960}$ equal to $\frac{7}{8}$; and the Work is done; ſo that for $\frac{3}{4}\frac{4}{5}\frac{5}{6}$ and $\frac{7}{8}$, I have $\frac{720}{960}$ $\frac{668}{760}$ $\frac{800}{960}$ and $\frac{840}{960}$.

2. Reduce $\frac{11}{12}$, $\frac{14}{25}$, and $\frac{19}{21}$ in a common Denominator, *faciunt*, $\frac{3311}{5796}$, $\frac{3725}{6786}$, and $\frac{5247}{5795}$.

VIII. *To reduce a Fraction of one Denomination to another.*

1. This either Aſcending or Deſcending. Aſcending is when a Fraction of a ſmaller is brought to a greater Denomination; Deſcending, when a Fraction of a greater Denomination is brought lower.

2. When a Fraction is to be brought from a leſſer to a greater Denomination, then make of it a Compound Fraction, by comparing it with the intermediate Denominations between it, and that you would have it reduced to; then (by the 6th Rule foregoing) reduce your Compound to a ſingle Fraction, and the Work is done. *Example.*

Queſt 1. It is required to know what Part of a Pound *Sterling* $\frac{5}{7}$ of a Penny is?

To reſolve this, I conſider that 1 *d.* is $\frac{1}{12}$ of a Shilling, and a Shilling is $\frac{1}{20}$ of a Pound; wherefore $\frac{5}{7}$ *d.* is $\frac{5}{7}$ of $\frac{1}{12}$ of $\frac{1}{20}$ of a Pound, which by the ſaid 6th Rule I find to be $\frac{5}{1680}$ of a Pound *Sterl.* of *Engliſh* Money.

Queſt. 2. What Part of a Pound *Troy-weight* is $\frac{4}{5}$ of a Penny-weight? *Anſ.* $\frac{4}{5}$ of $\frac{1}{20}$ of $\frac{1}{12}$, equal to $\frac{4}{1200}$ *Troy.*

3. When a Fraction is to be brought from a greater to a leſſer Denomination, then multiply the Numerator by the Parts contained in the ſeveral Denominations betwixt it, and the Parts you would reduce it to; then place the laſt Product over the Denomination of the given Fraction. *Exam-*

Queſt. 3. I would reduce $\frac{3}{5}$ *l.* to the Fraction of 1 *d.* to do which, I multiply the Numerator 3 by 20 and 12, the Product is 720, which I put over the Denominator 5, it makes $\frac{720}{5}$ of 1 *d.* equal to $\frac{3}{5}$ *l.*

Queſt. 4. What Part of an Ounce *Troy* is $\frac{69}{16}$? *Anſwer,* $\frac{1}{13}$ oz.

CHAP.

CHAP. XX.

Addition of Vulgar Fractions.

1. IF your Fractions to be added have a common Denominator, then add all the Numerators together, and place their Sum for a Numerator to the common Denominator, which new Fractions is the Sum of all the given Fractions; and if it be improper, reduce it to a whole or mixt Number by the 3d Rule in the 29th Chapter.

Queſt. 1. What is the Sum of $\frac{7}{24}$, $\frac{9}{24}$, $\frac{16}{24}$ and $\frac{14}{24}$?

The Denominators are equal, *viz.* every one is 24, wherefore add the Numerators together, *viz.* 7, 9, 16, and 14, their Sum is 46, which put over the Denominator 24, it makes $\frac{46}{24}$ the Sum of the given Fractions, which will be reduced to the mixt Numbers 1 $\frac{22}{24}$, or 1 $\frac{11}{12}$.

2. But if the Fractions to be added have unequal Denominators, then reduce them to a common Denominator by the 7th Rule of Chapter 19, and then add the Numerators together, and put the Sum over the common Denominator, *&c.* as before in the laſt Example.

Queſt. 2. What is the Sum of $\frac{3}{5}$, $\frac{7}{8}$, $\frac{6}{13}$, and $\frac{11}{12}$;

The Fractions reduced to a common Denominator, are $\frac{1585}{4800}$, $\frac{4300}{4800}$, $\frac{4320}{4800}$, and $\frac{4400}{4800}$, the Sum of their Numerators is 14905, which put over the common Denominator makes $\frac{14905}{3240}$, or $\frac{158}{48}$ equal to the mixt Numbers 3 $\frac{14}{48}$ or 3 $\frac{7}{24}$, for the Sum required.

Queſt. 3. What is the Sum of $\frac{13}{17}$, $\frac{11}{42}$, and $\frac{36}{47}$?

Anſwer. 1 $\frac{17555}{19151}$.

3. If you are to add mixt Numbers, together, then add the Fractional Parts as before, and if their Sum be an improper Fraction, reduce it to a mixt Number, and add its integral Part to the integral Parts of the given mixt Numbers, and the Work is done.

Queſt 4. What is the Sum of 13 $\frac{3}{4}$ and 24 $\frac{5}{8}$?

First add the Fractions $\frac{3}{4}$ and $\frac{5}{8}$, the Sum is $\frac{12}{32}$, then add the Integer 1 13 and 2 $\frac{1}{1}$, their Sum is 38, and put after it the Fraction $\frac{42}{32}$ it is 3 $\frac{42}{32}$ for the Anſwer, or it is 38 $\frac{3}{8}$.

Queſt. 5. What is the Sum of 48 $\frac{3}{7}$, 64 $\frac{5}{8}$ and 13 $\frac{1}{4}$?

Facit 243 $\frac{110}{124}$, or 253 $\frac{45}{56}$.

4. If any of the Fractions to be added, is a Compound Fraction, it muſt firſt be reduced to a Simple Fraction by

the ſixth Rule of Chapter 19, and then add it to the re according to the ſecond Rule of this Chapter. *Examp*

Queſt. 6. What is the Sum of $\frac{3}{4}$, $\frac{5}{6}$ and $\frac{}{8}$ of $\frac{3}{4}$ of $\frac{5}{6}$?

Reduce $\frac{7}{8}$ of $\frac{3}{4}$ of $\frac{3}{5}$ into a ſimple Fraction, and it $\frac{105}{195}$, which reduced with the other two, and added, a $1\frac{4580}{3166}$.

Queſt. 7. What is the Sum of $\frac{1}{12}$ and $\frac{3}{4}$ of $\frac{4}{5}$ of $\frac{5}{6}$?

Anſwer. $1\frac{5}{12}$.

5. If the Fraction to be added are not of one Denomination, they muſt be ſo reduced, and then proceed before.

Queſt. 8. What is the Sum of $\frac{3}{4}$ *l.* and $\frac{5}{6}$ *s.*

Of the given Fractions here, one is of a Pound, and the other the Fraction of a Shilling; and before you can a them together, you muſt reduce $\frac{5}{6}$ *s.* to the Fraction of Pound as the other is (by the 8th Rule of Chap. 19.) a it makes $\frac{5}{120}$ *l.* then $\frac{3}{4}$ and $\frac{5}{120}$ *l.* will be found to be or $\frac{33}{48}$ *l.* by the 7th Rule of Chap, 19) and in its low Terms $\frac{19}{34}$ *l.* by the 4th Rule of Chap. 19.

It would have been the ſame (if by the latter Part the 8th Rule of Chapter 19.) you have reduced $\frac{3}{4}$ *l.* to Fraction of a Shilling, which you would have found have been $\frac{60}{4}$ *s.* which added to $\frac{5}{9}$ *s.* by the ſaid 17 Rule of the laſt Chapter, the Sum is 15 *s.* $\frac{20}{24}$ which equal to the Sum found, as before, *viz* $\frac{19}{24}$ *l.* for (by 5th Rule of Chapter 12,) the Value of $\frac{16}{24}$ *l.* will be fou to be 15 *s.* 10 *d.* and ſo will 15 *s*, $\frac{20}{24}$ be found to be j as much.

Queſt. 9. What is the Sum $\frac{3}{4}$ *l.* $\frac{3}{5}$ *s.* and $\frac{3}{5}$ *d*?

Anſwer. $\frac{37500}{40000}$ or $\frac{3795}{9000}$ *l.* or in its loweſt Terms

CHAP. XXI.

Subtraction of Vulgar Fractions.

1. THE Rules in Addition for reducing the gi Fractions to one Denomination, are here to be ſerved; for before Subtraction can be made, the Fracti muſt be reduced to a cmomon Denominator, then ſubtr one Numerator for the other and place the Remain over a common Denominator, which Fraction ſhall be

Exceſs or Difference between the given Fractions. Examples.

Queſt. 1. What is the Difference between $\frac{3}{4}$ and $\frac{5}{8}$? The given Fractions are reduced to $\frac{21}{28}$, and $\frac{20}{28}$, then ſubtract the Numerator 20 from the Numerator 21, and there remains 1, which being put over the Denominator 28, makes $\frac{1}{28}$ for the Anſwer or Difference between $\frac{3}{4}$ and $\frac{5}{8}$.

Queſt. 2. What is the Difference between $\frac{5}{6}$ and $\frac{5}{8}$ of $\frac{3}{4}$? Reduce the Compound Fraction $\frac{3}{4}$ of $\frac{5}{8}$ to a ſimple Fraction, then proceed as before, and the Anſwer is $\frac{110}{14}$ equal to $\frac{12}{24}$.

2. When a Fraction is given to be ſubtracted from a whole Number, ſubtract the Numerator from the Denominator, and put the Remainder for a Numerator to the given Denominator, and ſubtract an Unit (for that you borrowed) for the whole Number, and the Remainder place before the Fraction found, as before, which mixed Number is the Remainder or Difference ſought. Example.

Queſt. 3. Subtract $\frac{7}{10}$ from 48?

Anſwer, 37 $\frac{3}{10}$; for if you ſubtract 7 (the Numerator) from 10 (the Denominator) there remains 3, which put over is $10\frac{3}{80}$, and it makes $47\frac{3}{10}$ for the Exceſs.

Queſt. 4. Subtract $\frac{13}{18}$ from 47, remain in $56\frac{5}{18}$.

3. If it be required to ſubtract a Fraction from a mixt Number, or one mixt Number from anoother, reduce the Fractions to a common Denominanator, and if the Fraction to be ſubtracted be leſſer than the other, then ſubtract the leſſer Numerator from the greater and that is a Numerator for the common Denominator; then ſubtract the leſſer integral Part from the greater, and the Remainder with the remaining Fractions thereunto annexed, is the Difference required between the two given mixt Numbers. Example.

Queſt. 5. Subtract $26\frac{3}{7}$ from $54\frac{5}{6}$.

Firſt, Subtract $\frac{3}{7}$, *viz.* $\frac{18}{41}$ from $\frac{3}{2}$. *viz.* $\frac{35}{42}$, the Remainder is $\frac{17}{42}$, then 20 from 44, remaineth 28, to which annex $\frac{14}{42}$ it makes $28\frac{18}{42}$ for the Anſwer.

4. But if the Fraction to be ſubtracted is greater than the Fraction from whence you ſubtract, then having firſt reduced the Fractions to a common Denominator, take the Numerator of the greateſt Fraction out of the Denominator,

and add the Remainder to the Numerator of the leſſer Fraction, and their Sum is a new Numerator to the common Denominator, which Fraction Note, then (for the one you borrowed) add one to the integral Part to be ſubtracted and ſubtract it from the greater Number, and to the Remainder annex the Fraction you noted before, ſo this new mixt Number ſhall be the Difference ſought. *Example.*

Queſt. 6. Subtract $14\frac{3}{4}$ from $29\frac{4}{7}$.

The Fraction, reduced are, *viz* $\frac{3}{4}$ equal to $\frac{21}{28}$. and equal to $\frac{16}{28}$, now I ſhould ſubtract $\frac{21}{28}$ from $\frac{16}{28}$, but I cannot, therefore I ſubtract 21 from 28, reſt 7, which added to 16 (the leſſer Numerator) make 23 for a Numerator to 28, *viz* $\frac{23}{28}$; then I come to the integral Parts 14 and 29 and ſay, 1 that I borrowed and 14 is 15, which taken from 29, there reſts 14, to which annexing $\frac{23}{28}$ it is $14\frac{23}{28}$, for the Remainder or Difference between $14\frac{3}{4}$ and $29\frac{4}{7}$.

Queſt. 7. Subtract $36\frac{9}{10}$ from $74\frac{4}{9}$? *Facit*, $37\frac{49}{90}$.

CHAP. XXII.

Multiplication Vulgar Fractions.

1. IF the Multiplicand and Multiplier are ſimple Fractions, then multiply the Numerators together for a new Numerator, and the Denominators for a new Denominator, and the new Fraction is the Product required.

Queſt. 1. What is the Product of $\frac{5}{7}$ by $\frac{9}{11}$? *Facit* $\frac{45}{77}$, for the Numerators 5 and 9 being multiply'd, make 45, and the Denominators 7 and 11 being multiply'd make 77.

Queſt. 2. What is the Product of $\frac{8}{25}$ by $\frac{21}{31}$? *Facit*

2. If the Fractions to be multiplied be mixt Numbers reduce them to improper Fractions by the firſt Rule of the 19th Chapter; then proceed as before.

Queſt. 3. What is the Product of $28\frac{3}{5}$ by $13\frac{5}{6}$?

The given mixt Numbers being reduced to improper Fractions are $48\frac{3}{5}$ equal to $\frac{243}{5}$ and $13\frac{5}{6}$ equal to $\frac{13}{6}$, now $\frac{243}{5}$ multiplied by $\frac{3}{6}$ according to the firſt Rule of this Chapter, produceth $\frac{20169}{205}$, or $972\frac{29}{75}$.

Queſt. 4. What is the Product of $430\frac{7}{10}$ by $18\frac{3}{7}$? *Facit* $45\frac{14}{72}$, or $703\frac{64}{70}$.

3. If a Compound Fraction is to be multiplied by a Sim-

ple Fraction, firſt reduce the Compound Fraction into a Simple Fraction, then multiply the one by the other, as is taught above.

Queſt. 5. What is the Product of $\frac{16}{21}$ by $\frac{3}{4}$ of $\frac{5}{7}$ of $\frac{6}{5}$?

The Compound Fraction $\frac{3}{4}$ of $\frac{7}{5}$ of $\frac{4}{5}$ reduced is $\frac{80}{140}$, or $\frac{6}{14}$ which multiply by $\frac{16}{21}$ produceth $\frac{96}{294}$, which in its loweſt Term is $\frac{19}{49}$ for the Anſwer.

And if the Multiplicand and Multiplier are both Compound Fractions, reduce them both to Simple ones, then multiply theſe few Fractions as before, ſo you have the Product.

Queſt. 6. What is the Product of $\frac{3}{4}$ of $\frac{1}{2}$ of $\frac{1}{2}$?

Anſwer. $\frac{18}{120}$ in its loweſt Term $\frac{3}{20}$.

Queſt. 7. What is the Product of $\frac{3}{5}$ of $\frac{5}{4}$ by $\frac{3}{4}$ of $\frac{5}{8}$?

Anſwer. $\frac{60}{360}$, or $\frac{6}{36}$, or in its leaſt Terms $\frac{1}{6}$.

4. If a Fraction to be multiplied by a whole Number, put under the given whole Number an Unit for a Denominator, whereby it will be an improper Fraction, then multiply the Fractions as before. *Example.*

Queſt. 8. What is the Product of 24 by $\frac{2}{3}$?

Anſwer. $\frac{48}{3}$, for 24 by putting an Unit under it, will be $\frac{24}{1}$, and $\frac{24}{1}$ by $\frac{2}{3}$ produceth $\frac{48}{3}$ or 16.

Queſt. 9. What is the Product of 36 by $\frac{9}{11}$?

Anſwer. $\frac{324}{11}$ or 29 $\frac{5}{11}$.

CHAP. XXIII.

Diviſon of Vulgar Fractions.

1. IF the Dividend and the Diviſor are both ſimple Fractions, then multiply the Numerator of the Dividend into the Denominator of the Diviſor, and the Product is a new Numerator, and multiply the Denominator of the Dividend into the Numerator of the Diviſor, and the Product is a new Denominator, which new Fraction thus found is the Quotient you deſire. *Example.*

Queſt. 1. What is the Quotient of $\frac{5}{8}$ divided by $\frac{3}{5}$?

Anſwer. $\frac{24}{25}$ or 1 $\frac{1}{24}$, for the firſt I multiply (5) the Numerator of the Dividend into (5) the Denominator of the Diviſor, and the Product (25) is a Numerator for the Quotient, then I multiply (8) the De-

$$\frac{3}{5}\Big)\frac{5}{8}\Big(\frac{25}{34}$$

Denominator of the Dividend, into (3) the Numerator of the Diviſor, and the Product (24) I put in the Quotient for Denominator, ſo I find $\frac{23}{24}$ is the Quotient ſought.

Queſt. 3. What is the Quotient of $\frac{10}{21}$ divided by $\frac{2}{3}$?

Anſw. $\frac{30}{42}$ equal to $\frac{5}{7}$ in its loweſt Terms.

2. But if you will divide a ſimple Fraction by a Compound, or a Compound by a Simple, firſt reduce ſuch Compound to a Fraction, then go on as before.

Queſt. 3. What is the Quotient of $\frac{3}{10}$ divided by $\frac{3}{4}$ of $\frac{2}{3}$?

Anſwer $\frac{36}{60}$ or $\frac{3}{5}$ firſt reduce $\frac{3}{4}$ of $\frac{2}{3}$ into a ſimple Fraction, and it is $\frac{6}{12}$, by which $\frac{3}{10}$ being divided, the Quotient is $\frac{36}{60}$ equal in its leaſt Terms to $\frac{3}{5}$ and if the Dividend and Diviſor be both of Compound Fractions, reduce them both to a ſimple Fraction, then divide the one by the other, as in Rule 1. foregoing.

Queſt. 4. What is the Quote of $\frac{2}{3}$ of $\frac{4}{4}$ divided by $\frac{1}{2}$ of $\frac{5}{8}$?

Anſwer $\frac{120}{80}$ or $\frac{18}{12}$, or $1\frac{6}{12}$, or $1\frac{1}{2}$ in its loweſt Terms.

3. If the Dividend, or Diviſor, or both, are mixed, Numbers, reduce them to improper Fractions, and perform Diviſion as you are taught before.

Queſt. 5. What is the Quote of $12\frac{3}{4}$ divided by $21\frac{4}{5}$?

Anſwer $\frac{255}{436}$ for $12\frac{3}{4}$ is equal to $\frac{51}{4}$. and $21\frac{4}{5}$ is equal to $\frac{109}{5}$, and the Quote of $\frac{51}{4}$ divided by $\frac{109}{5}$, is as before $\frac{255}{436}$.

4. If you divide a Fraction by a whole Number, or a whole Number by a Fraction, make the whole Number an improper Fraction, by putting an Unit for a Denominator to it, as was taught in Rule 4. Chap 22. and then perform Diviſion as was before taught.

Example.

Queſt. 6. What is the Quote of 8 divided by $\frac{3}{5}$?

Anſwer $\frac{40}{3}$, which is equal to $13\frac{1}{3}$, being reduced as is before directed. See the Work in the Margent.

$$\frac{5}{}\Bigg)\frac{8}{1}\Bigg(\frac{40}{3} \text{ or } 13\tfrac{1}{3}$$

Queſt. 7. What is the Quotient of $\frac{3}{5}$ divided by 8?

Anſwer. $\frac{3}{40}$ as *per* Margent.

$$\frac{8}{1}\Bigg)\frac{3}{5}\Bigg(\frac{3}{40}$$

CHAP

CHAP. XXIV.

The Rule of Three Direct in Vulgar Fractions.

AS in the Rule of Three in Whole Numbers, ſo likewiſe in Fractions, you muſt ſee that the Fractions the firſt and third Places be of the ſame Denomination.

2. If any of the given Fractions be compound, let them reduced to ſimple of the ſame Value.

3. If there are given mixed Numbers, reduce them to proper Fractions by the firſt Rule of Chap. XIX.

4. If any of the Terms is a whole Number, make an improper Fraction by conſtituting an Unit for its Deominator.

Having reduced your Fraction as is directed in the 4 laſt ules, then proceed to a Reſolution, which is performed he ſame Way as in whole Numbers. Reſpect being had to he Rules delivered for the working of Fractions, *viz.* ultiply the 2d and 3d Fractions together, according to the rſt Rule of Chap. XXII. and divide the Product by he firſt Fraction, according to the firſt Rule of Chap. XIII. and the Quotient is the Anſwer.

Or, (which is better)

5. Multiply the Numerator of the firſt Fraction into the enominator of the ſecond and third, and the Product is a ew Denominator; then multiply the Denominator of the rſt Fraction into the Numerator of the 2d and 3d, and the roduct is a new Numerator, which new Fraction is the h Proportional or Anſwer, which (if it be an improper raction) muſt be reduced to a whole or mixed Number by he 3d Rule of Chap. XIX. *Example.*

Queſt. 1. If $\frac{3}{4}$ Yards of Cloth coſt $\frac{5}{8}$ *l.* what will $\frac{7}{10}$ Yards coſt?

Having placed the given Fractions according to the 6th Rule of Chap. X. I proceed to the Reſolution, and firſt multiply the Numerator of the firſt Fraction (3) into 8 and 10, the Denominators of the ſecond and third Fracions, and the Product is 240 for a Denominator; then multiply 4 the *Denominator* of the firſt Fraction into 5 and 2, the Numerators of the ſecond and third Fractions, the Product is 182 for a Numerator, which Numerator 180, and Denominator 240 make $\frac{180}{240}$ *l.* for the Anſwer, equal to $\frac{3}{4}$ or 15 *s.*

$$\begin{array}{cccc} \text{yards} & l. & \text{Yards} & l. \\ \frac{3}{4} & \frac{5}{8} & \frac{9}{10} & \frac{180}{240} \end{array}$$

$$\textit{Facit}, \quad \overset{l.}{\frac{180}{240}} \text{ equal to } \frac{3}{4}$$

Queſt. 2. If $\frac{2}{3}$ *l.* buy $\frac{5}{6}$ Yards of Cloth, what will $\frac{11}{12}$ Yds coſt at that Rate?

Anſwer, kkk l. equal to $\frac{21}{25}$ *l.* or 14 *s.* 8 *d.*

Queſt. 3. If $\frac{7}{8}$ *l.* coſt $\frac{3}{4}$ *s.* what will $\frac{8}{9}$ *s.* buy?

Anſwer, $\frac{224}{216}$ *l.* equal to 1 $\frac{21}{27}$ *l.*

Queſt. 4. If $\frac{3}{5}$ of an Ell of Holland coſt h of a Pound, how much will 12 h Ells coſt at that Rate?

Anſwer, $\frac{120}{27}$ equal to 7 $\frac{1}{37}$ *l.*

In reſolving the laſt Queſtion and the two next, obſerve the 3d Rule of the Chapter foregoing.

Queſt. 5. If $\frac{9}{78}$ of a *C.* coſt 284 *s.* what will 7 $\frac{1}{2}$ *C.* coſt at that Rate?

Anſwer, 239 $\frac{7}{17}$ *s.* or 11 *l.* 19 *s.* 7 *d.*

Queſt. 6. If 3 $\frac{1}{4}$ Yards of Velvet coſt 3 $\frac{5}{8}$ *l.* how much will 10 $\frac{1}{2}$ Yards coſt at that Rate?

Anſwer, 11 $\frac{3}{5}$ *l.*

Queſt. 7. If five Yards of Broad cloth coſt 2$\frac{3}{4}$ *l.* what will 14$\frac{3}{4}$ Yards coſt?

Anſwer, 13 *l.* 9 *s.* 4 *d.*

In working the laſt Queſtion, and the four next, obſerve the 4th Rule of the Chapter foregoing.

Queſt. 8. If 14 *l.* of Pepper coſt 14 *s.* 6 $\frac{3}{5}$ *d.* I demand the Price of 73 $\frac{3}{4}$ *l.*

Anſwer, 3 *l.* 16 *s.* 7$\frac{43}{36}$ *d.*

Queſt. 9. If 1 *l.* of Cochineel coſt 1 *l.* 5 *s.* what will 36 $_{12}$ *l.* coſt?

Anſwer, 47 *l.* 17 *s.* 6 *d.*

Queſt. 10. If a Yard of Broad-cloth coſt 15 $\frac{5}{8}$ *s.* what will four Pieces, each containing 27$\frac{3}{8}$ Yards coſt at that Rate?

Anſwer, 85 *l.* 14 *s.* 3$\frac{2}{7}$ *d.*

Queſt. 11. A Mercer bought $3\frac{1}{2}$ Pieces of *Silk*, each Piece contained $24\frac{2}{3}$ Ells, at 6 *s.* 2 *d. per* Ell; I demand the Value of $3\frac{1}{2}$ Pieces at that Rate?

Anſwer, 26 *l.* 3 . $4\frac{3}{4}$ *d.*

In reſolving the four next Queſtions, obſerve the 8th Rule of Chap 19.

Queſt. 12. If $\frac{2}{5}$ of an Ounce of Silver coſt 2 *s.* I demand the Price of $11\frac{2}{8}$ *l.* at that rate?

Anſwer. 35 *l.*

Queſt. 13. If $1\frac{5}{7}$ *l.* of Gold is worth $61\frac{5}{7}$ *l.* Sterling what is a Grain worth at that rate?

Anſwer. $1\frac{1}{2}$ *d.*

Queſt. 14. If $\frac{2}{3}$ Yards of Silk is worth $\frac{3}{4}$ of $\frac{5}{8}$ *l.* what is the Price of $15\frac{2}{9}$ Ells Flemiſh?

Anſwer. 9 *l.* 12 *s.* 6 *d.*

Queſt. 15. If $\frac{2}{3}$ of $\frac{3}{4}$ of a Pound of Cloves coſt 6 *s.* $2\frac{2}{7}$ *d.* what coſt the C. weight at that rate?

Anſwer. 69 *l.* 6 *s.* 8 *d.*

Note, That when the Anſwer to the Queſtion in this and the next Chapter are given in Fractions, they are given in their loweſt Terms,

CHAP. XXV.

The Rule of Three Inverſe in Fractions.

1. IT hath been already taught (in the 3d Rule of the 11th Chapter) how to diſcover when the 4th proportional Number (to the three given Numbers) is to be found out by a *Rule of Three Direct*, and when by a *Rule of Three Inverſe*; to which Rule the Learner is now inſered.

2. When (in Fractions) you find a Queſtion to be reſolved by the *Rule of Three Inverſe, viz.* when the third Term is the Diviſor, then having reduced the Terms exactly) according to the Rules in Chap. 24.) multiply the Numerators of the three Fractions into the Denominators of the 2d and 1ſt Fractions, and the Product is a new Denominator; then multiply the Denominator of the 3d Fraction into the Numerators of the 2d and 1ſt Fractions, and the Product is a new Numerator, which new Fraction thus found, is the Anſwer to the Queſtion.

Queſt. 1. If $\frac{3}{4}$ of a Yard of Cloth that is two Yards wide, will make a Garment, how much of any other Drapery that is $\frac{3}{5}$ of a Yard wide will make the ſame Garment?

Anſwer, $2\frac{1}{2}$ Yards.

Queſt. 2. I lent my Friend 46 *l.* for $\frac{4}{5}$ of a Year, how much ought he to lend me for $\frac{7}{12}$ Parts of a Year;

Anſwer, $63\frac{3}{35}$ *l.*

Queſt. 3. If $\frac{2}{3}$ of a Yard of Cloth that is $2\frac{1}{2}$ Yards wide will make any Garment, what Breadth is that Cloth when $1\frac{3}{4}$ Yard will make the ſame Garment?

Anſwer, $\frac{57}{63}$ of a Yard wide.

Queſt. 4 How many Inches in Length of a Board that is 9 Inches broad, will make a Foot Square?

Anſwer, 16 Inches in Length.

Queſt. 5. If when the Buſhel of Wheat coſt 4 *s.* $\frac{3}{4}$, the Penny-loaf weighed $10\frac{2}{3}$ Ounces, what will it weigh when the Buſhel coſt 8 *s.* $\frac{9}{10}$?

Anſwer, $5\frac{185}{265}$ Ounces,

Queſt. 6. It 17 Men can mow $24\frac{1}{2}$ Acres in $10\frac{2}{3}$ Days, in how many Days will ſix Men do the ſame?

Anſwer, In $21\frac{1}{3}$ Days.

CHAP. XXVI.

Rules of Practice.

1. IN the ſingle Rule of Three, when the firſt of the 3 Numbers in the Queſtion (after they are diſpoſed according to the ſixth Rule of Chapter 10,) happeneth to be an Unit (or 1) that Queſtion many Times may be reſolved far more ſpeedily than by the Rule of Three, which kind of Operation is commonly called *Paradice*, and indeed it is of excellent Uſe among Merchants, Tradeſmen, and others, by Reaſon of its Speedineſs in finding a Reſolution to ſuch Kind of Queſtions.

2. The chiefeſt Queſtions reſolvable by theſe chief Rules, may be comprehended under the three general Heads or Caſes following, *viz.*

When the given Price of the Integer conſiſts

1 Of Farthings under 4.
2 Of Pence under 12.
3 Of Pence and Farthings.
4 Of Shillings under 20.
5 Of Shillings, Pence, and Farthings.
6 Of Pounds.
7 Of Pounds, Shillings, Pence, and Farth.

It would be very convenient for the Practical Arithmetician to have by Heart the ſeveral Products of the 9 Digits multiplied by 12, for his ſpeedy reducing Pence into Shillings and Shillings into Pence, which he may gain by the following Table.

	1		12
	2		24
	3		36
	4		48
12 Times	5	is	60
	6		72
	7		84
	8		96
	9		108

3. Shillings are practically reduced into Pounds, thus viz. Cut off the Figure ſtanding in the Place of Units with a Daſh of the Pen, and note it for Shillings; then draw a Line under the given Number, and take half the remaining Figures (after the firſt is cut off) and ſet them under the Line, and they are ſo many Pounds; but if the laſt Figure is odd, then take the leſſer half, and add 10 to the Figure ſo cut off (as before) for Shillings; as if I were to reduce 43658 Shillings into Pounds, firſt I cut off the laſt Figure (8) for Shillings, then I take half of the remaining Figures (4365) thus, half of 4 is 2, which I put under the Line, then half of 3 is 1, and becauſe 3 is an odd Number, I make the next Figure 6 to be 16, and I go on, ſaying, half of 16 is 8, then half of 5 is 2, which is the laſt Figure, wherefore becauſe 5 is an odd Number, I add 10 to the 8 I cut off, and it makes 18 *s.* ſo that I find it to be 2182 *l.* 18 *s.* as *per* Margent.

4365|8	
l.	*s.*
2182	18

4. It is likewiſe convenient that the Learner be acquainted with the Pratical Tables following, the firſt containing the Aliquot or even Parts of a Shilling, the 2d containing the Aliquot Parts of a Pound.

The even Part of a Shilling.	is
6	$\frac{1}{2}$
4	$\frac{1}{3}$
3	$\frac{1}{4}$
2	$\frac{1}{6}$
$1\frac{1}{2}$	$\frac{1}{8}$
1	$\frac{1}{12}$

The even Parts of a Pound.		is *l.*
10	00	$\frac{1}{2}$
6	08	$\frac{1}{3}$
5	00	$\frac{1}{4}$
4	00	$\frac{1}{5}$
3	04	$\frac{1}{6}$
2	06	$\frac{1}{8}$
2	00	$\frac{1}{10}$
1	08	$\frac{1}{12}$
1	00	$\frac{1}{20}$

Caſe 1.

5. When the Price of an Integar is a Farthing, then take the 6th Part of the given Number, which will be ſo many Three-half-pences, and if any Thing remain it is Farthings, by the 7th Rule of Chap. 9. then conſider that Three-half-pence is $\frac{1}{8}$ of a Shilling, wherefore take the 8th Part of them for Shillings, and if any Thing remain, they are ſo many Three-half-pences, which reduce into Pounds by the third Rule forgoing. *Example,* What comes 67486 *l.* to, at a Farthing *per l*? Firſt, I take $\frac{1}{6}$ of 67486, and it is 11247 Three-half-pences and four Farthings, or 1 Penny, then $\frac{1}{8}$ of 11247 is 1405 *s.* and ſeven remains, which is ſeven Three half-pences, or 10 $\frac{1}{2}$ *d.* which with the four Farthings before, make 11 $\frac{1}{2}$ *d.* and 1405 *s.* which by the third Rule is 70 *l.* 5 *s.* In all 70 *l.* 5 *s.* 11 *d.* for the Anſwer. See the Work following.

$\frac{1}{6}$	67486 at $\frac{1}{4}$ *per l.*	
		d.
$\frac{1}{8}$	11247	1
$\frac{1}{20}$	140|5	10 $\frac{1}{2}$
	l.—*s.*—*d.*	
	70 4 11 $\frac{1}{2}$ *Facit.*	

Other Examples follow.

1/8	8576 *l.* at 1 *qr.*	1/3	8347 *l.* at 1 *qr.*
1/8	1072 2 *qrs.*	1/8	1063 2 *qrs.*
1/20	176|8 8 *d.*	1/20	13|2 11 *d.*
	l. *s.* *d.*		*l.* *s.* *d.*
	88 8 8 *Facit*		6 12 11 *Facit.*

6. When the Price of the Integer is 2 Farthings, then take the third Part of the given Number, for ſo many Three-half-pence, and the Remainder if any, is Half-pence, then take the Eight Part of that for Shillings, as before, *&c.*

Example.

1/3	7386 *l.* at 2 *qrs.*	1/3	8347 *l.* at 2 *qrs.*
1/8	2456	1/8	2782 2 *qrs.*
1/20	0|7	1/20	34|7 9 *d.* 1/2
	l. *s.*		*l.* *s.* *d* *Facit.*
	15 7		17 7 9 1/2

7. When the Price of the Integer is 3 Farthings, then take half the given Number for Threehalf pence, and if any Thing remain it is 3 Farthings, then take the 8th for Shillings, as before, *&c.*

1/2	4726 *l.* at 5 *qrs.*	1/2	5425 *l.* at 3 *qrs.*
1/8	2368	1/8	2712 3 *qrs.*
1/20	29|6	1/20	33|9
	l. *s.*		*l.* *s.* *d.* *qrs.*
	14 16 *Facit*		16 19 0 3 *Facit.*

Caſe 2.

8. When the given Price of the Integer, is a Part or Parts of a Shilling, (*viz.* Pence) divide the given Number of Integers, (whoſe Vaule is ſought) by the Denomination of the Fraction, repreſenting the even Part, and the Quote is Shillings (always minding the 7th

Rule of the 9th Chapter) and thoſe Shillings may be reduced into Pounds by the third Rule of this Chapter. Example: Let it be required to find the Value of 438 *l.* at 3 *d. per l.* I conſider 3 *d.* is $\frac{1}{4}$ of a Shilling, and 438 *l.* will coſt ſo many 3 Pences, wherefore I divide 438 by 4 the Denominator or $\frac{1}{4}$, and the Quote is 109 Shillings, and two remains, which is two 3 *d.* or 6 *d.* the whole Value is 5 *l.* 9 *s.* 6 *d.* as by the following Work appeareth.

$\frac{1}{4}$	438 *l.* at 3 *d.*
$\frac{1}{20}$	10|9—6

l. *s.* *d.*
Facit 5 9 6

If the Learner is minded to try the Fruitfulneſs of his Genius, he may frame as many Examples as he thinks fit, and work them as before.

9. If the Price of the Integer be Pence under 12, and yet not an even Part, then it may be divided into even Parts, and ſo the Parts of the given Numbers taken accordingly, and add together, as if it were 5 *d.* which is 3 *d.* and 2 *d.* *viz.* $\frac{1}{4}$ and $\frac{1}{6}$ of a Shilling, firſt take $\frac{1}{4}$ of the given Number, and then $\frac{1}{6}$ thereof, and add them together, and their Sum is the Anſwer in Shillings, ſtill obſerving Rule 7 of Chapter 9, for the Remainder, (if any be) then bring the Shillings into Pounds by the third Rule foregoing. Likewiſe 7 *d.* is $\frac{1}{3}$ and $\frac{1}{4}$, ſo 9 *d.* is $\frac{1}{2}$ and $\frac{1}{4}$, and 10 *d.* is $\frac{1}{2}$ and $\frac{1}{3}$, and 11 *d.* is $\frac{1}{4}$ and $\frac{2}{3}$ of a Shillings; or elſe many Times your work may be ſhortned thus, *viz.* when the ſaid given Price it to be divided into even Parts of a Shilling, or of a Pound, after you have taken the firſt even Part, the other may be an even Part of that Part, as in the next Example, where are given 439 *l.* at 5 *d. per l.* now I may divide it thus, *viz.* into 4 *d.* and 1 *d.* and 4 *d.* being $\frac{1}{3}$ of a Shilling, and 1 *d.* being $\frac{1}{4}$ of 4 *d.* I firſt take $\frac{1}{3}$ of 439 *l.* and it gives 146 *s.* 4 *d.* and for the 1 *d.* I take $\frac{1}{4}$ of 146 *s.* 4 *d.* which is 36 *s.* 7 *d.* which in all comes to 9 *l.* 2 *s.* 11 *d.* Examples follow.

L.

	l.	*s.*
	439 at	5 *per l.*
1/3	146	4
1/4	36	7
	18|2	11
	9 *l.* 2 *s.* 11 *d. Facit*	

	Ells	*d.*
	587 at	7 *per Ell*
1/3	195	8
1/4	146	9
	34|2	5
	17 *l.* 2 *s.* 5 *d. Facit*	

	yds	*d.*
	836 at	8 *per yd.*
1/3	278	8
1/3	278	8
	65|7	4
	32 *l.* 17 *s.* 4 *d. Facit*	

	yds	*d.*
	417 at	9 *per yd.*
1/2	201	6
	104	3
1/20	31|2	9
	15 *l.* 12 *s.* 9 *d. Facit*	

	Ells	*d.*
1/2	386 at	10
1/3	193	
	128	8
	32|1	8
	16 *l.* 01 *s.* 8 *d. Facit*	

	l.	*d.*
	534 at	11
1/2	178	
1/3	178	
1/4	133	6
	48|9	6
	24 *l.* 9 *s.* 6 *d. Facit*	

10. When the Price of the Integar is Pence and Farthings, if it make an even Part of a Shilling, work as before; but if they are uneven, as Penny Farthing, Penny three Farthings, 2 *d.* 1 *qr.* or 2 *d.* 3 *qrs.* 1 *d.* 3 *qrs.* or the like, then first Work for ſome even Part, and then conſider what Part the reſt is of that even Part, and divide that Quotient thereby, then add them together,

and reduce them to Pounds as before. *Example.* 3470 *l.* at 1 *d.* 1 *qr. per l.* firſt I work for the Penny by dividing 3470 *l.* by 12, for 1 *d.* is $\frac{1}{12}$ of a Shilling, and the Quote is 289 *s.* 2 *d.* then I conceive that one Farthing is the $\frac{1}{4}$ of a Penny, and the Value of one Farthing will be $\frac{1}{4}$ of the Value of a Penny, and therefore I take $\frac{1}{4}$ of 289 *s.* 2 *d.* which is 72 *s.* 3 *d.* 2 *qrs.* and add them together, and they are 18 *l.* 1 *s.* 5 *d.* 2 *qrs.* as by the Margent.

	l.		*d.*	*qrs.*
	3470	at	1	1
$\frac{1}{4}$	289		2	
	72		3	
$\frac{1}{20}$	36|1		3	$\frac{1}{2}$
	l.	*s.*	*d.*	*qrs.*
	18	1	5	2

Caſe 4.

11. When the Price of the Integer is 2 *s.* then cut off the Figure in the Place of Units of the given Number, and double it for Shillings, and the Figure on the other Hand are Pounds. *Example.* 436 Yards at 2 *s. per* Yard, cut off the laſt Figure 6 and double it, makes 12 *s.* and the other two Figures, *viz.* 43, are ſo many Pounds; ſo that their Value is 43 *l.* 12 *s.* as *per* Margent.

43|6

43 *l.* 12 *s.*

12. Hence it is evident that when the given Price of an Integer is an even Number of Shillings, then if you take half of that (even) Number of Shillings, and multiply the given Number of Integers thereby, doubling the firſt Figure of the Product, and ſetting it apart for Shillings, the reſt of the Product will be Pounds, which Pounds and Shillings are the Value ſought. *Example.* What coſt 536 Yards at 8 *s. per* Yard? To reſolve which, I take Half of 8 *s.* (the Price of a Yard) which is 4, and multiply 536 thereby, ſaying, 4 Times 6 is 24, then I double the firſt Figure 4 makes 8 for Shillings and carry 2 to the next Product, *&c.* I find the reſt of the Product to be 214 which I note for Pounds; ſo that the Value of 536 Yards at 8 *s. per* Yard, is 214 *l.* 8 *s.* as by the Margent. Other Examples of the ſame Kind may be wrought after the ſame Manner.

536 *Yds at* 8

214 *l.* 8 *s.*

13. If the given Price of the Integer is an odd Number of Shillings, then work firſt for the even Number

of Shillings by the laſt Rule, and for the odd Shilling take $\frac{1}{20}$ of the given Number of Integers, according to the 3d Rule of this Chapter, and add them together, and you have your Deſire. *Examples* follow.

Yds	*s.*	*Ells*	*s.*
422 at	3 *per* Yard	431 at	13
l.	*s.*	*l.*	*s.*
42	4	258	12
21	2	21	11
63	6 *facit*	280	03 *facit*

Ells	*s.*	*Ells*	*s.*
516 at	7 *per* Ell	324 at	17 *per* Ell
l.	*s.*	*l.*	*s.*
154	16	259	04
25	16	16	04
180	12 *facit*	275	08 *facit*

14. Except when the given Price of the Integer is 5 *s.* for then it is ſooner anſwered by taking ¼ of the given Number, whoſe Value is ſought, as in the following Example.

	yds. *s.*		*Ells* *s.*
¼	436 at *per* Yard	¼	206 at 5 *per* Ell
	109 *l.* *Facit*		51 *l.* 10 *s.* *Facit.*

Caſe 5.

15. When the given Price of an Integer is Shillings and Pence, or Shillings, Pence and Farthings; then divide the given Number of Integers whoſe Value you ſeek by the Denominator of that Fraction repreſenting that even Part. As for Example, What is the Price of 384 yards at 6 *s.* 8 *d.* *per* Yard? Here I conſider that 6 *s.* 8 *d.* is ⅓ of a Pound, wherefore divide 384 by 3, and the Quote is the Anſwer, *viz.* 128 *l.* ſo that 384 yards at 6 *s.* 8 *d.* per yard, amounts to 128 *l.* as *per* Margent, ſtill obſerving the 7th Rule of the 9th Chapter.

⅓	384
	128 *l* *fa.*

16. When the given Value of the Integer is Shillings

and Pence, and not an even Part of a Pound, yet many times it may be divided into Parts, (*viz.* 6 *s.* 6 *d.* is 4 *s.* and 2 *s.* 6 *d.*) for the 4 *s.* Work according to the 12th Rule foregoing, and for the 2 *s.* 6 *d.* take the eighth Part of the given Number, and add them together, then their Sum is the Value required.

So 8 *s.* 6 *d.* will be divided into 6 *s.* and 2 *s.* 6 *d.* and the Price of the given Number may be found out as before, *&c.* Examples follow.

	yds.		*s.*	*d.*
	386	at	8	8
1/2	128 *l.*		13	4
1/10	38		12	0
	167 *l.* 5 *s.* 4 *d.* *Facit*			

	Ells		*s.*	*d.*
s.	427	at	8	6
	128 *l.*		2	6
	53		7	
	181 *l.* 9 *s.* 6 *Facit*			

	Ells		*s.*	*d.*
s.	240	at	5	4
2	54		0	
1/6	40		0	
	64 *l.* *Facit*			

	yds		*s.*	*d.*
s.	386	at	14	8
8	154 *l.*		8	0
1/2	128		13	4
	283 *l.*		01	4 *Facit*

17. When the given Price of an Integer is Shillings and Pence, and you cannot readily divide them according to the laſt Rule, then multiply the given Number whoſe Value you ſeek, by the Number of Shillings in the Price of the Integer, and then for the Pence work by the 8th Rule foregoing; then add the Numbers together, and their Sum is their Value ſought in Shillings; as for Example. What is the Value of 392 Yards at 6 *s.* 9 *d.* *per* Yard. Here 6 *s.* 9 *d.* cannot be made an even Part, nor indeed can it be divided into even Parts of a Pound; wherefore I multiply the given Number of Yards 322 by 6 for the 6 *s.* the Product is 2353 *s.* then for the 9 *d.* I divide it into 6 *d.* and 3 *d.* and work for them by the 8th Rule foregoing, and at laſt add the Shillings together, they make 2646 *s.* and by the 3d they are reduced to 132 *l.* 6 *s.* the Value of 92 Yards at 6 *s.* 9 *d.* *per* yard. See the Work.

—392 *yds* at 6 *s.* 9 *d.*

2352
$\frac{1}{2}$ 196
$\frac{1}{4}$ 98

264|6

132 *l.* 6 *s.* *Facit*

In like manner Variety of other Examples be wrought.

18. When the given Price of the Integer is Shillings, Pence, and Farthings, then multiply the given Number of Integers, by the Number of Shillings contained in the Value of the Integer, and for the Pence and Farthings follow the 10th Rule of this Chapter.

Example.

Ells *s.* *d.*
438 at 8 6 $\frac{3}{4}$

s.
8 3504
$\frac{1}{2}$ 219
$\frac{1}{8}$ 27 4 *d.* $\frac{1}{2}$

375|0 4 $\frac{1}{2}$

Fac. 187 *l.* 10 *s.* 4 *d.* $\frac{1}{2}$

Ells *s.* *d.*
139 at 9 2 $\frac{1}{2}$

s.
9 1215 0
$\frac{1}{8}$ 23 2
$\frac{1}{4}$ 5 9 $\frac{1}{2}$

125|0 4

Fac. 63 *l.* 19 *s.* 11 *d.* $\frac{1}{2}$

Ells *s.* *d.*
370 at 24 2 $\frac{3}{4}$

480
s. 370

14 3180 *d.*
$\frac{1}{4}$ 61 8
$\frac{1}{4}$ 15 5
$\frac{1}{4}$ 7 8

526|4 9 $\frac{1}{2}$

Fac. 263 *l.* 4 *s.* 9 *d.* $\frac{1}{2}$

Ells *s.* *d.*
431 at 2 4 $\frac{1}{2}$

2 862
$\frac{1}{4}$ 107 9 *d.*
$\frac{1}{8}$ 53 10 $\frac{1}{2}$

102|3 7 $\frac{1}{2}$

Fac. 51 *l.* 3 *s.* 7 *d.* $\frac{1}{2}$

Case

Caſe 6.

19. When the given Numbers of the Integers is Pounds, then multiply the Number of Integers, whoſe Value is ſought by the Price of the Integer, and the Product is Anſwer in Pounds.

Example.

C.	l.		C.	l.
42 at	2 *per C.*		13 at	8 *per C.*
84 *l. Facit*			104 *l. Facit*	
C.	l.		C.	l.
33 at	3 *per C.*		48 at	12 *per C.*
90 *l. Facit*			576 *l. Facit*	

Caſe 7.

20 If the Price of the Integer is Pounds and Shillings, then for the Pounds work as in the laſt Rule, and for the Shillings as in the 12th and 13th Rules before-going, then add the Numbers produced from them both, and the Sum is the Value ſought.

Examples.

	C.	l.	s.
	46 at	2	4
2*l.*	92	*s.*	
4*s.*	9	4	
	101	4 *s.*	
	Groſs	*l.*	*d.*
	58 at	3	7
3*l.*	174	*s.*	
6*s.*	17	8	
1*s.*	2	18	
	194 *l.*	6 *s. Facit*	

	Groſs	*l.*	*s.*
	82 at	4	10
4*l.*	328		
10*s.*	41		
	369 *l. Facit*		
	Groſs	*l.*	*s.*
	26 at	3	16
3 *l.*	78		
15*s.*	19		10
1 *l.*	1		6
	98 *l.*		16 *s. Facit*

21. When the given Price of an Integer conſiſt of Pounds, Shillings, Pence and Farthings, then work for the Shillings, Pence, and Farthings firſt, according to the 18th Rule of this Chapter, and find the Total Value of the given Number, if there was no Pounds, then work

with the Pounds according to the 19th Rule of this Chapter, and add the Numbers thus found, and their Sum is the Total Value required.

Example of this Rule follow.

C. *l.* *s.* *d.*
213 at 1 13 4½
639
213
2569 *d.*
13 s. 53 3
3 d. 26 7½
1½ d.
284|8 10½
142 *l.* 08 *s.* 10½
1 l. 113
355 *l.* 08 *s.* 10½ *Facit*

Groſs *l.* *s.* *d.*
416 at 2 9 3¾
9 s. 3744
3 d. 104
½ d. 26
387|4
2 l. 193 *l.* 14 *s.*
832
1025 *l.* 14 *s.* *Facit*

C. *l.* *s.* *d.*
37 at 3 8 10½
296 d. | 8 s.
18 6 | 6 d.
9 3 | 3 d.
4 7½ | 1½ d.
32|8 0½ d.
16 *l.* 8 *s.* 4¼ *d.* *Facit*
111 | 3 l.
127 *l.* 8 *s.* 4½ *d.* *Facit*

Groſs *l.* *s.* *d.*
48 at 3 15 11½
240
48
720 | 15 s.
24 | 6 d.
16 | 4 d.
6 | 1½ d.
76|6
38
144 | 3 l.
182 *l.* 6 *s.* *Facit*

22. When there is given the Value of an Integer, and it is required to know the Value of many ſuch Integers together, with ¾ or ½ or ⅓ of an Integer, the firſt (by the former Rules) find out the Value of the given Number of Integers, and then for ¼ of an Integer take ¾ of the given Value of the Integer, or for ½ take ½ of the given Value of the Integer, and for ¾

firſt take the Half of the given Value, and then Half of that Half, ſetting each Part under the Precedent, then adding them together, their Sum will be the required Value of the Integers and their Parts. *Example*, What is the Value of 116 Yards, a 4 *s.* 6 *d. per* Yard? To give an Anſwer, Firſt I work for the Value of 116 Yards, by the 5th Rule foregoing, and then for the half Yards, I take half of 4 *s.* 6 *d.* which is 2 *s* 3 *d.* and add to the reſt found as before, then is that Sum the total Value of 116½ yards at 4 *s.* 6 *d. per* Yard which I find to amount to 16 *l.* 4 *s.* 3 *d.* as by the Work in the Margent. And all other Examples of this Kind, are wrought the ſame Way.

yds, *s.* *d.*	
116½ at 4 6	
11 *l.* 12 *s.*	2 *s.*
14 *l.* 10 *d.*	2 *s.* 6 *d*
23	½ *yards.*
26 4 3 *Frcit*	

Many more Queſtions may be ſtated, and ſeveral other Rules of Practice may be ſhewn according to the Methods of diverſe Authors; but what have been delivered here, are ſufficient for the Practical Arithmetician in all Caſes whatſoever.

CHAP. XXVII

The Rule of Barter.

1. BArter is a Rule among Merchants, which (in the Exchange of one Commodity for another) inform them ſo to proportion their Rates, as that neither may ſuſtain Loſs.

2. To reſolve Queſtions in Barter, will not be difficult to him that is acquainted with the Golden Rule, or Rule of Three; it being altogether uſed in reſolving ſuch Queſtions.

Queſt. 1. Two Merchants, (*viz* A and B) Barter, A hath 13 *C.* 3 *qrs.* 15 *l.* of Pepper at 2 *l.* 16 *s. per C.* and B hath Cotten at 9 *d. per l.* I demand how much B muſt give A for his Pepper?

Anſwer 9 *C.* 1 *qr.*

Firſt find by the Rule of Three, or the Rule of Practice foregoing, how much the Pepper is worth, ſaying.

If 1 *C.* coſt 2 *l.* 16 *s.* what will 12 *C.* 3 *qrs.* 14 *l.* coſt?

Anſwer, 38 *l.* 17 *s.*

Secondly, By the Rule of Three, ſay, If 9 *d.* buy 1 *l.* of Cotten how much will 38 *l.* 17 *s.* buy?

Anſwer, 9¼ *C.* and ſo much Cotten muſt *B* give to *A* for 13 *C.* 3 *qrs.* 14 *l.* of Pepper, at 2 *l.* 16 *s. per Cent.* when the Cotten is worth 9 *d. per l.*

Queſt. 2. *A* and *B* Barter, *A* hath 120 Yards of broad Cloth, worth 6 *s. per* Yard, but in the Barter he will have 8 *s. per* Yard; *B* hath Shalloon worth 4 *s. per* Yard. Now I demand how many Yards of Shalloon *B* muſt give *A* for his Broad-cloth, making his Gain in Barter equal to that of *A.*

Anſwer, 110 Yards of Shalloon.

Firſt (as in the laſt Queſtion) find out how *B* ought to ſell his Shalloon in Barter, *viz.* ſay, If 6 *s.* require 8 *s.* what will 4 *s.* require?

Anſwer, 5 *s.* 4 *d.*

Thus you ſee that *B* muſt ſell his Shalloon in Barter at 3 *s.* 4 *d.* if *A* ſell his Broad-cloth at 8 *s. per* Yard.

It remaineth now to find out how much Shalloon *B* muſt give for 120 Yards of Broad cloth, which reſolved after the Method in the firſt Queſtion of this Chapter is found to be 180, and ſo many Yards of Shalloon muſt *B* give *A* for the 100 Yards of Broad-cloth.

Queſt. 3 *A* and *B* bartered, *A* had 14 *C.* of Sugar worth 6 *d. per l.* for which *B* gave him 1 *C.* 3 *qrs.* of Cinnamon. I demand how *B* rated his Cinnamon *per l.*

Anſwer, 4 *s. per l.*

Queſt. 4. *A* and *B* Barter, *A* hath 4 Tun of Brandy, worth 37 *l.* 16 *s.* ready Money, but in Barter he hath 50 *l.* 8 *s. per* Tun, and giveth *B* 21 *C.* 2 *qrs.* 11⅚ *l.* of Ginger for the 4 Tun of Brandy, I deſire to know how much *B* ſold his Ginger in Barter *per C.* and how much it is worth in ready Money?

Anſwer, For 9 *l.* 6 *s.* 8 *d.* in Barter, and it is worth 7 l. *per Cent.* in ready Money.

Queſt. 5. *A* and *B* Barter, *A* hath 320 Dozen of Candles, at 4 *s.* 6 *d. per* Dozen, for which *B* giveth him 30 *l.* in Money, and the reſt in Cotten at 8 *d. per l.* I demand how much Cotten he muſt give him more than 30 *l.*

Anſwer, 11 *C.* 1 *qr.*

CHAP.

CHAP. XXVIII.

Queſtions in Loſs and Gain.

Q. 1. A Merchant bought 436 Yards of Broad-cloth for 8 *s.* 6 *d. per* Yard, and ſelleth it again at 10 *s.* 4 *d per* Yard; now I deſire to know how much he gained in the 436 Yards?

Anſwer 39 *l.* 12 *s.* 4 *d.*

Firſt, Find out by the Rule of Three, or by Practice, how much the Cloth coſt him at 8 *s*, 6 *d per* Yard, which I find to be 183 *l.* 6 *s.* then by the ſame Rule find out how much he ſold it for, *viz* 225 *l* 5 *s.* 4 *d.* then ſubtract 185 *l.* 6 *s.* which it coſt him, for 225 *l.* 5 *s.* 4 *d.* which he ſold it for, and there remaineth, 32 *l.* 09 *s.* 4 *d.* for his Gain in the Sale thereof.

Otherwiſe, it may ſooner be reſolved thus, firſt find out how much he gained *per* Yard, *viz.* Subtract 8 *s.* 6 *d.* which he gave *per* Yard, from 10 *s* 4 *d.* which he ſold it for *per* Yerd, the Remainder is 1 *s.* 10 *d.* for his Gain *per* Yard, Then ſay,

If one Yard gain 1 *s.* 10 *d.* what will 436 Yards gain? The Anſwer, by Practice or the Rule of Three, is 39 *l.* 19 *s.* 4 *d.* as was found before.

Queſt. 2. A Draper bought 124 Yards of Holland-cloth, which he gave 31 *l.* I deſire to know how he muſt ſell it *per* Yard to gain 10 *l.* 6 *s.* 8 *d.* in the whole Sale of 124 Yards?

Anſwer. At 6 *s.* 8 *d. per* Yard.

Add the Price which it coſt him, (*viz.* 31 *l.*) to his intended Gain, (*viz.* 10 *l.* 6 *s.* 8 *d.*) the Sum is 41 *l.* 6 *s.* 8 *d.* Then ſay,

If 124 Yards require 41 *l.* 6 *s.* 8 *d.* what will 1 Yd require? By the Rule of Three, I find the Anſwer 6 *s.* 1 *d.*

Queſt. 3. A Grocer bought 3 *C.* 1 *qr.* 13 *l.* of Cloves, which coſt him 2 *s.* 4 *d. per l.* and ſold them for 52 *l.* 14 *s.* I deſire to know how much he gained in the Whole?

Anſwer 8 *l.* 12 *s.*

Queſt 4. A Draper bought 86 Kerſeys for 129 *l.* I demand how he muſt ſell them *per* Piece to gain 15 l. in laying out 100 *l.* at that rate? *Anſwer* 1 *l.* 14 *s.* 6 *d. per* Piece; for, As 100 is to 115 *l.* ſo is 129 *l.* to 148 *l.* 7 *s.*

So that by the Proportion above, I have found how much he muſt receive for the 86 Kerſeys, to gain after the Rate of 15 *per C.* Then to find how he muſt ſell them *per* Piece, I ſay,

As 86 Pieces are to 141 *l.* 7 *s.* ſo is one Piece to 1 *l.* 4 *s.* 6 *d.* which is the Nnmber ſought.

Queſt. 5. A Grocer bought $4\frac{1}{4}$ *C.* of Pepper for 15 *l.* 17 *s.* 4 *d.* and it proving to be damnified) is willing to loſe 12 *l.* 10 *s.* *per Cent,* I demand how he muſt ſell it *per l.*

Anſwer. 7 *d.* *per l.*

Subtract 12 *l.* 10 *s.* the Loſs of 100 *l.* from 100 *l.* and there remains 87 *l.* 10 *s.* Then ſay,

As 100 *l.* is to 87 l. 10 s. ſo is 15 l. 17 s. 4 d. to 13 l. 17 s. 8 d. and ſo much he muſt ſell it all for, to loſe after the Rate propounded; Then to know how he muſt ſell it per *l.* I ſay,

As 13 l. 17 s. 6 d. is to $4\frac{1}{4}$ *C.* ſo is 1 l. to 7 d.

Queſt. 6. A Plummer ſold 10 Fodder of Lead (the Fodder containing 19 $\frac{1}{2}$ *C.*) for 204 l. 10 s. and gained after the Rate of 12 l. 10 s. *per* 100 l. I demand how much it coſt him *per C?*

To reſolve this Queſtion, add 12 *l.* 10 s. (the Gain *per Cent.*) to 10 l. and it makes 112 l. 10 s. Then ſay,

As 112 l 10 s. is to 100 l. ſo is 204 l. 15 s. to 182 l. which 182 l. is the Sum it coſt him in all; then reduce your 10 Fodders to Half Hundreds, and it makes 390. Then ſay,

As 390 Half Hundreds is to 182 l. ſo is 2 Half Hundreds to 18 s. 8 d. the Price of two Half Hundreds, or 1 *C. wt.* and ſo much it ſtood him in *per. C. wt.*

Queſt. 7. A Merchant bought eight Tuns of Wine, which being ſophiſticated, he ſelleth for 400 l. and loſeth after the Rate of 12 l. in receiving 100 l. Now I demand how much it coſt him *per* Tun, and how he ſelleth it *per* Gallon to loſe after the ſaid Rate?

Anſwer. It coſt him 56 l. *per* Tun, and he muſt ſell it at 3 s. 11 d. $\frac{10}{21}$ *qrs. per* Gallon, to loſe 12 l. in receiving 100 l.

To reſolve this Queſtion, I conſider in the firſt Place, that in receiving 100 *l.* he loſeth 12 l. therefore 100 l. comes in for 112 l. laid out; wherefore to find out how much he laid out for the whole, I ſay,

As 100 l. is to 112 l. ſo is 400 l. to 448 l. and ſo much the 8 Tun coſts him: Then to find out how much it coſt *per* Tun, I ſay,

As 8 is to 448 l. ſo is 1 to 56 l. the Price it coſt *per* Tun.

8 Now to find how he muſt ſell it *per* Gallon, reduce the Tuns into Gallons, make 2016. Then ſay.

As 2016 Gallons is to 400 l, ſo is 1 Gallon to 3 s. 11 d. $2\frac{1}{20}$ *qrs.* the Price he muſt ſell it at *per* Gallon to loſe as aforeſaid.

Queſt. 8. A Merchant bought 8 Tuns of Wine, which being ſophiſticated, he is willing to ſell for 400 l. and loſeth at that Rate 12 l. in laying out 100 l. upon the ſame now I demand how much it coſt him *per* Tun?

Here I conſider that for 100 l. laid out, he received but 88 l. wherefore to find what 8 Tuns coſt him, I ſay,

As 88 l. is to 100 l. ſo is 400 l. to $454\frac{6}{11}$ the Price it all coſt him; then to find out how much *per* Tun. I ſay,

As 8 is to $464\frac{6}{11}$, ſo is 1 to $56\frac{2}{11}$, or 56 l. 16 s. 4 d. $2\frac{5}{11}$ *qrs, per* Tun.

CHAP. XXIX.

Equation of Payments.

1. EQuation of Payments is that Rule among Merchants, whereby we reduce the Times for Payment of ſeveral Sums of Money to an equated Time for Payment of the whole Debt, without Damage to Debtor or Creditor; and,

The Rule is,

2. Multiply the Sums of each particular Payment by its reſpective Time, then add the ſeveral Products together, and their Sum divide by the total Debt, and the Quotient thence ariſing is the equated Time, for the Payment of the Whole Debt. *Example.*

Queſt. 1. A is indebted to B in the Sum of 130 l. whereof 50 l. is to be paid at 2 Months, and 50 l. at 4 Months, and the reſt at 6 Months, now they agree to make one Payment of the total Sum; the Queſtion is, What is the equated Time for Payment, without Damage to Debtor or Creditor?

To reſolve this Queſtion, I multiply each Payment by its Time, *viz.*

50 l. Multiply'd by 2 Mon. produceth ———— 100
50 l. Multiply'd by 4 Mon. produceth ———— 200
30 l. Multiply'd by 6 Mon. produceth ———— 180

The Sum of the Product is —— 480

Then I divide 480 (the Sum of the Products) by 130 (the total Debt) and the Quotient is 3 $\frac{9}{11}$ Months for the Time of paying the whole Debt.

Queſt. 2. A Merchant hath owing him 1000 l. to be paid as followeth, *viz* 600 l. at 4 Months, 200 l. at 6 Months, and the reſt (which is 200 l.) at 12 Months, and he agreeth with the Debtor to make one Payment of the whole, I demand the Time of Payment without Damage to Debtor or Creditor?

600 l. Multiply'd by 4 Months is ———— 2400
200 l. Multiply'd by 6 Months is ———— 1200
200 l. Multiply'd by 12 Months is ———— 2400

The Sum of the Products is —— 6000

and the Sum of the Products (6000) being divided by the whole Debt (1000 l.) quotes 6 Months for the Time of Payment of the whole Debt.

3. The Truth of the Rule is thus manifeſt, if the Intereſt of that Money which is paid by the equated Time (after it is due, be equal to the Intereſt of that Money, which by the equated Time) is paid ſo much ſooner than it is due at any rate *per C.* then the Operation is true, otherwiſe not. Example.

The Proof of the Rule of Equation of Payments.

In the laſt Queſtion 600 l. ſhould have been paid at 4 Months, but is is not diſcharged till 6 Months, (that is 2 Months after it is all due) wherefore its Intereſt of 2 Months at 6 *per Cent. per Annum* is 6 l. and then 200 l.

was to be paid at 6 Months, which is the equated Time for its Payment, therefore no Intereſt is reckoned for it; but 200 l. ſhould have been paid at 12 Months, but is paid at 6 Months, which is 6 Months ſooner than it ought, wherefore the Intereſt of 200 l. for 6 Months is 6 l. (eccounting 6 l. *per Cent. per Annum*) which is equal to the Intereſt of 600 l. for 2 Months, wherefore the Work is right.

Queſt. 3. A Merchant hath owing him a certain Sum to be diſcharged at 3 equal Payment, *viz.* $\frac{1}{3}$ at two Months, $\frac{1}{3}$ at four Months, and $\frac{1}{3}$ at eight Months, the Queſtion is, What is the equated Time for the Payment of the whole Debt?

In Queſtions of this Nature, (*viz.* where the Debt is divided into unequal Parts) each of its Parts is to be multiply'd by its Time, and the Sum of the Product is the Anſwer.

$\frac{1}{3}$ multiply'd by 2 Mon. produceth $\frac{7}{8}$
$\frac{1}{3}$ multiply'd by 4 Mon. produceth $1\frac{1}{3}$
$\frac{1}{3}$ multiply'd by 8 Mon. produceth $2\frac{2}{4}$

The Sum of the Product is $4\frac{2}{3}$

which is $4\frac{2}{3}$ Months for the equated Time of Payment.

If inſtead of the Fractions repreſenting the Parts, you had wrought by the Numbers themſelves (repreſented by thoſe Parts) according to the firſt and ſecond Example, it would have been the ſame Anſwer; and ſuppoſe the Debt had been 90 l. then $\frac{1}{3}$ of it is 30 l. for each Payment, *viz.* at 2, 4, and 8 Months. Then,

30 l. multiply'd by 2 Mon. produceth 60
30 l. multiply'd by 4 Mon. produceth 120
30 l. multiply'd by 8 Mon. produceth 240

The Sum of the Product is 420

which divided by 90 (the whole Debt) quoteth $4\frac{60}{90}$, or $4\frac{1}{3}$ Months as before.

Queſt. 4. A Merchant oweth a Sum of Money to be paid $\frac{1}{2}$ at 5 Months, and $\frac{1}{4}$ at 8 Months and $\frac{1}{4}$ at 10 Months, and he agreeth with his Creditor to make one total Payment; I demand the Time without Damage to Debtor or Creditor; Work as in the laſt Queſtion, and you will find the Anſwer to be 7 Months.

Queſt. 5. *A* is indebted to *B* 640 l. whereof he is to pay 40 l. preſent Money, 350 l. at 3 Months, and the reſt, *viz.* 250 l. at 8 Months, and they agree to make an equated Time for the whole Payment, now I demand the Time?

In Queſtion of this Nature, *viz.* where there is ready Money paid) you are multiplying to neglect the Money that is to be paid preſent, and work with the reſt, as is before directed, and divide the Sum of the Products by the whole Debt, and the Quote is the Anſwer; for here 40 l. is to be paid preſent, and hath no Time allowed; and according to the Rule it ſhould be multiplied, by its Time, which is 0; therefore 40 Times 0 is 0, which neither augmenteth nor diminiſheth the Dividend; wherefore to proceed (according to Direction) I ſay,

353 by 3 Months, produceth ——— 1050
250 by 8 Months, produceth ——— 2000

The Sum of the Product is 3050

which divided by 640, the whole Debt, the Quote is $4\frac{40}{64}$ Months, the Time of Payment.

Queſt. 6. *A* is indebted to *B* in a certain Sum, half whereof is to be paid preſent Money, one 3d at 6 Months, and the reſt at 8 Months; now I demand the equated Time for Payment of it all?

Anſwer. $3\frac{1}{2}$ Months is the Time of Payment.

Queſt. 7. *A* is indebted to *B* 120 l. whereof $\frac{1}{3}$ is to be paid at 3 Months, $\frac{1}{4}$ at 6 Months, and the reſt at 9 Months What is the equated Time for the Payment of the whole Sum?

Anſwer. At 6 Months?

Queſt. 1. *A* is indebted to *B* 420 l. which is due at the End of 6 Months, but *A* is willing to pay him 140 l. preſent provided he can have the Remainder forborn ſo much the longer, to make Satiſfaction for his Kindneſs; which is agreed upon, I deſire to know what Time ought to be allotted for the Payment of the 280 l. remaining?

The Operation of this Queſtion is left to the Learner, to try his Genious; and who, in this Caſe, muſt have an Eye to the Rule of Three.

CHAP. XXX.

EXCHANGE.

1. THE Rule of Exchange informeth the Merchants how to exchange Monies, Weights, or Meaſures of one Country into (or for) the Monies, Weighss, or Meaſures of another Country, and when the Rate, Reaſon or Proportion betwixt the Money, Weights or Meaſures of different Countries is known, it will not be difficult for the Practitioner that is well acquainted with the Rule of Proportion (or Rule of Three) to reſolve any Queſtion, wherein it is required to exchange a given Quantity of the one Kind into the ſame Value of another Kind.

2. In Queſtion of Exchange there is always a Compariſon made between the two Coins, &c. of two Countries (or Kinds) or of more.

3. In Queſtions were there is a Compariſon made between two Things, (whether they be Monies, Weights, &c. of different Kinds, there may be a Solution found by a ſingle Rule of Three, as by the following Example.

Queſt. 1. A Merchant at *London* deliver'd 370 *l.* *Ster.* to receive the ſame at *Paris* in *French* Crowns, the Exchange $3\frac{1}{3}$ *French* Crowns *per l.* *Sterling*, I demand how many *French* Crowns he ought to receive?

In placing the Numbers, obſerve the 6th Rule of the 11th Chapter, which being done, the given Number will ſtand thus:

l. Crowns l.
1 ———— $3\frac{1}{3}$ ———— 370

and being reduced according to the Rules of the 12th Chapter, will ſtand thus:

As $\frac{1}{1}$ is to $\frac{10}{3}$, ſo is $\frac{307}{1}$ to $1233\frac{1}{3}$,

So that I conclude he ought to receive $1233\frac{1}{2}$ *French* Crowns at *Paris* for his 370 l. delivered at *London*.

Queſt. 2. A Merchant delivered at *Amſterdam* 587 l. *Flemiſh*, to receive the Value thereof at *Naples* in Ducats, the exchange 4$\frac{4}{5}$ Ducats *per l. Flemiſh*. I demand how many Ducats he ought to receive?

The Proportion is as followeth.

l. Ducats. l. Ducats.

As 1 is to $\frac{24}{4}$, ſo is $\frac{587}{1}$ to 2817$\frac{1}{5}$

So I find he ought to receive 2817$\frac{1}{5}$ Ducats at *Naples* for the 587 *l. Flemiſh* delivered at *Amſterdam*.

Queſt. 3. A Merchant at *Florence* delivered 2478 Ducatoons, to receive the Value at *London* in Pence, the Exchange at 53 $\frac{1}{2}$ *Sterl. per* Ducatoon; I demand how much *Sterling* he ought to receive?

The Proportion for Reſolution is

Duc. d. Duc. d.

As $\frac{1}{2}$ is to $\frac{107}{10}$ ſo is $\frac{3478}{1}$ to 186073.

which is equal to 775 *l.* 6 $\frac{1}{2}$ for the Anſwer.

4. When there is a Compariſon made between more than two different Coins, Weights, or Meaſures, there ariſeth ordinarily two different Caſes from ſuch a Compariſon.

1. When it is required to know how many Pieces of the firſt Coin, Weight or Meaſure, are equal in Value to a known Number of Pieces of the laſt Coin, Weight or Meaſure.

2. When it is required to find out how many Pieces of the laſt Coin, Weight, or Meaſure, are equal in Value to a given Number of the firſt ſort of Coin, Weight, or Mea-

An Example of the firſt Caſe may be this, viz.

Queſt. 4. If 150 Pence at *London* are equal to 3 Ducats at *Naples*, and 4$\frac{4}{5}$ Ducats at *Naples* make 34$\frac{1}{2}$ Shillings at *Bruſſels*; then how many Pence at *London* are equal to 139 *s.* at *Bruſſels*? *Facit*, 960 *d.*

The Queſtion may be reſolved by two ſingle Rules of Three: For firſt I ſay,

If $\frac{1}{3}$ Ducats at *Naples* make 150 *d* at *London*, how many Pence will 3$\frac{4}{5}$ Ducats make? *Anſ.* 240 *d.*

By the foregoing Proportion we have diſcovered that 4$\frac{4}{5}$ Ducats at *Naples* make 240 Pence at *London*; and by the Tenor of the Queſtion we ſee that 4$\frac{4}{2}$ Ducats at *Venice* make 35 $\frac{1}{2}$ Shillings at *Bruſſels*, therefore 240 *d.* at *London* are equal to 34$\frac{1}{2}$*s.* at *Bruſſels*, (for the Things that are equal to one and the ſame Thing, are alſo equal to one another) wherefore we have a Way laid open to give a Solution to this Queſtion by another Single Rule of Three, whoſe Proportion is,

As 34 ½ *s* at *Bruſſels* is to 240 *d.* at *London*, ſo is 131 *s.* at *Bruſſels* to 960 *d.* at *London*; which is the Anſwer to the Queſtion.

An Example of the ſecond Caſe may be this, viz.

Queſt. 5. If 40 l. *Averdupois weight* at *London* is equal to 36 l. weight at *Amſterdam*, and 90 l. at *Amſterdam* makes 116 l. at *Dantzick*, then how many Pounds at *Dantzick*, are equal to 122 l. *Averdupois-weight* at *London l.* *Anſwer.* $129\frac{24}{1}$ l. at *Dantzick.*

This Queſtion is likewiſe anſwered by two ſingle Rules of Three, *viz.* Firſt, I ſay,

As 36 l. at *Amſterdam* is to 46 l. at *London.*

So is 90 l. at *Amſterdam* to 100 l. at *London.*

And by the Queſtion you find that 90 l. at *Amſterdam*, is 116 l. at *Dantzick*; and therefore 100 at *London* is likewiſe equal thereunto; wherefore again I ſay,

As 100 l. at *London* is to 116 l. at *Dantzick.*

So is 112 l. at *London* to $129\frac{21}{25}$ l. at *Dantzick.*

By which I find that $129\frac{22}{25}$ l. at *Dantzick* are equal to 112 *Averdupois-weight* at *London.*

5. There is a more ſpeedy Way to reſolve ſuch Queſtions as are contained under the two Caſes before mention'd, laid down by Mr. *Kerſey* in the 3d Chapter of his Appendix to *Wingate*'s Arithmetick, where he hath given two Rules for the Reſolution of the Queſtions pertinent to the two ſaid Caſes.

6. But I ſhall lay down a general Rule for the Solution of both Caſes; and 1ſt, Let the Learner obſerve the following Directions in placing of the given Terms, *viz.*

7. Let there be made two Columns, and in theſe Columns ſo place the given Terms one over the other, as that in the ſame Column there may not be found two Terms of the ſame Kind one with the other.

Having thus placed the Terms, the general Rule is,

Obſerve which of the ſaid Columns, hath the moſt Terms placed in it, and multiply all the Terms therein continually, and place the laſt Product for a Dividend;

then multiply the Terms in the other Column continually, and let the laſt Product be a Diviſor; then divide the ſaid Dividend by the ſaid Diviſor, and the Quotient thence ariſing will be the Anſwer to the Queſtion.

So the Example of the firſt of the ſaid Caſes being again repeated, *viz.* If 150 Pence at *London* make 3 Ducats at *Naples*, and $4\frac{4}{5}$ Ducats at *Naples* make $34\frac{1}{2}$ Shillings at *Bruſſels*, then how many Pence at *London* are equal to 131 Shillings at *Bruſſels*;

The Term being placed according to the 7th Rule will ſtand as followeth:

	A	B	
Pence at *Lond.*	150	3	Ducats at *Naples.*
Ducats at *Nap*	$4\frac{1}{5}$	$34\frac{1}{2}$	Shillings at *Bruſſels.*
Shill. at *Bruſſ*	138		

Having thus placed the Terms, that in neither Column there is two Terms of one Kind, then obſerve that the Column under A hath moſt Terms in it, therefore they muſt be multiplied together for a Dividend, *viz* 150 multiplied by $4\frac{4}{5}$ produceth $\frac{3600}{5}$, which multiplied by 138, produceth $\frac{496800}{5}$, for a Dividend then in the Column under B there are 3, and $34\frac{1}{2}$, which multiply'd together produce $\frac{207}{2}$, the Quotient is 960 Pence for the Anſwer as before.

Again, Let the Example of the ſecond Caſe be again repeated, *viz.* If 40 *l. Averdupois-weight* at *London* make 36 *l.* Weight at *Amſterdam*, and 90 *l.* at *Amſterdam* make 116 at *Dantzick*, then how many Pounds at *Dantzick* are equal to 112 *l. Averdupois-weight* at *London*?

The Terms being diſpoſed according to the 7th Rule foregoing will ſtand thus:

l. at *London*	40	36	*l.* at *Amſterdam.*
l. at *Amſterdam*	90	116	*l.* at *Dantzick.*
		112	*l.* at *London.*

whereby I find that the Terms under B multiplied together produce 497712 for a Dividend, and the Terms under A, *viz.* 40 and 90, produce 3600 for a Diviſor, and Diviſion being finiſhed, the Quotient giveth $129\frac{3312}{3600}$ Pounds, *Dantzick* for the Anſwer.

CHAP.

CHAP. XXXI.

Single Poſition.

1. NEgative Arithmetick, called the *Rule of Falſe*, is that by which we find out a Truth, by Numbers invented or ſuppoſed, either Single or Double.

2. The Rule of Single Poſition, is, when at once, *viz.* by one falſe Poſition, or feigned Number, we find out the true Number ſought.

3. In the *Single Rule of Falſe*, when you have made choice of your Poſition, work it according to the Tenor of the Queſtion, as if it were the true Number ſought; and if by the ordering your Poſition you find either the Reſult too much or too little, you may then find out the Number ſought by this Proportion following, *viz.*

As the Reſult of you Poſition into the Poſition, ſo is the given Number to the Number ſought.

Example.

Queſt. 1. A Perſon having about him a certain Number of Crowns, ſaid, If a 4th, 3d, and 6th of them were added together, they would make juſt 45 *l.* now I demand the Number of Crowns he had about him?

Anſwer 60 Crowns.

To reſolve this Queſtion, I ſuppoſe he had 24 Crowns (or any other Number that will admit of the like Diviſion) now the 4th of 24 is 6, and the 3 is 8, and the 6th is 4 all which Parts, (6, 8, and 4) being added together, make but 18, but it ſhould be 45, wherefore I ſay by the *Rule of Three*.

As 18 the Sum of the Parts is to the Poſition 24, ſo is 45 the given Number to 60 the true Number ſought.

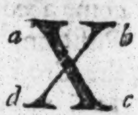
For the 4th of 60 is 15, and the 3d of 60 is 20, and the 6th of 60 is 10, which added together make 45.

CHAP. XXXII.

Double Poſition.

1. THE Rule of double Poſition is when two falſe Poſitions are aſſumed to give a Reſolution to the Queſtion propounded.

2. When any Queſtion is ſtated in double Poſition, make ſuch a Croſs as in the Margent.



3. Then make choice of any Number you think may be convenient for your working, which call your firſt Poſition, and place it at the End of the Croſs at *a*; then work with this Poſition, and it were the true Number ſought, according to the Nature of your Queſtion; then having found out your Error, either too much or too little, place it on that Side the *d*, then make choice of another Number of the ſame Denomination with the firſt Poſition (which call your ſecond Poſition) and place it on the Side of the Croſs at *b*; then work with this Poſition as with the former, and having found out your Error, either too much or too little, place it on that Side of the Croſs at *c*; and then the Poſitions will ſtand at the Top of the Croſs, and the Errors at the Bottom, each under his correſpondent Poſition, and then multiply the Errors into the Poſition croſs-wiſe, that is, multiply the firſt Poſition by the ſecond Error, and the ſecond Poſition by the firſt Error, and put each Product over its Poſition.

4. Having proceeded ſo far, then conſider whether the Errors are both alike, that is, whether they are both too much, or both too little; and if they are alike; then ſubtract the leſſer Product from the greater; and ſet the Remainder for a Dividend; then ſubtract the leſſer Error from the greater, and let the Remainder be a Diviſor, and the Quotient ariſing by this Diviſion is the Anſwer to the Queſtion.

5. But if the Errors are unlike, that is one too much and the other too little, then add the Products of the Poſitions and Errors together, and their Sum ſhall be a Dividend, then add the Errors together, and their Sum ſhall

be a Diviſor, and the Quotient ariſing hence is the Anſwer.

Queſt. 1. *A*, *B*, and *C* built a Houſe, which coſt 76 *l.* of which *A* paid a certain Sum unknown, *B* paid as much as *A*, and 10 *l.* over, and *C* as much as *A* and *B* : Now I deſire to know each Man's Share in that Charge ?

Having made a Croſs according to the ſecond Rule, I come according to the 3d Rule to make choice of my firſt Poſition, and here I ſuppoſe *A* paid 6 *l.* which I put upon the Croſs as you ſee, then *B* paid 16 *l.* (for its ſaid he paid 10 *l.* more than *A*) and *C* paid 22 *l.* (for it's ſaid he paid as much as *A* and *B*) then I add their Parts.

l.		*l.*
9		*A* 6
19		*B* 16
28	120 168 288	*C* 22
—	6 X 9	—
56	2) (14	Sum 44
	32 20	
76	12	76
56		44
—		—
20		Error 32

And they amount to 44, but it is ſaid they paid 76 *l.* wherefore there is 32 too little, which I note down at the Bottom of the Croſs under its Poſition for the firſt Error.

2dly, I ſuppoſe *A* paid 9 *l.* then *B* paid 19 *l.* and *C* 28 *l.* all which add together make 56, but they ſhould make 76, wherefore the Error of this Poſition is 20, which I put at the Bottom of the Croſs under its Poſition for the 2d Error ; then I multiply the Errors and Poſition Croſs-wiſe *viz.* 32 (the Error of the firſt Poſition) by 9 (the 2d Poſition) and the Product is 288. Then I multiply 20, (the Error of the ſecond Poſition) by 6 (the firſt Poſition) and the Product is 120.

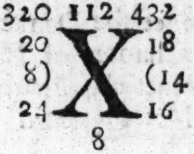
Then (according to the 4th Rule) I ſubtract the leſſer Product from the greater, *viz.* 120 from 288, becauſe the Errors are both alike, (*viz.* too little) and there remaineth 168 for a Dividend; then I ſubtract 22 (the leſſer Error) from 32, the greater Error, and the Remainder is 12 for a Diviſor; then I divide 168 by 12, and the Quotient is 14 for the Anſwer, which is the Share of A in the Payment.

6. Again, 2dly, If the Errors had been both too big, it had had the ſame Effect, as appeareth by the following Work; for firſt, I ſuppoſe A paid 20 l. then B paid 30 l. and C 50 l. which in all is 100 l. but it ſhould have been no more than 76, wherefore the firſt Error is 24 too much. Again, I ſuppoſe A paid 18 l. then B muſt pay 28 l. and C muſt pay 46 l. which in all is 92 l. but it ſhould have been but 76.

20 A
30 B
50 C

100 Sum
76 Subtr.

24 Error



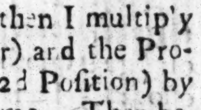
A 18
B 28
C 46

Sum 92
Subtr. 76

Error 16

wherefore the 2d Error is 16 too much; then I multiply 20 (the firſt Poſition) by 16 (the 2d Error) and the Product is 320; again, I multiply 18 (the 2d Poſition) by 24 (the firſt Error) and the Product is 432. Then becauſe the Errors are both too much, I ſubtract 320 (the leſſer Product) from 432 (the greater Product) and there remaineth 112 for a Dividend; likewiſe I ſubtract 16 (the leſſer Error) from 24 (the greater Error) and the Difference is 8 for a Diviſor; then perform Diviſion, and the Quotient is 14, as before for the Anſwer.

Again, 3dly, If the Errors had been the one too big, and the other too little, Reſpect being had to the fifth Rule foregoing, the Anſwer would have been the ſame; as thus, I take for my firſt Poſition 6, and then the Error is 32 too little; then I take for my ſecond Poſition 18, and then the Error is 16 too much; then I multiply the Poſitions and Errors croſs-wiſe, and the Product are 96 and 576, and becauſe the Errors are unlike, *viz.* one too big, and another too little, I add the Product 26 and 576 together,



ther, and their Sum is 672 ſor a Dividend; I likewiſe add the Errors 32 and 16 together, and their Sum is 48 for a Diviſor; then having finiſhed Diviſion, I find the Quotient to be 14, which is the Anſwer, as was found out at the two ſeveral Trials before.

For Proof of the Work, I ſay,
If A paid ———————————— 14
Then B paid 14 and 10 (that is) —— 24
Then C paid 14 and 24 (that is) —— 38

The Sum of all is —— 76

which is the total Value of the Building, and equal to the given Number.

Thoſe who deſire to ſee the Demonſtration of this Rule, let them read the 7th Chapter of Mr. *Kerſey*'s Appendix to Mr. *Wingate*'s Arithmetick, *Petiſeus* in the 5th Book of his *Trigonometria*, or Mr. *Oughtred* in his *Clavis Mathmetica.*

Queſt. 2. Three Perſons A, B, and C, thus diſcourſed together concerning their Age; quoth A, I am 18 Years of Age; quoth B, I am as old as A and half C; and quoth C, I am as old as you both, if your Years were added together. Now I deſire to know the Age of each Perſon?

Anſwer, A is 18, B is 54 and C is 72 Years of Age.

Queſt. 3. A Father lying at the Point of Death, left to his three Sons, *viz* A, B, and C, all his Eſtate in Money, and divided it as followeth, *viz.* to A he gave half wanting 44 l. to B, he gave $\frac{1}{3}$ and 24 l. over, and to C he gave the Remainder, which was 83 l. leſs than the Share of B; now I demand what was the Sum left, and each Man's Part?

Anſwer. The Sum bequeathed was 588 l. wherefore A had 250 l. B had 210 l. and C had 128 l.

Queſt. 4. Two Perſons, *viz.* A and B had each in their Hands a certain Number of Crowns, and A ſaid to B, If you give me one of your Crowns, I ſhall have five times as many as you; and ſaid B to him again, If you give me one of yours, then we ſhall each of us make an equal Number; now I demand how many Crowns had each Perſon?

Anſwer. A had 4, and B had two Crowns.

Queſt. 5. What Number is that unto which if I add 1—4th of it ſelf, and from the Sum ſubtract 1—8th of it ſelf, the Remainder will be 216?

Anſwer. 192.

Many more Queſtions may be added, but theſe well underſtood, will be ſufficient, (even from the meaneſt Capacity) for the Reſolution of any other Queſtion pertinent to this Rule.

There may be an Objection made, becauſe we have not treated particularly upon Intereſt and Rebate; but the Operation of ſuch Queſtions being more applicable to Decimals, are omitted, till we come to acquaint the Learner therewith.

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